

## **DESIGN AND CONSTRUCTION OF A SENSITIVE CAPACITIVE SENSOR SYSTEM**

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**Abstract** Design and construction of a capacitor sensor with a precise readout system are described in this paper. A variable air-gap capacitive transducer was constructed and for signal measurement a successful attempt was made to exploit the capacitance changes in terms of the phase angle of the detected signal. The reported setup makes it possible to detect capacitance changes of the order of 2.5 fF in a 4.5 pF range and the readout circuit can detect a capacitance change of about 22 aF (5 in  $10^6$ ). There is a linear relation between the air-gap distance and the output of the sensor over an experimented gap range of 0.5-4.5 mm. It shows a nonlinearity deviation factor of 1% from the expected theoretical line. The dynamic range of the system is variable from 5 mm to 2.5mm and it mainly depends on the initial air-gap distance. Adding a stray capacitance of 180 pF to the system only causes a 0.1% error in the sensor output. In comparison with the other sensor systems the one reported in this paper is much more sensitive, reliable, and stray-immune to electrical interferences.

**Key Words** Design, Capacitor, Sensor, Readout Circuit

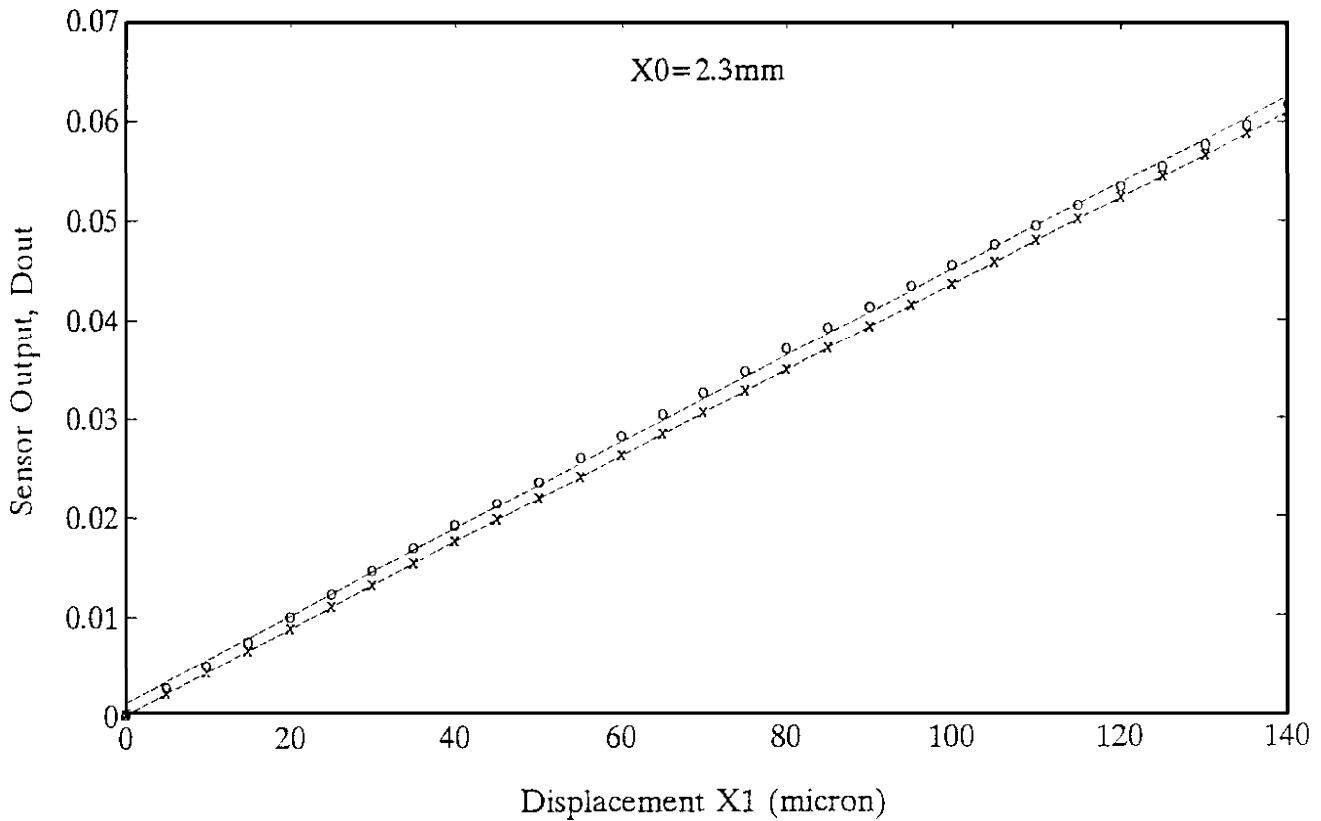
تبدیل تغییرات در ظرفیت الکتریکی یک خازن متغیر با تغییر فاصله هوا به تغییر در فاز سیگنال اندازه گیری شده. در این سیستم می توان تغییرات در ظرفیت الکتریکی در حد 2.5 فمتوفاراد در محدوده 4.5 پیکوفاراد را تشخیص داد و مدار خروجی قادر به تشخیص تغییرات در ظرفیت الکتریکی در حد 22 اتوفاراد (5 در 10<sup>6</sup>) است. رابطه خطی بین فاصله هوا و خروجی سنسور در محدوده فاصله 0.5 تا 4.5 میلی متر مشاهده شد. انحراف از خط تئوری مورد انتظار 1 درصد است. دامنه پهنای سیستم متغیر از 5 میلی متر تا 2.5 میلی متر است و عمدتاً به فاصله اولیه هوا بستگی دارد. افزودن ظرفیت پراکنده 180 پیکوفاراد به سیستم تنها باعث ایجاد 0.1 درصد خطا در خروجی سنسور می شود. در مقایسه با سایر سیستم های سنسور، سیستم گزارش داده شده در این مقاله بسیار حساس تر، قابل اعتمادتر و مقاوم تر در برابر تداخل های الکتریکی است.

### **INTRODUCTION**

Much progress has been made over the last few years in developing the capacitor transducers [1-4] and complementing measuring circuits [5,6]. However, for the precision in instrumentation and measurements, the capacitances to be measured are in the range of 0.1-10 pF with a required resolution of better than 0.1-10 fF, respectively. This requirement along with other considerations such as environmental effects and structural stability challenges the development of a much more

sensitive capacitive sensor system. To alleviate some of the problems a sensitive sensor system was developed of which the results are reported in this paper.

