



Evaluating Construction Projects by a New Group Decision-Making Model Based on Intuitionistic Fuzzy Logic Concepts

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ABSTRACT

Selecting an appropriate project is a main key for contractors to increase their profits. In practice, in this area the uncertainty and imprecise of the involved parameters is so high. Therefore, considering fuzzy sets theory to deal with uncertainty is more appreciate. The aim of this paper is to present a multi-criteria group decision-making model under an intuitionistic fuzzy environment. The weight of each decision maker and each criterion are considered different. Indeed, decision makers' weights are determined based on a new intuitionistic fuzzy index, and criteria' weights are specified by proposed decision method according to the concept of closer to ideal solution and farther from negative ideal solution. Then, the potential projects are ranked based on new intuitionistic fuzzy relative closeness coefficient. Thus, the proposed intuitionistic fuzzy group decision-making model is applied in an illustrative example about construction project selection from the recent literature. Finally, the ranking results are compared with a fuzzy TOPSIS method to indicate the applicability and efficiency of the proposed model.

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1. INTRODUCTION

Since Zadeh [1] introduced fuzzy sets theory, this theory and their extensions have been widely applied in solving the problems which have uncertain parameters. These problems are regarded in some fields such as artificial intelligence [2, 3], management [4, 5], pattern recognition [6, 7] and decision making [8-10]. Decision making is a procedure which is defined as final result of problems and assist decision makers for choosing the best potential candidates or set of potential candidates.

The multi-criteria decision making (MCDM) has established an efficient framework for evaluation of the problems which have been judged by multiple decision makers. In traditional MCDM methods, the evaluations of problems are provided based on crisp values, but in an uncertain situation the problems should be judged based on the fuzzy sets theory, and on the other hand it

could be considered as fuzzy multi-criteria decision making (FMCDM) approach [e.g., 11-13]. In addition, employing some decision makers under a group to assess the problem under imprecise condition is leading to fuzzy multi-criteria group decision-making (FMCGDM) approach.

In real world, the parameters have been considered uncertain/vague because decision makers cannot express their preferences and judgments by a crisp value. Thus, the decision makers' judgments for constructing the decision matrix and criteria' weights should be better to be defined by fuzzy values [8, 14, 15], such as interval values [16-19], hesitant fuzzy sets [20-23], linguistic terms [24, 25], and intuitionistic fuzzy sets [26-28]. A few studies have considered the group decision-making methods in fuzzy conditions. Hence, they considered fuzzy approaches which are based on Zadeh's fuzzy set. Thus, in this fuzzy set theory, the membership degree for an object x is $\mu(x)$ and the non-membership degree is $1 - \mu(x)$ automatically. In addition, the membership degree integrates the preferences for x and against x . In real-life

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conditions, information about objects is fitting to a fuzzy concept which may be insufficient and incomplete. Therefore, the sum of the membership and non-membership degrees may be less than one [29, 30]. In Zadeh’s fuzzy set, no tools are existed to incorporate the membership degree when we have faced with lack of knowledge [30, 31]. In this respect, Atanassov [26, 32] introduced an appropriate solution called intuitionistic fuzzy set as a generalization of the Zadeh’s fuzzy set which the membership grades are ill-known. The intuitionistic fuzzy sets theory appears to be well suited for defining the preferences values of decision makers in decision-making problems and its applications [30, 31]. In this respect, numerous authors focused on fuzzy sets theory and its extension to overcome the existed uncertain parameters in their decision-making problems [18, 33, 34].

The fuzzy sets theory can be utilized in construction problems by considering their main advantages because the uncertainty of involved parameters in these problems can be high. In this respect, some authors have utilized the fuzzy sets theory for the assessment and have solved their construction problems [35-37]. In this respect, Gu et al. [38] proposed a modified TOPSIS method based on interval-valued intuitionistic fuzzy set to select the best bridge construction project, in which the criteria’ weights were completely known. Ning and Wang [39] presented an intuitionistic fuzzy TOPSIS method to assess the best site layout problem to select the most suitable site layout from the site layout candidates. Zhou et al. [40] developed the combined TOPSIS method with grey system theory based on intuitionistic triangular fuzzy numbers to rank the green risks in construction projects.

In this study, a new intuitionistic fuzzy group decision procedure is presented to select the most appropriate project in construction industry. In proposed model, the weights of criteria and decision makers are determined by proposed compromise solution and new intuitionistic fuzzy index, respectively. In addition, decision makers evaluate the project’s candidates versus the conflicted criteria based on linguistic terms, which converted to intuitionistic fuzzy numbers. The main contributions of this study are outlined as follows: (1) a novel group decision making method is proposed based on the intuitionistic fuzzy logic; (2) the relative importance of each decision maker is computed by a new intuitionistic fuzzy index; (3) the criteria’ weights are determined by developed compromise solution in an intuitionistic fuzzy setting; and (4) an intuitionistic fuzzy relative closeness coefficient is proposed for each candidate to rank the potential projects.

