A Computational Study about the Effect of Turbines Pitched Blade Attack Angle on the Power Consumption of a Stirred Tank

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A B S T R A C T

In this study, the stirring mechanism of shear-thinning fluids benefiting from four blades in turbulent flow is considered. The fluid is studied inside a stirred cylindrical tank with a flat bottom. The height of fluid is equal to the cylinder’s diameter and the impeller is positioned centrally. A CFD simulation has been carried out and three-dimensional turbulent flow is numerically analyzed using the Shear Stress Transport k-ω (k-ω SST) model. The parameters related to power consumption including attack angle and flow index were studied. The power consumed during the mixing of the shear thinning liquids under a specific Reynolds number and attack angle is less than that consumed when the fluid used is water, which is a Newtonian fluid. As the power law index decreases, the corresponding power consumption also declines. At a certain attack angle and power law index, an increase in the Reynolds number first significantly decreases power consumption; beyond a given range, the consumption plateaus. To validate the numerical simulation results, the findings derived on the basis of the power number used in this work were compared with the test results of other studies, and good agreement was observed.


1. INTRODUCTION

The stirring mechanism of fluids in one or multiple phases has been an interesting field for many researchers working in different industries including nuclear, food, petrochemical, dyeing, etc. Many of these processes benefit from mechanical stirrers which usually consist of a number of flat impellers in a cylindrical vessel for the purpose of stirring Newtonian and non-Newtonian fluids which usually have shear thinning behavior. For shear thinning fluids, the viscosity decreases when the shear rate increases. Therefore, in higher rotational speeds the flow is usually turbulent [1-3].

One of the first researches that can be noted in the field of stirring fluids in stirred vessels is that of Hiraoka et al. [1]. They performed a 2D numerical study on Newtonian and non-Newtonian fluids generated by two-blade impellers and paddle agitators in low impeller speed that shows flow is essentially tangential for a low impeller speed. Abid et al. [3] simulated the 3D flow fields inside a tank filled with a Newtonian fluid and two-blade impellers in low Reynolds numbers. Suzukawa et al. [4] investigated the effect of the attack angle with four-bladed paddle impellers in a stirred vessel via laser-Doppler velocimetry (LDV). Schäfer et al. [5] examined the turbulent flow structures generated by a four bladed 45° pitched bladed impeller. The main aims of Aubin et al. [6] are to characterize the single phase turbulent flow in a tank stirred by a 45° pitched blade impeller using CFD. Beshay et al. [7] presented the results of an experimental investigation concerning the power input of pitched blade impellers and standard Rushton turbine impellers in a cylindrical vessel under a turbulent regime of flow of agitated water. Roy and Acharya [8] investigated the scalar mixing in a turbulent stirred tank with pitched blade turbine. In the present study on turbulent pitched blade turbine impeller, the impeller speed is perturbed at the macroinstability frequency and changes in mixing pattern and mixing
measures are quantified. Venneker et al. [9] examined the impact of Reynolds number and flow index for the turbulent flow of non-Newtonian fluid, experimentally and using LDV. Hamed Bashiri et al. [10] investigated the turbulent fluid flows in stirred tanks using a non-intrusive particle tracking technique. In this research, CFD simulation is conducted using RANS-based turbulence models for a 6-flat blade Rushton turbine and 45° four-pitched blade turbine.

The literature review shows that no concrete studies have been directed toward four-blade impeller agitators. We therefore investigated the flow characteristics of shear thinning fluids in a stirrer with a four-blade impeller under turbulent flow. Specifically, the effects of changes in blade attack angle, rotational speed, and fluid rheological behavior on power consumption were examined. CFX 16.2 (ANSYS, Inc.) was used to numerically simulate the turbulent flow of the fluids. The Metzner–Otto concept was adopted to model the properties of the non-Newtonian fluids, and the k-ω SST model was used to model the turbulent flow regime.

2. NUMERICAL ISSUES

The stirring system considered for this study is depicted in Figure 1. As can be seen, the stirring tank is a cylindrical vessel of flat-bottomed type and most of its dimensions are considered as a constant function of tank diameter, D = 450 mm. A four-blade turbine with a diameter of d = D/2 and clearance of C = d are taken as impellers and the height of the fluid is exactly the same as tank height (H=D). The thickness of each blade is 2 mm and its height w = D/10. The shaft, having a diameter of d₁ = D/30, is coaxial with the centerline of the cylinder. The attack angle of blades (θ) is considered equal to 45°, 60°, 75° and 90°. Moreover, the results of simulation are presented in nondimensionalized form, so that they could be extended to any arbitrary diameter of the tank.