In order to have a reliable sensor system several parameters should be taken into account its design and its operation. Regarding the transducer part, high structural stability, sensitivity, flexibility, and dynamic range of operation are important. In fact parameters such as sensitivity, stability, and immunity to stray capacitances have encouraged the development of the new readout circuits. The



**Figure 1.** Cross-sectional view of the capacitive transducer. The main components are the upper electrode (50 mm diameter and 2 mm thickness), a lower electrode (25mm diameter and 2mm thickness) with a guard-ring (outer diameter 50mm and inner diameter 26mm), the lower and upper electrode supports (82mm diameter and 8mm thickness), three adjusting screws (M5, 30mm length), three springs, and a micrometer screw.

complexity of the readout circuit and the system cost are the other important factors which play key roles in the sensor mass production and in the real field applications.

In this paper, first, we describe the design and construction of the transducer and the readout detection circuit. The mechanical details of the designed sensor is given and its operational advantages and disadvantages are discussed. In the detection part, the electrical characteristics of the readout circuit are presented and the operation of the new setup for measuring the capacitive changes is demonstrated. Second, we present the experimental results with more emphasis on the special features of the reported system. Finally,

we conclude this paper by giving a summary of the results and making some suggestions for further improvement of the system.

### TRANSDUCER DESIGN

A schematic cross section of the designed transducer is shown in Figure 1. The basic instrumentation associated with this type of transducers is simple and requires only a variable gap capacitor, a mechanical mount, and a drive mechanism to change the air-gap distance.

The main body of the unit consists of two pieces of plexiglasses as shown in Figure 1. These two plates are machined carefully and connected together by three spring loaded

screws. By using these screws the coarse spacing between the two plexiglass plates is controllable. In practice, it is possible to change the distance between the capacitor main electrodes and also to check the parallelism of the electrodes with respect to each other.

The capacitor electrodes are machined from brass or aluminum rods. The upper electrode has a diameter of about 50mm and a thickness of about 2mm. This electrode plate is mounted on another piece of plexiglass which has a diameter of about 55mm. Actually this is the moving electrode of the capacitor and is connected to a micrometer screw.

The lower electrode of the capacitor consists of an inner electrode plate with a diameter of 25mm and a Kelvin guard-ring [7,8] with the outer diameter of 50mm. The two electrodes are carefully mounted on a plexiglass piece. The gap provided between the inner electrode and the guard-ring is about 0.5mm thick which is from the plexiglass material. Two electrodes have a thickness of about 2mm. Like the other electrode these electrodes are carefully machined from the aluminum rod and are polished for a good surface quality.

The error sources in the transducer design and operation can be the guard- electrode, gaps, sensitivity to electrode distance variation, sensitivity to lateral displacement, tilt and bending of the electrodes, electrode contamination, and the gap dielectric condition. The gap condition includes the dielectric variation due to humidity, temperature, and the absorptin effect. In our design we have considered all these parameters and care has been taken to minimize these errors during both construction and measurements.

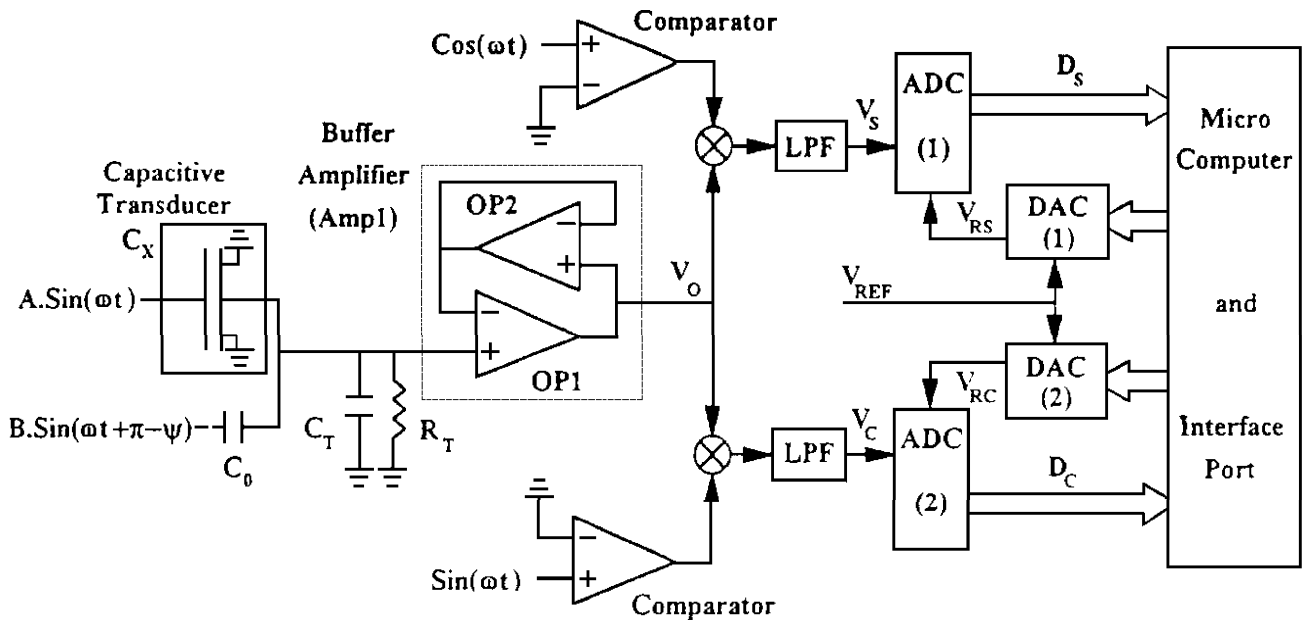
For a more precise linear positioning a stepping motor is connected to the micrometer screw by a flexible coupler. With a 500 mm/turn

screw pitch and a motor with 800 steps/turn (Step-Syn model number 103-7550-0110) it is possible to have a minimum step size of about 0.625 mm in the displacement measurements. For automating the system, an interface board is designed which controls the motor movement. A fine movement of the capacitor electrode and as a result a precise control of the capacitor gap distance are accomplished by this hardware-software combination.

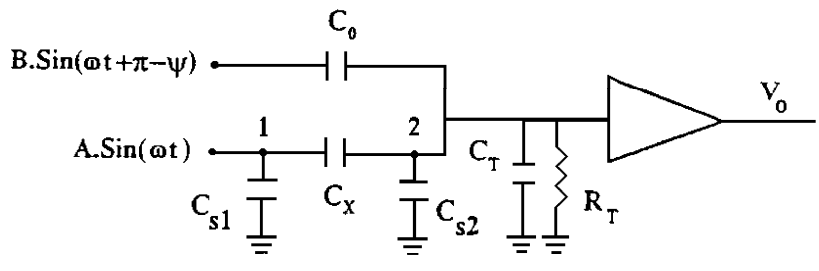
## DESCRIPTION OF THE READOUT CIRCUIT

Several techniques such as resonance, oscillation, charge/discharge and AC bridge are used in many applications. For detecting signal, we have taken the advantage of a new technique which is based on the capacitance-to-phase angle conversion [9,10]. The schematic representation of the readout circuit is shown in Figure 2a, which requires a circuit design for producing two signals with an appropriate phase difference ( $\rho - \gamma$ ). This circuit design is not shown in Figure 2a but can be found in references [9,11]. More details of producing two sinusoidal input signals can be found in Ref. [9], where the phase angle  $\gamma$  is determined from  $\tan^{-1}(R_1 C_1 \omega)$ . For the operating frequency of 10kHz,  $R_1 = 1k \Omega$  and  $C_1 = 10nF$  the phase angle  $\gamma$  is about 3.67 degrees. The amplitude of these signals A and B, Figure 2b, is about 5 V which is adjustable for one of the input signal (in this case A).