The reminder of this paper is structured as follows: In section 2, the proposed model is presented to solve the group decision-making problems. Hence, in section 3, an illustrative example about the construction project is provided to show the suitability of the proposed

model. Finally, some concluding remarks and future direction are presented in section 4.

2. PROPOSED INTUITIONISTIC FUZZY DECISION MODEL

A decision-making problem can be demonstrated in a decision matrix, in which x_{ij} as an element can be indicated the assessment of the i th alternative (A_i) regarding to j th criterion (C_j). This study will develop the classical group decision matrix to intuitionistic fuzzy group decision matrix (R) based on the opinions of a group of experts. Let A_i be a set of candidates and let C_j be a set of attributes, where $A_i = \{A_1, A_2, \dots, A_m\}$ and $C_j = \{C_1, C_2, \dots, C_n\}$. The properties of the candidate are expressed by the IFS, indicated as below:

$$A_i = \{(C_1, \mu_{i1}, \nu_{i1}), (C_2, \mu_{i2}, \nu_{i2}), \dots, (C_n, \mu_{in}, \nu_{in})\}, i = 1, 2, \dots, m \quad (1)$$

where the satisfaction degree of candidates versus the attributes are denoted by μ_{ij} , and ν_{ij} represented the non-satisfaction degree of candidates versus the attributes $C_j (\mu_{ij}, \nu_{ij}), i = 1, 2, \dots, m; j = 1, 2, \dots, n$.

However, the proposed model is explained to determine the weight of each attribute and experts, and also rank the potential candidates which are provided as follows:

Step 1. Establish a group of experts to determine the attributes and specify the prospective candidates for the group decision-making problem. The chosen attributes are defined qualitatively and assessed in linguistic terms which converted to intuitionistic fuzzy numbers.

Step 2. Calculate the weight of each expert (λ_k) based on new intuitionistic fuzzy index. In this respect, an intuitionistic fuzzy number for evaluating the k th experts is denoted by $D_k = [\mu_k, \nu_k, \pi_k]$.

$$\lambda_k = \frac{1 - \prod_{i=1}^m \prod_{j=1}^n \mu_{ij}^k + \left(\prod_{i=1}^m \prod_{j=1}^n \mu_{ij}^k - \prod_{i=1}^m \prod_{j=1}^n \nu_{ij}^k \right) \left(\frac{1 - \prod_{i=1}^m \prod_{j=1}^n \mu_{ij}^k}{1 - \prod_{i=1}^m \prod_{j=1}^n \mu_{ij}^k + \prod_{i=1}^m \prod_{j=1}^n \nu_{ij}^k} \right)}{\sum_{k=1}^K \left[1 - \prod_{i=1}^m \prod_{j=1}^n \mu_{ij}^k + \left(\prod_{i=1}^m \prod_{j=1}^n \mu_{ij}^k - \prod_{i=1}^m \prod_{j=1}^n \nu_{ij}^k \right) \left(\frac{1 - \prod_{i=1}^m \prod_{j=1}^n \mu_{ij}^k}{1 - \prod_{i=1}^m \prod_{j=1}^n \mu_{ij}^k + \prod_{i=1}^m \prod_{j=1}^n \nu_{ij}^k} \right) \right]} \quad \forall k \quad (2)$$

and $\sum_{k=1}^K \lambda_k = 1$.

Step 3. Compute the criteria’ weights by proposed compromise solution based on the concept of closer to ideal solution and farther from negative ideal solution by considering the following sub-steps.

Step 3.1. Establish the intuitionistic fuzzy decision matrix (G_j) for each criterion ($C_j; 1, 2, \dots, n$) respecting to the candidates ($A_i; 1, 2, \dots, m$) and opinions of each experts ($k; 1, 2, \dots, K$).

$$G_j = \begin{pmatrix} DM_1 & DM_2 & \dots & DM_k \\ A_1 \left(\begin{matrix} (\mu_{1j}^1, \nu_{1j}^1, \pi_{1j}^1) & (\mu_{1j}^2, \nu_{1j}^2, \pi_{1j}^2) & \dots & (\mu_{1j}^k, \nu_{1j}^k, \pi_{1j}^k) \\ \vdots & \vdots & \ddots & \vdots \\ A_m \left(\begin{matrix} (\mu_{mj}^1, \nu_{mj}^1, \pi_{mj}^1) & (\mu_{mj}^2, \nu_{mj}^2, \pi_{mj}^2) & \dots & (\mu_{mj}^k, \nu_{mj}^k, \pi_{mj}^k) \end{matrix} \right) \end{matrix} \right) \end{pmatrix} \quad \forall j \quad (3)$$

where, μ_{mj}^k is the intuitionistic fuzzy membership degree for m th candidate which judged by k th expert to establish the j th intuitionistic fuzzy decision matrix.