Other components are a buffer amplifier, comparators, low pass filters, analog with the digital converters, and digital to analog converters. Figure 2b shows the arrangement of the stray capacitance measurements. If  $C_x$  is an unknown capacitance then this technique can be used to measure any small changes on its capacity ( $DC_x$ ). Also by placing a well defined capacitance  $C_0$  in parallel with  $C_x$  one is able to



(a)



(b)

**Figure 2.** (a) Schematic block diagram of the readout and the monitoring circuits. The main components are a capacitive transducer,  $C_x$  (variable from 75 pF to 9 pF), a reference capacitor  $C_0$  (12 pF, 24 pF or 34 pF),  $C_T$ (12 pF) and  $R_T$ (22 M $\Omega$ ), a buffer amplifier (OP1 and OP2, LF 353), two comparators (LM319), two low pass filters ( $f_0=2$  Hz), two ADCs (ICL 7109), two DACs (DAC0800), interface board, and a PC for signal processing. (b)  $C_{s1}$  and  $C_{s2}$  are the stray capacitances (180 pF) added alternatively to the circuit at node 1 or 2.

measure the value of the  $C_x$  with a high accuracy.

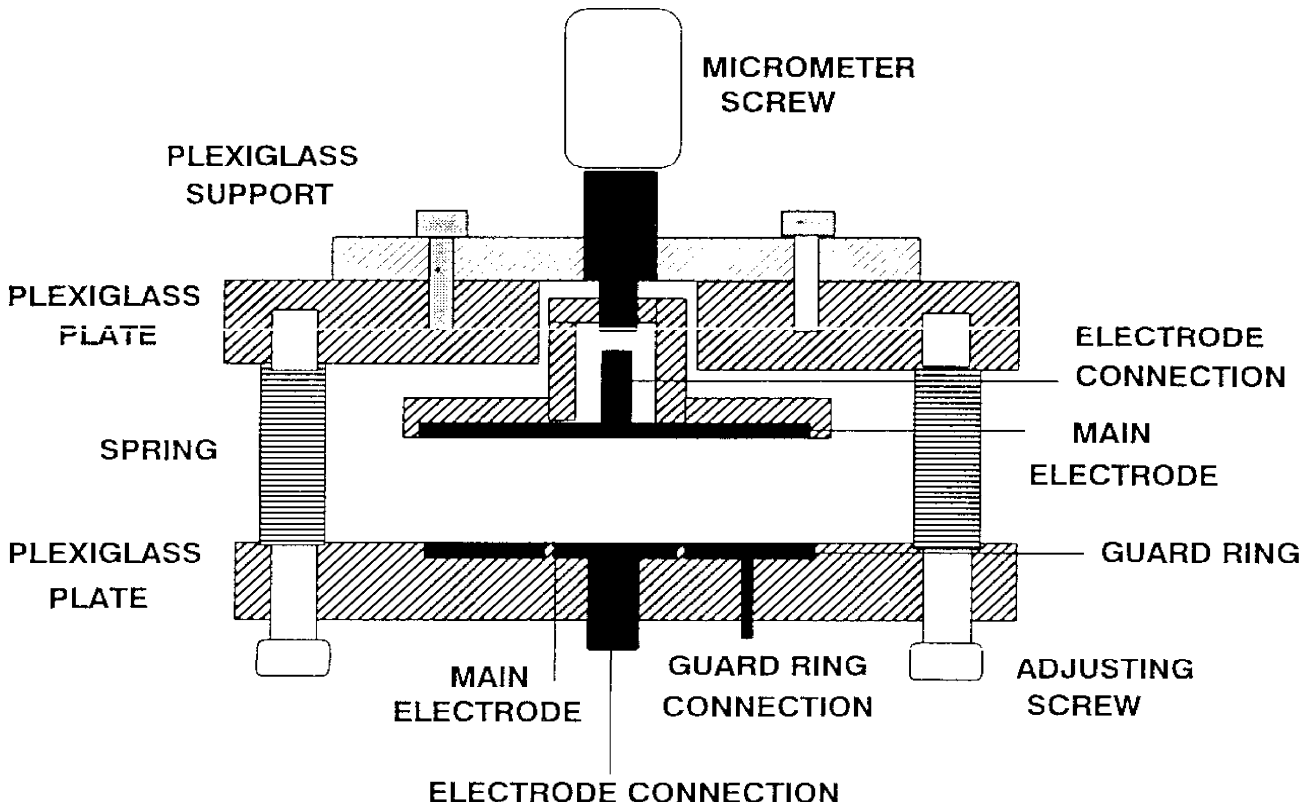
Alternatively, we can measure a normalized capacitance ratio such as  $C_x/C_{x0}$ , where  $C_{x0}$  is a reference value for  $C_x$  and we define  $C_x=C_{x0}+C_{x1}$ . Here  $C_{x1}$  is the capacitance change of the transducer due to a displacement of  $X1$  from its initial position,  $X_0$ . The block diagram of the detection and monitoring system is also shown

in Figure 2a. As can be seen, the final signal is processed digitally by a PC, while the output is recorded as a dimensionless number.

Following the theoretical analysis given in Reference [9], the normalized digitized output,  $D_{out}$ , can be written as

$$D_{out} = \frac{C_{x1}}{C_{x0}} = \frac{\tan(\gamma)}{n} \frac{D_c}{D_s} \quad (1)$$

where,  $\gamma$  is the phase difference,  $D_c$  and  $D_s$  are



**Figure 3.** Variation of the sensor output with respect to the displacement for  $X_0=2.3\text{mm}$ . The line denoted by, o, is for the experimental results and by, x, is for the theoretical calculations.

digitized output of two ADCs as shown in the block diagram of Figure 2a, and  $n$  is the parameter that depends on the voltage ratio of the two multipliers ( $V_{RS}/V_{RC}$ ).

Now any change in the value of  $C_{x1}$  such as  $DC_{x1}$  can produce variation in the output such as (for constant values of  $n$  and  $\gamma$ ):

$$DD_{out} = \frac{DC_{x1}}{C_{x0}} = \frac{\tan(\gamma)}{n * 2^{m-2}} \quad (2)$$

where,  $m$  is the number of bits of the ADC and other parameters are defined previously. The parameter  $DC_{x1}$  can be considered as the minimum resolvable capacitance change (MRCC) of the reported readout scheme.

By substituting the capacitances in terms of the gap distances in Equation(1) and exchanging the positions of  $C_{x0}$  and  $C_0$  in the circuit (see Figure 2a) the final equation for

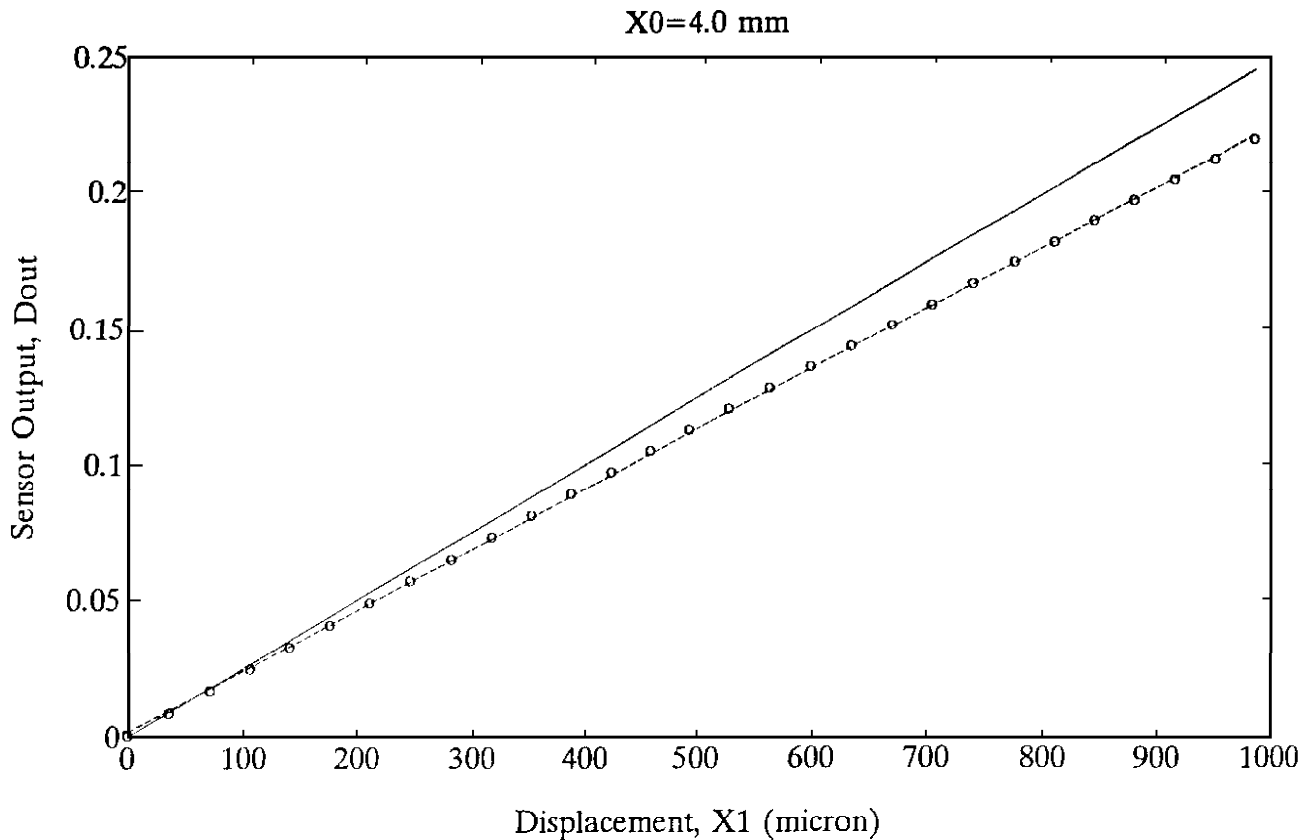
data analysis becomes.

$$D_{out} = X_l/X_0 \quad (3)$$

where  $X_0$  is the distance at which the zero adjustment is made and  $X_l$  is the displacement from  $X_0$ . In fact Equation(3) shows the calibration line for the sensor system. The importance of this scheme is the linear relationship between the output signal and the parameters to be controlled (the gap distance in this case). Another advantage of this method is that output readout signal corresponding to the capacitance change is independent of the  $C_0$  value. However,  $C_{x0}$  and as a result  $X_0$  value control the slope of the calibration line in sensor operation.

### EXPERIMENTAL RESULTS

Our experimental system consists of a



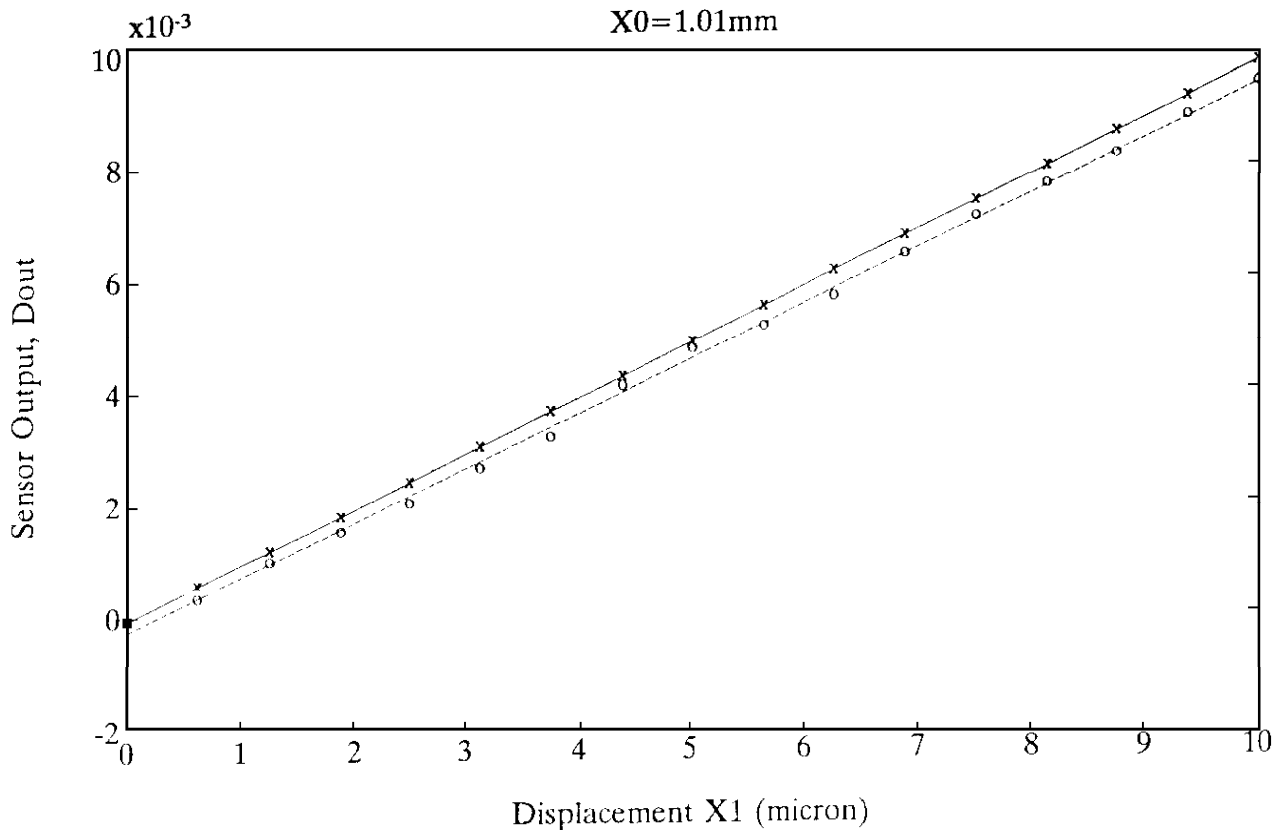
**Figure 4.** Sensor output as a function of displacement for  $X_0=4\text{mm}$ . The line denoted by, o, is the experimental results and the solid line shows the theoretical results.