Step 3. 2. Determine the intuitionistic fuzzy positive/negative ideal solutions (IFPIS/IFNIS) matrixes ($A_{w_j}^+ / A_{w_j}^-$) based on the intuitionistic fuzzy decision matrix, respectively.

$$A_{w_j}^+ = \left(\left[(\mu_i^{*k}, \nu_i^{*k}, \pi_i^{*k}) \right] \right)_{m \times k} \\ = \begin{pmatrix} DM_1 & DM_2 & \dots & DM_k \\ A_1 \left(\begin{matrix} (\mu_{1j}^{*1}, \nu_{1j}^{*1}, \pi_{1j}^{*1}) & (\mu_{1j}^{*2}, \nu_{1j}^{*2}, \pi_{1j}^{*2}) & \dots & (\mu_{1j}^{*k}, \nu_{1j}^{*k}, \pi_{1j}^{*k}) \\ \vdots & \vdots & \ddots & \vdots \\ A_m \left(\begin{matrix} (\mu_{mj}^{*1}, \nu_{mj}^{*1}, \pi_{mj}^{*1}) & (\mu_{mj}^{*2}, \nu_{mj}^{*2}, \pi_{mj}^{*2}) & \dots & (\mu_{mj}^{*k}, \nu_{mj}^{*k}, \pi_{mj}^{*k}) \end{matrix} \right) \end{matrix} \right) \end{pmatrix} \quad \forall j \quad (4)$$

$$A_{w_j}^- = \left(\left[(\mu_i^{-k}, \nu_i^{-k}, \pi_i^{-k}) \right] \right)_{m \times k} \\ = \begin{pmatrix} DM_1 & DM_2 & \dots & DM_k \\ A_1 \left(\begin{matrix} (\mu_{1j}^{-1}, \nu_{1j}^{-1}, \pi_{1j}^{-1}) & (\mu_{1j}^{-2}, \nu_{1j}^{-2}, \pi_{1j}^{-2}) & \dots & (\mu_{1j}^{-k}, \nu_{1j}^{-k}, \pi_{1j}^{-k}) \\ \vdots & \vdots & \ddots & \vdots \\ A_m \left(\begin{matrix} (\mu_{mj}^{-1}, \nu_{mj}^{-1}, \pi_{mj}^{-1}) & (\mu_{mj}^{-2}, \nu_{mj}^{-2}, \pi_{mj}^{-2}) & \dots & (\mu_{mj}^{-k}, \nu_{mj}^{-k}, \pi_{mj}^{-k}) \end{matrix} \right) \end{matrix} \right) \end{pmatrix} \quad \forall j \quad (5)$$

where the average of the intuitionistic fuzzy group decision matrix is calculated by the following relations:

$$(\mu_{ij}^{*k}, \nu_{ij}^{*k}) = \left(1 - \prod_{j=1}^n (1 - \mu_{ij}^{*k})^{\frac{1}{n}}, \prod_{j=1}^n (\nu_{ij}^{*k})^{\frac{1}{n}} \right) \quad \forall i, k \quad (6)$$

$$\pi_{ij}^{*k} = 1 - \mu_{ij}^{*k} - \nu_{ij}^{*k} \quad (7)$$

$$(\mu_{ij}^{-k}, \nu_{ij}^{-k}) = \left(\min_j \{ \mu_{ij}^k \}, \max_j \{ \nu_{ij}^k \} \right) \quad \forall i, k \quad (8)$$

$$\pi_{ij}^{-k} = 1 - \mu_{ij}^{-k} - \nu_{ij}^{-k} \quad (9)$$

Step 3.3. Compute the separation measure for each intuitionistic fuzzy decision matrix from the intuitionistic fuzzy positive/negative ideal solution matrixes by using the intuitionistic fuzzy Euclidean distance measure which denoted by S_j^* and S_j^- , respectively.

$$S_{w_j}^* = \sqrt{\frac{1}{2mk} \sum_{i=1}^m \sum_{k=1}^K \left((\mu_i^k - \mu_{ij}^{*k})^2 + (\nu_i^k - \nu_{ij}^{*k})^2 + (\pi_i^k - \pi_{ij}^{*k})^2 \right)} \quad \forall j \quad (10)$$

$$S_{w_j}^- = \sqrt{\frac{1}{2mk} \sum_{i=1}^m \sum_{k=1}^K \left((\mu_i^k - \mu_{ij}^{-k})^2 + (\nu_i^k - \nu_{ij}^{-k})^2 + (\pi_i^k - \pi_{ij}^{-k})^2 \right)} \quad \forall j \quad (11)$$

Step 3.4. Specify the intuitionistic fuzzy relative closeness of criteria (C_{w_j}) for determining the most important criterion.

$$C_{w_j} = \frac{\sqrt{\left(\prod_{j=1}^n (1 - \mu_j^{*k})^{\frac{1}{n}} + \bar{S}_{w_j}^- - 1 \right)^2}}{\sqrt{\left(\prod_{j=1}^n (1 - \mu_j^{*k})^{\frac{1}{n}} + \bar{S}_{w_j}^- - 1 \right)^2} + \sqrt{\left(\prod_{j=1}^n (1 - \mu_j^{*k})^{\frac{1}{n}} + \bar{S}_{w_j}^* - 1 \right)^2}} \quad (12)$$

where $\bar{S}_{w_j}^*$ the average of $S_{w_j}^*$ ($j = 1, 2, \dots, n$), and also the average of $S_{w_j}^-$ ($j = 1, 2, \dots, n$) represented as $\bar{S}_{w_j}^-$.