transducer, a detection circuit, and finally a digital signal processing unit. By using the constructed transducer and readout circuit, data collection was accomplished by a PC via a written program to control both the stepper motor and the signal processing. In the first experiment the variation of the output,  $D_{out}$  with respect to the gap distance,  $X_0$ , was studied. The digitally averaged output values at different  $X_0$  values were recorded and the result of this study for  $X_0=2.3\text{ mm}$  is shown in Figure 3. To compare these results with the theoretical calculations, the experimental slope  $\Delta D_{out}/\Delta X_0$  was computed through a least line fit method. The experimental slope is  $4.38 \times 10^{-4}$  which is in clear agreement with the theoretical slope of  $4.35 \times 10^{-4}$ .

In order to determine the deviation of the

experimental values from the expected theoretical values and as a result the linearity of the system we calculated the deviations at several  $X_0$  values. In general this deviation or nonlinearity factor is of the order of 1%.

To check the linearity of the sensor at higher gap distances the output variation for  $X_0=4\text{mm}$  is displayed in Figure 4. As can be seen in Figure 4 this sensor system shows a linear behavior at this value of  $X_0$ . The results of this study indicate that for this range of operation ( $X_0=0.5\text{-}4.5\text{mm}$ ) the linearity of the system is quite acceptable. However, by increasing  $X_0$  one expects that the deviations of the output signals from the expected theoretical values increase. This nonlinearity could be due to two factors, one is the nonlinearity of the mechanical drive system and the other is the transducer



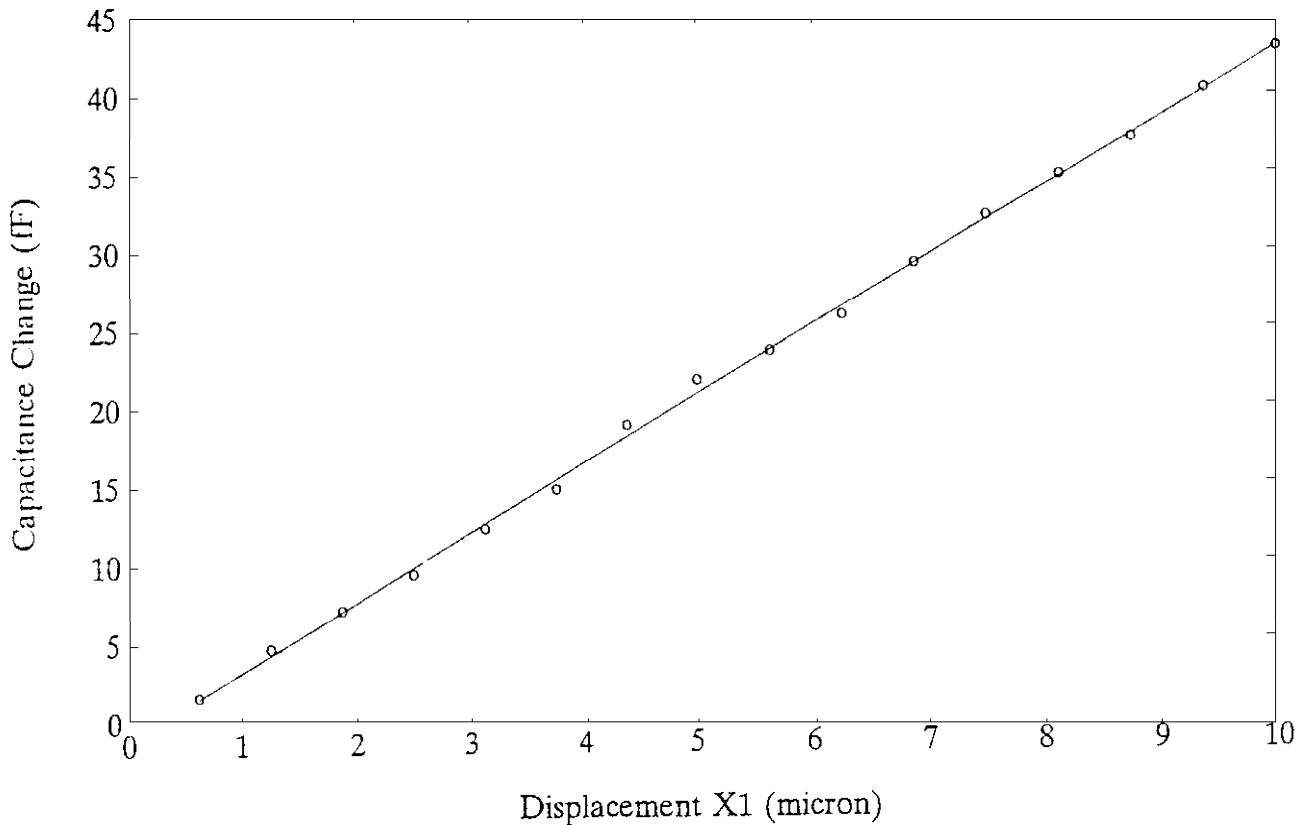
**Figure 5.** Sensor output variation as a function of displacement for  $X_0=1.01$  mm to show the sensor resolution. The line denoted by, o, is the experimental results and the one denoted by, x, is the theoretical calculations.