Step 3. 5. Aggregate the preferences experts' judgments about the criteria' weights (w_j^f) as follows:

$$w_j^f = (\mu_{w_j^f}, \nu_{w_j^f}, \pi_{w_j^f}) = \\ IFWA_{\lambda} (w_1^{(1)}, w_2^{(2)}, \dots, w_j^{(k)}) = \lambda_1 w_1^{(1)} \oplus \lambda_2 w_2^{(2)} \oplus \dots \oplus \lambda_k w_j^{(k)} = \quad (13)$$

$$\left[1 - \prod_{k=1}^K (1 - \mu_j^{(k)})^{\lambda_k}, \prod_{k=1}^K (\nu_j^{(k)})^{\lambda_k}, \prod_{k=1}^K (1 - \mu_j^{(k)})^{\lambda_k} - \prod_{k=1}^K (\nu_j^{(k)})^{\lambda_k} \right]$$

Step 3.6. Estimate the weight of each criterion (ϖ_j) regarding to the relative closeness.

$$\varpi_j = \frac{w_j^f C_j}{\sum_{j=1}^n w_j^f C_j} \\ = \frac{1 - (1 - \mu_{w_j^f})^{c_j} + \left((1 - \mu_{w_j^f})^{c_j} - (\nu_{w_j^f})^{c_j} \right) \left(\frac{1 - (1 - \mu_{w_j^f})^{c_j}}{1 - (1 - \mu_{w_j^f})^{c_j} + (\nu_{w_j^f})^{c_j}} \right)}{\sum_{j=1}^n \left(1 - (1 - \mu_{w_j^f})^{c_j} + \left((1 - \mu_{w_j^f})^{c_j} - (\nu_{w_j^f})^{c_j} \right) \left(\frac{1 - (1 - \mu_{w_j^f})^{c_j}}{1 - (1 - \mu_{w_j^f})^{c_j} + (\nu_{w_j^f})^{c_j}} \right) \right)} \quad \forall j \quad (14)$$

Step 4. Construct the integrated intuitionistic fuzzy decision matrix based on the preferences experts' judgments. In this case, $R^{(k)} = (r_{ij}^{(k)})_{m \times n}$ is defined as an intuitionistic fuzzy decision matrix for each expert. Then, integrated intuitionistic fuzzy decision matrix ($R = (r_{ij})_{m \times n}$) can be obtained based on the IFWA operator which is proposed by Xu [28].

$$r_{ij} = IFWA(r_{ij}^{(1)}, r_{ij}^{(2)}, \dots, r_{ij}^{(k)}) = r_{ij}^{(1)} \oplus r_{ij}^{(2)} \oplus \dots \oplus r_{ij}^{(k)} \\ = \left[1 - \prod_{k=1}^k (1 - \mu_{ij}^{(k)})^{\frac{1}{k}}, \prod_{k=1}^k (\nu_{ij}^{(k)})^{\frac{1}{k}}, \prod_{k=1}^k (1 - \mu_{ij}^{(k)})^{\frac{1}{k}} - \prod_{k=1}^k (\nu_{ij}^{(k)})^{\frac{1}{k}} \right] \quad (15)$$

Here, $r_{ij} = (\mu_{r_i}(x_j), \nu_{r_i}(x_j), \pi_{r_i}(x_j))$, $i = 1, 2, \dots, m$; $j = 1, 2, \dots, n$. The aggregated intuitionistic fuzzy decision matrix is represented as follows:

$$R = \begin{bmatrix} (\mu_{r_1}(x_1), v_{r_1}(x_1), \pi_{r_1}(x_1)) & (\mu_{r_1}(x_2), v_{r_1}(x_2), \pi_{r_1}(x_2)) & \cdots & (\mu_{r_1}(x_n), v_{r_1}(x_n), \pi_{r_1}(x_n)) \\ (\mu_{r_2}(x_1), v_{r_2}(x_1), \pi_{r_2}(x_1)) & (\mu_{r_2}(x_2), v_{r_2}(x_2), \pi_{r_2}(x_2)) & \cdots & (\mu_{r_2}(x_n), v_{r_2}(x_n), \pi_{r_2}(x_n)) \\ \vdots & \vdots & \ddots & \vdots \\ (\mu_{r_m}(x_1), v_{r_m}(x_1), \pi_{r_m}(x_1)) & (\mu_{r_m}(x_2), v_{r_m}(x_2), \pi_{r_m}(x_2)) & \cdots & (\mu_{r_m}(x_n), v_{r_m}(x_n), \pi_{r_m}(x_n)) \end{bmatrix} \quad (16)$$

Step 5. Establish the weighted intuitionistic fuzzy decision matrix by regarding step 3.6.

Step 6. Compute the intuitionistic fuzzy positive/negative ideal solution of each criterion (P_j^+ / P_j^-) as follows:

$$P_j^+ = (\mu_j^+, v_j^+, \pi_j^+) = (\max_i \{\mu_{ij}\}, \min_i \{v_{ij}\}, 1 - \mu_j^+ - v_j^+) \quad \forall j \quad (17)$$

$$P_j^- = (\mu_j^-, v_j^-, \pi_j^-) = (\min_i \{\mu_{ij}\}, \max_i \{v_{ij}\}, 1 - \mu_j^- - v_j^-) \quad \forall j \quad (18)$$

Step 7. Calculate the intuitionistic fuzzy separation measure as follows:

$$S_i^+ = \sqrt{\frac{1}{2n} \sum_{j=1}^n ((\mu_{ij} - \mu_j^+)^2 + (v_{ij} - v_j^+)^2 + (\pi_{ij} - \pi_j^+)^2)} \quad \forall i \quad (19)$$

$$S_i^- = \sqrt{\frac{1}{2n} \sum_{j=1}^n ((\mu_{ij} - \mu_j^-)^2 + (v_{ij} - v_j^-)^2 + (\pi_{ij} - \pi_j^-)^2)} \quad \forall i \quad (20)$$

Step 8. Compute the intuitionistic fuzzy relative closeness coefficient of each candidate (C_i) by utilizing the following proposed index:

$$C_i = \frac{\frac{1}{m} \left(\sum_{i=1}^m |S_i^- - \bar{S}^-| + \sum_{i=1}^m |S_i^+ - \bar{S}^+| \right)}{\frac{1}{m} \sum_{i=1}^m |S_i^- - \bar{S}^-| + \frac{1}{m} \sum_{i=1}^m |S_i^+ - \bar{S}^+|} \quad \forall i \quad (21)$$

$$\bar{S}^+ = (\bar{\mu}^+, \bar{v}^+) = \left(1 - \prod_{i=1}^m (1 - \mu_i^+)^{\frac{1}{m}}, \prod_{i=1}^m (v_i^+)^{\frac{1}{m}} \right) \quad (22)$$

$$\bar{\pi}^+ = 1 - \bar{\mu}^+ - \bar{v}^+ \quad (23)$$

$$\bar{S}^- = (\bar{\mu}^-, \bar{v}^-) = \left(\prod_{i=1}^m (1 - \mu_i^-)^{\frac{1}{m}}, \prod_{i=1}^m (v_i^-)^{\frac{1}{m}} \right) \quad (24)$$

$$\bar{\pi}^- = 1 - \bar{\mu}^- - \bar{v}^- \quad (25)$$

Finally, we have Equation (26)

$$C_i = \frac{\frac{1}{m} \left(\mu_i^{s^-} + \mu_i^{s^+} + v_i^{s^-} + v_i^{s^+} + \pi_i^{s^-} + \pi_i^{s^+} + \bar{\mu}^- + \bar{\mu}^+ + \bar{v}^- + \bar{v}^+ + \prod_{i=1}^m (1 - \mu_i^+)^{\frac{1}{m}} + \prod_{i=1}^m (1 - \mu_i^-)^{\frac{1}{m}} - \prod_{i=1}^m (v_i^+)^{\frac{1}{m}} - \prod_{i=1}^m (v_i^-)^{\frac{1}{m}} - 6 \right)}{\sqrt{\frac{1}{m} \left(\mu_i^{s^-} + \pi_i^{s^-} + v_i^{s^-} + \bar{\mu}^- + \bar{v}^- + \prod_{i=1}^m (1 - \mu_i^-)^{\frac{1}{m}} - \prod_{i=1}^m (v_i^-)^{\frac{1}{m}} - 3 \right)} + \sqrt{\frac{1}{m} \left(\mu_i^{s^+} + \bar{\mu}^+ + \bar{v}^+ + \pi_i^{s^+} + v_i^{s^+} + \prod_{i=1}^m (1 - \mu_i^+)^{\frac{1}{m}} - \prod_{i=1}^m (v_i^+)^{\frac{1}{m}} - 3 \right)}} \quad \forall i \quad (26)$$

where \bar{S}^+ is the average of $\bar{S}_1^+, \bar{S}_2^+, \dots, \bar{S}_m^+$, and also the average of $\bar{S}_1^-, \bar{S}_2^-, \dots, \bar{S}_m^-$ are represented as \bar{S}^- .