(depends on the difference between the radius of the guard-ring and the inner electrode with respect to the gap distance). At higher  $X_0$  values the edge effects become more pronounced, thus the small nonlinearity can be explained by considering these factors.

To check the resolution of the system, in another study we have used the smallest single step scan (0.625mm) in the range of  $X_0=1.01$  mm ( $C_{x0}=4.5$  pF). The result of this study, shown in Figure 5, indicates that the theoretical slope of this line is  $9.9 \times 10^{-4}$  corresponding to a resolution of about  $5 \times 10^{-6}$ . Comparing this resolution with  $44 \times 10^{-6}$  for  $X_0=2.3$ mm and  $127 \times 10^{-6}$  for  $X_0=4$ mm, one can observe that the resolution of the system is decreased by increasing the  $X_0$  value. Theoretically this can be noticed from Equation (3) in which  $DD_{out}$  is

inversely proportional to  $X_0$  and directly proportional to the  $DX_1$ . However, it would be noticed that although decreasing  $X_0$  will considerably increase the sensitivity of the device, the dynamic range of its operation decreases. So depending on the application conditions, one can optimize the system for an appropriate operation range and resolution.

The variation of the capacitance change for  $X_0=1$  mm is presented in Figure 6. The minimum resolvable capacitance change (MRCC) of the readout circuit for  $C_{x0}$  value of about 4.5 pF is 22 aF. Theoretically MRCC can be obtained from Equation (2). Three parameters  $Y$ ,  $n$ , and  $m$  influence the resolution of the readout circuit. To increase the resolution, one can increase  $n$  and  $m$  or change the phase angle  $Y$ . The overall resolution of the



**Figure 6.** Capacitance changes as a function of displacement for  $C_{x0}$  value of about 4.5pF.

device is controlled in part by the mechanical drive system and the readout circuit. The minimum resolvable displacement for the mechanical drive unit is limited by the pitch of the micrometer screw and the number of motor steps per turn. Because of the low resolution of the mechanical drive system the overall resolution of the present system is limited to a capacitance change of about 2.5 fF in 4.5 pF range ( $5.5 \times 10^{-4}$ ). With the present combination a minimum displacement change of about 0.625 mm is possible. This value is much less than that of the readout system which is around 25 nm. However, the mechanical resolution can be reduced to the half of this value by driving the motor at half step mode of operation.

Although increasing  $n$  increases the resolution, it decreases the dynamic range of

the measurements. This is illustrated in Figure 7 for different  $n$  values which clearly shows the variation. As can be observed from Figure 7 the dynamic range is about 952.5 mm for  $n=0.4$  while it decreases to 7.5 mm for  $n=7$  (for  $X_0=2.3\text{mm}$  and  $Y=3.67$  degree).

One of the most important parameters in the sensor performance is the reproducibility of the system. In order to test this parameter we plotted the results of the two different runs at the same value of  $X_0=4.28$  mm. To see the data points better in Figure 8 intentionally we picked up the two runs with different scanning increments (one has an increment of 1.25mm and the other 1.875mm). As can be seen in Figure 8 there is a good agreement between the result of the two trials, which confirms the reproducibility of the system.