Step 9. Rank the candidates by decreasing sorting.

3. ILLUSTRATIVE EXAMPLE FOR CONSTRUCTION PROJECT SELECTION PROBLEM

In this section, an illustrative example about the selection of an appropriate construction project is adopted from study of Tan et al. [41]. In their numerical example, a local contractor defined three available projects ($A_i, i=1,2,\dots,m$) based on the available information in the market. Indeed, a group of experts by three decision makers ($DM_k, k=1,2,3$) is established to evaluate the construction project selection problem under nine criteria ($C_j, j=1,2,\dots,9$). In this respect, the considered criteria are defined as follows:

- C_1 : Profitability;
- C_2 : Difficulty;
- C_3 : Relationship with owner;
- C_4 : Need for work;
- C_5 : Resources and capabilities;
- C_6 : Keeness of competitors;
- C_7 : Competitors' competitiveness;
- C_8 : Project execution risk;
- C_9 : Financial risk.

In this respect, decision makers could assess the project selection problem and the importance of each criterion by linguistic variables, indicated in Table 1. Therefore, the relative importance of each criterion and the intuitionistic fuzzy decision matrix are defined by linguistic terms which are given in Tables 2 and 3, respectively. In addition, these tables are converted to intuitionistic fuzzy numbers which are indicated by Tables 4 and 5.

TABLE 1. Linguistic terms for the rating of weights and alternatives

Linguistic terms	Intuitionistic fuzzy numbers
Very good (VG)/ Very high (VH)	(0.90, 0.10)
Good (G)/High (H)	(0.75, 0.20)
Medium good (MG)/Medium high (MH)	(0.60, 0.30)
Fair (F)/Medium (M)	(0.50, 0.40)
Medium bad (MB)/Medium low (ML)	(0.40, 0.50)
Bad (B)/Low (L)	(0.25, 0.60)
Very bad (VB)/ Very low (VL)	(0.10, 0.90)

TABLE 2. Preferences experts’ judgments about the criteria’ weights based on linguistic terms

Attributes	Experts		
	DM ₁	DM ₂	DM ₃
C ₁	H	H	VH
C ₂	M	MH	M
C ₃	H	H	MH
C ₄	H	MH	M
C ₅	VH	H	H
C ₆	M	MH	MH
C ₇	H	H	H
C ₈	H	MH	MH
C ₉	MH	H	H

TABLE 3. Preferences experts’ judgments for rating the alternatives based on linguistic terms

Criteria	Experts								
	DM ₁			DM ₂			DM ₃		
	A ₁	A ₂	A ₃	A ₁	A ₂	A ₃	A ₁	A ₂	A ₃
C ₁	VG	F	F	VG	F	MG	G	MG	F
C ₂	MG	F	MG	F	F	F	MG	MG	F
C ₃	F	F	F	F	F	F	F	MP	MG
C ₄	F	G	MG	F	MG	MG	MG	G	MG
C ₅	G	F	MG	MG	F	MG	MG	F	MG
C ₆	G	MG	F	F	MG	F	MG	MG	F
C ₇	G	G	F	MG	MG	F	MG	F	F
C ₈	MG	F	F	MG	F	F	MG	MG	F
C ₉	MG	F	F	F	MG	F	F	MG	F

TABLE 4. Preferences experts’ judgments about the criteria weights based on IFS

Attributes	Experts		
	DM ₁	DM ₂	DM ₃
C ₁	(0.75, 0.20)	(0.75, 0.20)	(0.90, 0.10)
C ₂	(0.50, 0.40)	(0.60, 0.30)	(0.50, 0.40)
C ₃	(0.75, 0.20)	(0.75, 0.20)	(0.60, 0.30)
C ₄	(0.75, 0.20)	(0.60, 0.30)	(0.50, 0.40)
C ₅	(0.90, 0.10)	(0.75, 0.20)	(0.75, 0.20)
C ₆	(0.50, 0.40)	(0.60, 0.30)	(0.60, 0.30)
C ₇	(0.75, 0.20)	(0.75, 0.20)	(0.75, 0.20)
C ₈	(0.75, 0.20)	(0.60, 0.30)	(0.60, 0.30)
C ₉	(0.60, 0.30)	(0.75, 0.20)	(0.75, 0.20)

The relative significance of each decision maker is determined based on the new intuitionistic fuzzy index and represented in Table 6. Then, a compromise method is developed based on the concept of closer to ideal solution and farther from negative ideal solution to compute the weight of each criterion. In this respect, the IFPIS and IFNIS matrixes are established based on the Step 3.2. The results are given in Table 7. Thus, the separation measure, the intuitionistic fuzzy relative closeness of criteria and also the final weight of each criteria are determined by Steps 3.3-3.6 and are shown in Table 8.