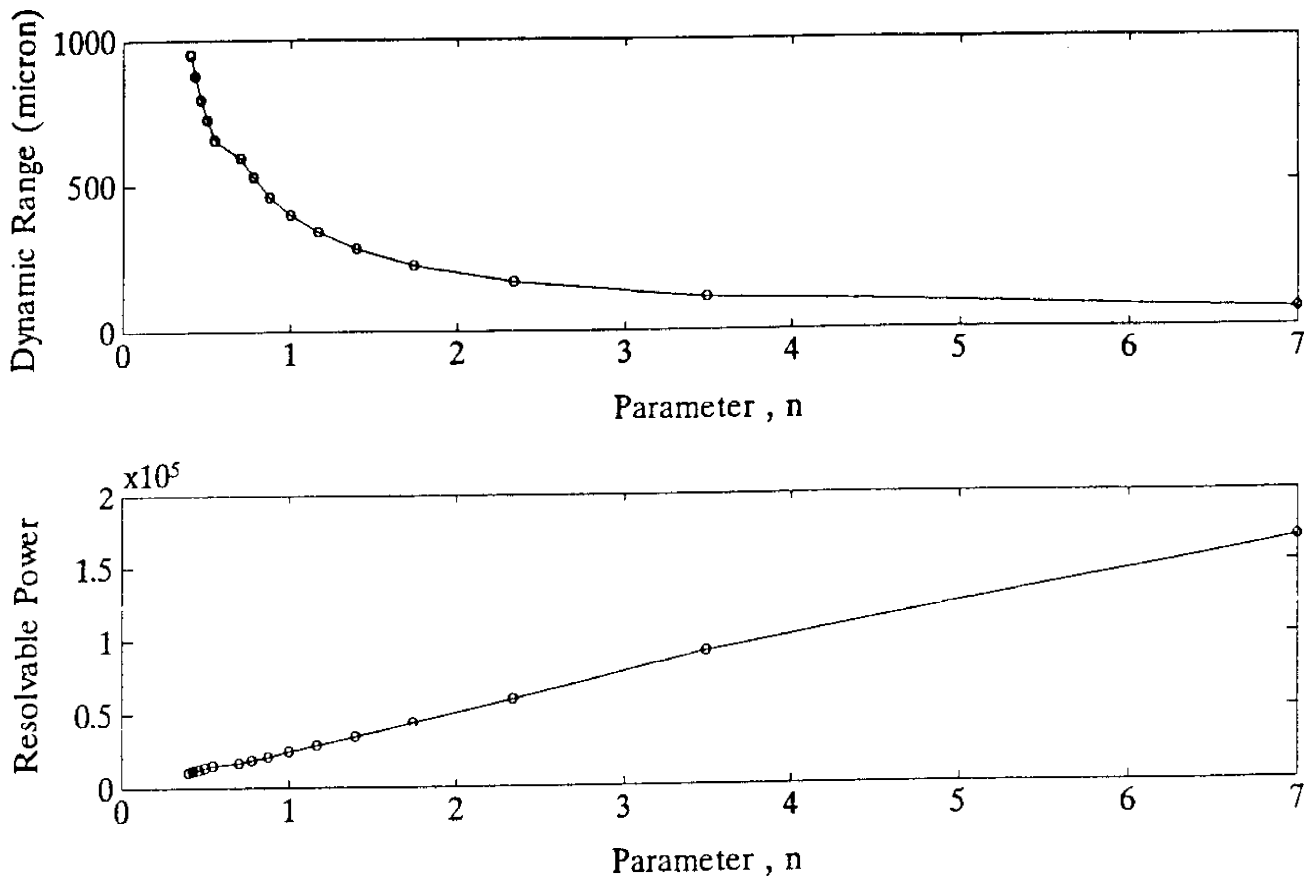


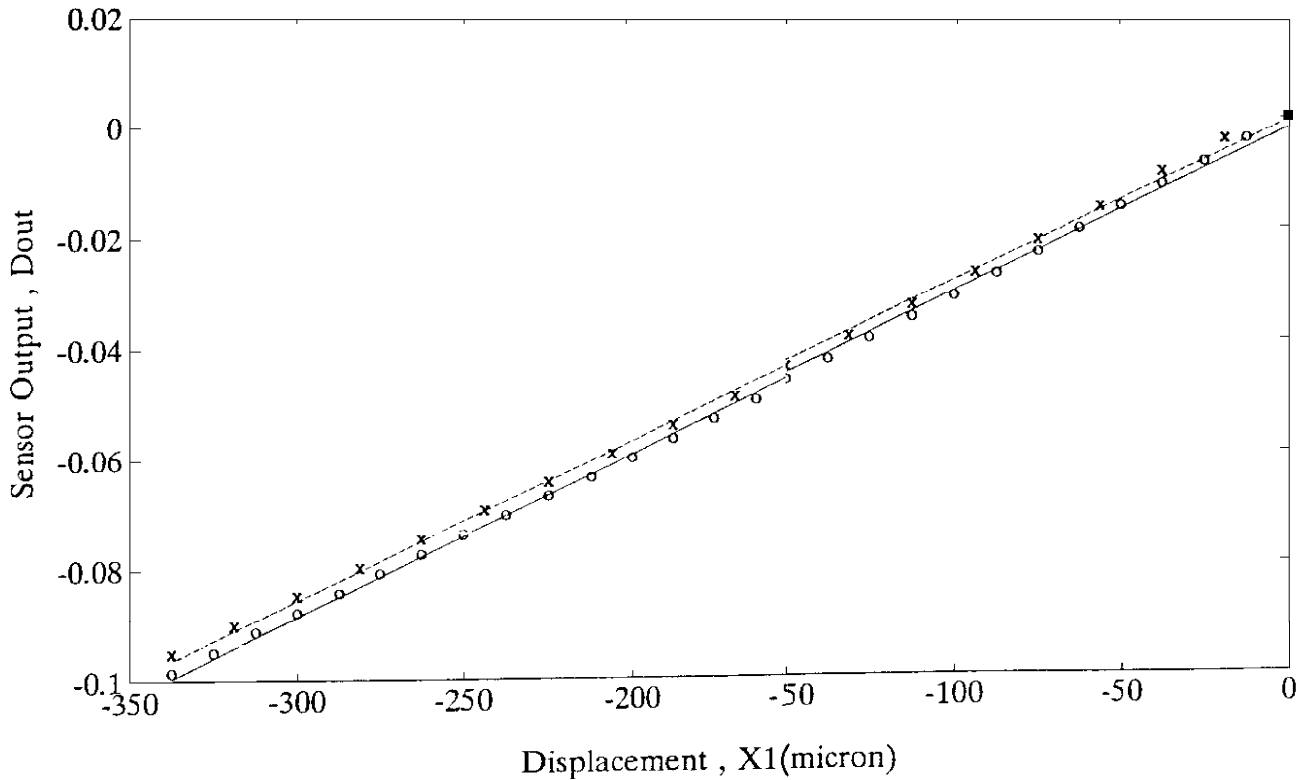
Figure 7. Sensor dynamic range as a function of parameter  $n$  at a fixed value of  $X_0=2.3\text{mm}$ , top. The bottom part shows the corresponding readout resolving power.

It should be mentioned that the experimental slope of the line denoted by symbol,  $\circ$ , is  $2.9 \times 10^{-4}$  while the slope of the other line is  $2.84 \times 10^{-4}$ . As can be seen the difference in the slopes is only  $0.06 \times 10^{-4}$  which is negligible. However, the remaining difference is due to the zero adjustment (difference in the line intercepts) which could be corrected by the zero adjustment option of the readout system. This difference, however, does not have any effect on the slope of the calibration line, which is the more important parameter of the sensor system.

The effect of changing the value of the reference capacitance,  $C_0$ , (see Figure 2a) in the sensor output was studied for different capacities. The result of this study for  $C_0=12$

pF, 24 pF, and 34 pF are presented in Figure 9. Two important points can be concluded from the results of this study. First, the slopes of the calibration lines are  $1.3 \times 10^{-4}$ ,  $9.9 \times 10^{-4}$ , and  $9.6 \times 10^{-4}$  for the case of  $C_0=12\text{pF}$ , and 24pF, and 34 pF, respectively. The slopes within the experimental error of the system ( $0.4 \times 10^{-4}$  at this range) are the same which means that the slope of the calibration line is independent of the  $C_0$  value. This fact is in agreement with the outcome of Equation (3) which clearly shows that the final formula does not depend on the  $C_0$  quantity. Second, as can be seen in Figure 9, by increasing  $C_0$  value the dynamic range of the operation also increases accordingly. The dynamic range for  $C_0=12\text{pF}$ , 24pF, and 34pF are 170mm, 220mm, and 270 mm, respectively