TABLE 5. Preferences experts’ judgments for rating the alternatives based on intuitionistic fuzzy set

Attributes	Experts								
	DM ₁			DM ₂			DM ₃		
	A ₁	A ₂	A ₃	A ₁	A ₂	A ₃	A ₁	A ₂	A ₃
C ₁	(0.90, 0.10)	(0.50, 0.40)	(0.50, 0.40)	(0.90, 0.10)	(0.50, 0.40)	(0.60, 0.30)	(0.75, 0.20)	(0.60, 0.30)	(0.50, 0.40)
C ₂	(0.60, 0.30)	(0.50, 0.40)	(0.60, 0.30)	(0.50, 0.40)	(0.50, 0.40)	(0.50, 0.40)	(0.60, 0.30)	(0.60, 0.30)	(0.50, 0.40)
C ₃	(0.50, 0.40)	(0.50, 0.40)	(0.50, 0.40)	(0.50, 0.40)	(0.50, 0.40)	(0.50, 0.40)	(0.50, 0.40)	(0.40, 0.50)	(0.60, 0.30)
C ₄	(0.50, 0.40)	(0.75, 0.20)	(0.60, 0.30)	(0.50, 0.40)	(0.60, 0.30)	(0.60, 0.30)	(0.60, 0.30)	(0.75, 0.20)	(0.60, 0.30)
C ₅	(0.75, 0.20)	(0.50, 0.40)	(0.60, 0.30)	(0.60, 0.30)	(0.50, 0.40)	(0.60, 0.30)	(0.60, 0.30)	(0.50, 0.40)	(0.60, 0.30)
C ₆	(0.75, 0.20)	(0.60, 0.30)	(0.50, 0.40)	(0.50, 0.40)	(0.60, 0.30)	(0.50, 0.40)	(0.60, 0.30)	(0.60, 0.30)	(0.50, 0.40)
C ₇	(0.75, 0.20)	(0.75, 0.20)	(0.50, 0.40)	(0.60, 0.30)	(0.60, 0.30)	(0.50, 0.40)	(0.60, 0.30)	(0.50, 0.40)	(0.50, 0.40)
C ₈	(0.60, 0.30)	(0.50, 0.40)	(0.50, 0.40)	(0.60, 0.30)	(0.50, 0.40)	(0.50, 0.40)	(0.60, 0.30)	(0.60, 0.30)	(0.50, 0.40)
C ₉	(0.60, 0.30)	(0.50, 0.40)	(0.50, 0.40)	(0.50, 0.40)	(0.60, 0.30)	(0.50, 0.40)	(0.50, 0.40)	(0.60, 0.30)	(0.50, 0.40)

TABLE 7. FPIS/IFNIS matrixes

Alternatives	IFPIS ($A_{w_i}^+$)		
	DM_1	DM_2	DM_3
A_1	(0.6919, 0.2473, 0.0608)	(0.6118, 0.3115, 0.0766)	(0.6011, 0.3057, 0.0932)
A_2	(0.5819, 0.3321, 0.0860)	(0.5472, 0.3520, 0.1008)	(0.5827, 0.3236, 0.0938)
A_3	(0.5358, 0.3634, 0.1007)	(0.5358, 0.3634, 0.1007)	(0.5358, 0.3634, 0.1007)
Alternatives	IFNIS ($A_{w_i}^-$)		
	DM_1	DM_2	DM_3
A_1	(0.5, 0.4, 0.1)	(0.5, 0.4, 0.1)	(0.5, 0.4, 0.1)
A_2	(0.5, 0.4, 0.1)	(0.5, 0.4, 0.1)	(0.5, 0.4, 0.1)
A_3	(0.5, 0.4, 0.1)	(0.5, 0.4, 0.1)	(0.5, 0.4, 0.1)

TABLE 10. Intuitionistic fuzzy relative closeness coefficient of each candidate and ranking the potential candidates by comparative analysis

Alternatives	S_i^*	S_i^-	C_i	Ranked by proposed model	Ranked by Tan et al. [41] method
A_1	0.0249	0.0789	0.0948	2	2
A_2	0.0545	0.0613	0.0422	3	3
A_3	0.0810	0.0203	0.1007	1	1
\bar{S}^+	0.0535				
\bar{S}^-		0.0534			

TABLE 6. Experts' weights based on new index

DM's weight	DM_1	DM_2	DM_3
λ_k	0.331	0.335	0.334

TABLE 8. Separation measure, intuitionistic fuzzy relative closeness and the criteria' weights

Criteria	$S_{w_j}^*$	$S_{w_j}^-$	C_{w_j}	ϖ_j
C_1	0.0863	0.1419	0.6566	0.1728
C_2	0.0422	0.0624	0.5986	0.1006
C_3	0.0737	0.0236	0.7324	0.1588
C_4	0.0754	0.1080	0.5677	0.1165
C_5	0.0408	0.0791	0.0059	0.0024
C_6	0.0344	0.0825	0.1500	0.0306
C_7	0.0471	0.0898	0.6251	0.1531
C_8	0.0327	0.0624	0.4471	0.1021
C_9	0.0467	0.0577	0.7612	0.1626
$\bar{S}_{w_j}^+$	0.0534			
$\bar{S}_{w_j}^-$		0.0791		

The intuitionistic fuzzy decision matrix is aggregated and the weighted intuitionistic fuzzy decision matrix is constructed. Then, the intuitionistic fuzzy positive / negative ideal solutions of each criterion are calculated based on step 5, and the results are demonstrated in Table 9. Finally, the rank of each

potential candidate is obtained by computing the intuitionistic fuzzy separation measure and intuitionistic fuzzy relative closeness coefficient of each candidate based on steps 7 and 8. The aforementioned results are given in Table 10. In addition, the obtained ranking results are compared with Tan et al. [41]' study that have implemented the triangular fuzzy TOPSIS method in the construction project selection problem. The same results of comparing the two methods are shown that our proposed group decision model is validated. The most appropriate project for the selection is the third project, and the worst project is the second potential candidate project.

TABLE 9. Intuitionistic fuzzy positive / negative ideal solution of each criterion

Criteria	P_j^+	P_j^-
C_1	(0.2919, 0.6991, 0.0090)	(0.1242, 0.8395, 0.0363)
C_2	(0.0744, 0.9031, 0.0225)	(0.0813, 0.8944, 0.0243)
C_3	(0.1148, 0.8515, 0.0337)	(0.0956, 0.8748, 0.0296)
C_4	(0.1335, 0.8421, 0.0244)	(0.0856, 0.8887, 0.0257)
C_5	(0.0027, 0.9967, 0.0007)	(0.0017, 0.9977, 0.0006)
C_6	(0.0210, 0.9723, 0.0067)	(0.0302, 0.9626, 0.0073)
C_7	(0.1007, 0.8691, 0.0302)	(0.1515, 0.8146, 0.0339)
C_8	(0.0754, 0.9017, 0.0228)	(0.0894, 0.7903, 0.1203)
C_9	(0.1174, 0.8482, 0.0344)	(0.1385, 0.6876, 0.1739)

4. CONCLUDING REMARKS

Multi-criteria group decision-making method is one of significant technique which has helped contractors to select the most suitable project for increasing their income. For this purpose, this study proposed a new group decision-making model based on the closer to ideal solution and farther from negative ideal solution and the intuitionistic fuzzy set was considered to cope with uncertain parameters. Hence, decision makers and criteria' weights were calculated by proposed new intuitionistic fuzzy index and compromise solution, respectively. In addition, the preferences decision makers' judgments about the criteria' weights and the weight of each decision makers were considered in proposed compromise solution for determining the criteria' weights to obtain a precise solution. Then, an illustrative example was provided to show the applicability and efficiency of the proposed intuitionistic fuzzy group decision by comparing with the fuzzy TOPSIS method in the literature, in which same ranking results were obtained. For future direction, the proposed method can be developed under the interval-valued intuitionistic fuzzy and also a hierarchical structure can be developed to define the criteria and to consider all aspects of the project problem. In this respect, the proposed compromise solution method for determining the criteria' weights can be extended.

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Evaluating Construction Projects by a New Group Decision-Making Model Based on Intuitionistic Fuzzy Logic Concepts

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انتخاب پروژه‌ی مناسب، یک کلید اصلی به منظور افزایش سود برای پیمانکاران است. در عمل، عدم قطعیت پارامترهای دخیل در این حوزه بسیار بالاست. بنابراین، در نظر گرفتن نظریه‌ی مجموعه‌های فازی به منظور مقابله با عدم قطعیت، بسیار قابل توجه است. هدف از این مقاله، ارائه‌ی یک مدل تصمیم‌گیری گروهی چند معیاره تحت محیط مجموعه‌ی فازی شهودی می‌باشد. وزن هر کدام از تصمیم‌گیران و معیارها متفاوت در نظر گرفته شده‌اند. در واقع، وزن تصمیم‌گیران براساس یک شاخص فازی شهودی جدید تعیین می‌گردد و وزن معیارها نیز بوسیله‌ی یک روش پیشنهادی بر مبنای مفهوم نزدیک به راه حل ایده‌آل و دور از راه حل ضد ایده‌آل محاسبه می‌شوند. سپس، پروژه‌های بالقوه براساس ضریب نزدیکی نسبی فازی شهودی جدید رتبه‌بندی می‌شوند. از اینرو، مدل تصمیم‌گیری گروهی فازی شهودی پیشنهادی در یک مثال عددی در مورد انتخاب پروژه‌های ساخت از ادبیات اخیر انتخاب و در آن اجرا شده است. در پایان، نتایج رتبه‌بندی به منظور نشان دادن کارایی و کاربردی بودن مدل پیشنهادی با یک روش تاپسیس فازی مورد قیاس قرار گرفته است.

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