$X_0=4.28\text{mm}$



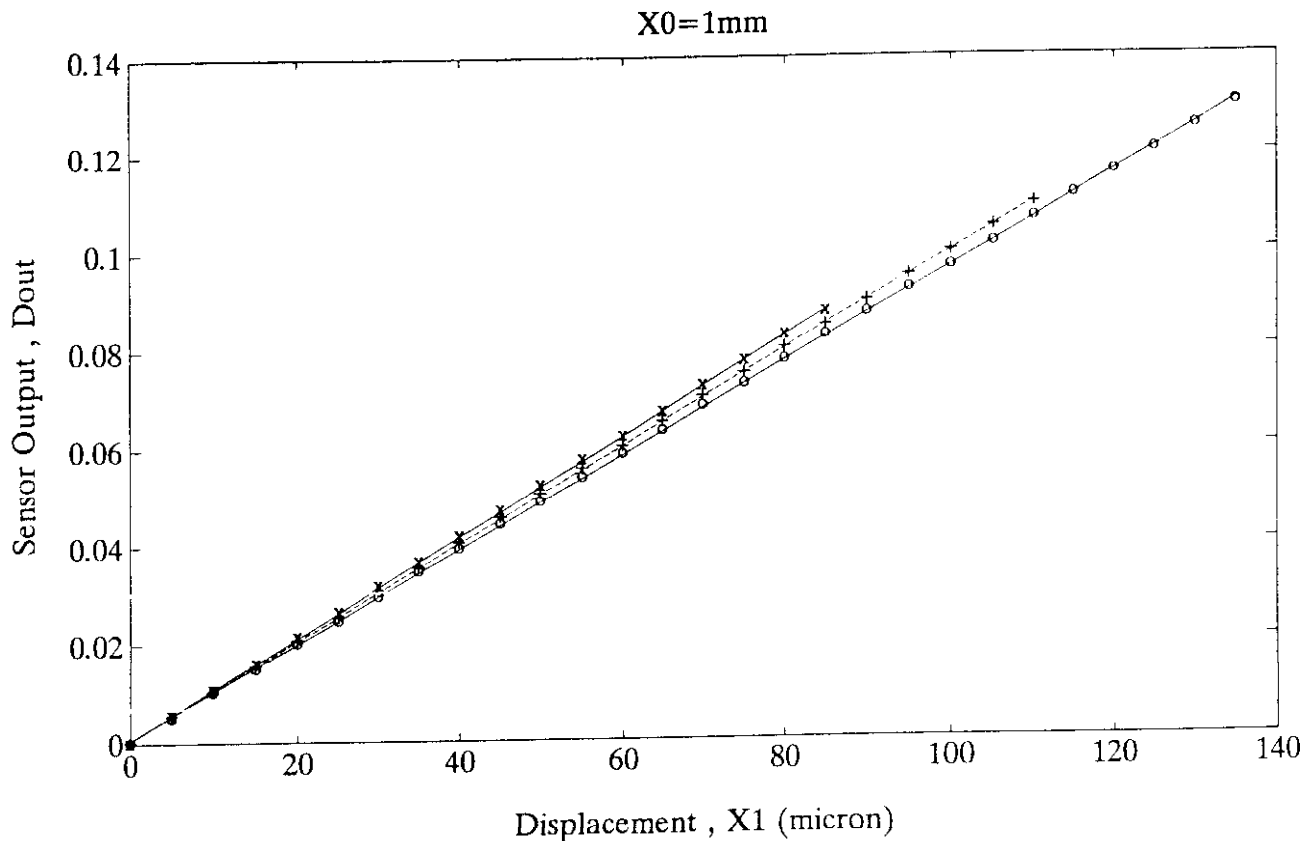
**Figure 8.** Sensor output readouts at the two different trials denoted by, x, and, o, to show the reproducibility of the system for a fixed value of  $X_0=4.28\text{mm}$ .

( $X_0=1\text{mm}$ ). However, it should be mentioned that increasing the  $C_0$  value will decrease the sensitivity of the detection system to some extent. So there is as usual a trade off between the system dynamic range and its sensitivity.

A comparison of the results of this study with those of others reported in the literature will reveal some of the features of the new system. A digital readout technique for capacitor sensor application has been reported[5] in which a capacitor difference with a resolution of 0.05 fF on capacitors in the 20-100 fF range has been obtained. Later some attempts have been made in order to cancel the noise effect for the readout system. This readout circuit has been used for a pressure sensor chips containing 100 pF air - gap capacitors and a resolution in the 30 aF range has been reported[6].

In another study [12] the use of a long range capacitive displacement sensor is explained which has a resolution of 1mm over a wide range of about 150 nm. In comparison with this report our readout system has a resolution of about 25 nm and the transducer with 1 mm air-gap distance shows a resolution of about 5 ppm. The result of our prototype system reveals a high sensitivity and linearity at a reasonable mid dynamic range.

However, increasing the number of averaging points in data recording increases the resolution, but with the available ADCs it increases the measurement time. The resolution of the readout system is however much more than the resolution of the drive unit for the transducer. It must be pointed out that the design of capacitors with very small capacity is



**Figure 9.** Shows the effect of varying  $C_0$  in the sensor operation. The solid line denoted by the symbol, x, is for the case of  $C_0=12\text{pF}$ , the dashed-line denoted by, +, is for  $C_0=24\text{ pF}$ , and the one denoted by, o, corresponds to  $C_0=34\text{ pF}$ .

only possible in the integrated circuits and would be hard to build in a discrete fashion. The readout system reported here with a high sensitivity is very suitable for measuring such small capacitance changes in integrated circuits.

To check the stray immunity of the system, we have measured the output changes due to adding the stray capacitances  $C_{s1}$  (node 1) or  $C_{s2}$  (node 2) as shown in Figure 2b. For adding  $C_{s1}=180\text{ pF}$  the output change was about  $1.88 \times 10^{-3}$  which corresponds to a capacitance change of  $8.46 \times 10^{-3}\text{ pF}$  for the  $C_{x0}$  value of  $4.5\text{pF}$ . Placing  $C_{s2}=180\text{ pF}$  at node 2 the output variation is even less in the order of  $10^{-3}$  ( $4.5 \times 10^{-3}\text{pF}$ ) for the same  $C_{x0}$  value which indicates that the system is more immune to the stray capacitances from this side of the system.

If we define the stray immunity factor as  $DC_x/C_s$ , then we can compare our results with those of the others[13]. In that report a stray immunity factor of  $10^{-4}$  has been obtained (for  $C_s=100\text{pF}$ ) while our system shows a factor of  $4.7 \times 10^{-5}$  at node 1. The stray immunity factor as  $DC_x/C_s$  of  $4.7 \times 10^{-5}$  at node 1. The stray immunity factor at node 2 for our system is  $2.5 \times 10^{-5}$  in comparison to  $5 \times 10^{-5}$  for that report which is better by a factor of 2.

## CONCLUSIONS

In summary, there is a good agreement between the experimental results of this work and the calculated values for the system calibration line, resolution, and the operation range. Other advantages of this system are the reliability,

stability, and the stray-immunity which allows its operation in open environment without any shielding requirement. Although the results are satisfactory, the mechanical drive system can be further improved to increase the mechanical resolution and also to increase the dynamic range of the operation. The resolution of the readout circuit can also be improved by using high speed ADCs with higher bit numbers. Even though the capacitance changes were measured in this study, it is also possible to implement the reported system for sensing other parameters that somehow have small influence on the transducer capacity [14,15].

Error analysis of the reported transducer and the readout circuit requires a detailed discussion which is out of the scope of this paper and is planned for the future report. However, in such analysis one must consider the nonlinearity, stray-immunity, offset errors and the noise problem causing an overall error in the measurements. In our design care was taken to minimize the stray capacitances, gap effects, and the environmental effects on the transducer and error sources for the circuit. Although we have tested the readout circuit at the frequency of 10 kHz, the design is capable of operating at frequencies up to 50 kHz. The environmental conditions such as air temperature and humidity effects can influence the capacitance variation, but these minor changes can be compensated for by the zero adjustments at the start of a measurement and are negligible for the short period of the measurement. Finally, we admit that there are some other methods for the construction of the more accurate micro sensors, but such method of fabrication requires micro machining and micro technology that are

not available at the present time.

## ACKNOWLEDGMENTS

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