In this study, the computer program CFX 16.2 (ANSYS-Inc) was used to simulate the 3D flow fields in stirred vessel equipped with a four bladed impeller. The Navier-Stokes equations were written in a rotating reference frame. Therefore, the centrifugal and the Coriolis acceleration terms are added. In this numerical study, the pressure at the center of each cell, and the velocity components at the center of the six faces of the cell (one component on the two corresponding orthogonal faces) were calculated. The pressure-velocity coupling is handled by the semi-implicit algorithm SIMPLE which is described by Patankar [11].

The geometry was created using ANSYS Design Modeler. The volume of the vessel was divided into two parts: stationary (e.g., vessel) and rotating (e.g., impeller). There are three different approaches for solving such a problem, namely, the sliding mesh (SM) method, the mixing plane method and the multiple reference frame (MRF) method. Reviews on the matter can be studied in (Zadghaffari et al. [12]; Ameur [13]; Bashiri et al. [10]). The MRF method is the simplest of the three. This approach is appropriate when flows at the boundary between inner and outer zones are nearly uniform. Since there are no baffles, in stirred tanks, large-scale transient effects are absent and MRF method can be used. The boundary conditions consist of setting each velocity component equal to zero on the blades and the axial shaft, because the rotating frame, and setting the angular velocity component equal to the rotation speed at the vertical walls. On the bottom, the angular velocity is chosen equal to 2πN [17].

The MRF method can be used in our study since there are no baffles in stirred tanks and large-scale transient effects are not present. In this method, the boundary conditions consist of setting each velocity component equal to zero on the blades and the axial shaft, because of the rotating frame, and setting the angular velocity component equal to the rotation speed at the vertical walls and on the bottom surface the angular velocity is chosen equal to 2πN.

![Figure 1. Numerical mesh and Geometry of mixing system](image-url)
Figure 1 shows the mesh created by the ANSYS Meshing program. The mesh size is decreased near the walls and blades. To examine the independency of the mesh, several mesh configurations were analyzed and finally a mesh with 1530000 elements for which the velocity changes of its blade tip were less than 2% with respect to the previous model with 1250000 elements was selected.

3. RHEOLOGICAL MODEL

In the present work, simulations were conducted on non-Newtonian shear thinning fluids. According to the reports in this field, the shear-thinning behavior was controlled by means of the weight percentage of polymer added in water. The polymer Xanthan gum, with the commercial name Keltrol RD is employed in this study. Rheological properties of the fluids used are based on measurement performed by Venneker et al. [9] as given in Table 1.

The method of Metzner and Otto [14] was used to obtain the average shear rate and the apparent viscosity was then calculated from the power law equation:

$$\dot{\gamma} = k_s N$$  \hspace{1cm} (1)

where $k_s$ is a weak function of the stirrer type and for Rushton turbine is equal to 11.5. For a Newtonian fluid, the Reynolds number is given by:

$$Re = \rho N d^2 / \eta$$  \hspace{1cm} (2)

And for a shear thinning fluid with the average shear rate Equation (1):

$$Re = \rho N^2 a d^2 / m k_s^{n-1}$$  \hspace{1cm} (3)

The power consumption, $P$, in a stirred tank can be calculated from the torque acting on the impeller [15]:

$$P = 2\pi N \tau$$  \hspace{1cm} (4)

where $N$ is the rotational speed in rev/s and $\tau$ is the torque applied on the impeller. The power number is then computed as:

$$Np = P / \rho N^2 d^5$$  \hspace{1cm} (5)

The radial coordinate is defined in dimensionless form as:

$$R' = \frac{2r}{D} , Z' = \frac{Z}{D}$$  \hspace{1cm} (6)

4. RESULT AND DISCUSSIONS

In order to validate the CFD model, the results were compared to that of K. Suzukawa et al. [4] tests with the same geometrical configuration. The fluid under study was water and blades attack angle was set to 90°, 75°, 60° and 45°. Figure 2, visualizes the Power number ($Np$) for a tank with a diameter of 450 mm and velocity of 2.37 rev/s, i.e. $Re = 1.2 \times 10^5$. As is obvious, a good agreement exists between numerical and experimental results.

5. EFFECT OF BLADE ATTACK ANGLE

To evaluate the attack angle effect ($\beta$) on the shear thinning fluid stirring mechanism, velocity field contour for Keltrol solution with a power law index of $n = 0.8$ and $Re = 50000$ is studied in Fig 3. Velocity field contour is drawn for two planes of coordinate system, namely, XY and YZ plane and for four attack angles: 45°, 60°, 75° and 90°. It can be seen that the more the attack angle is reduced from 90° and approaches 45°, the more fluid is pumped toward the bottom of the tank and higher mixing efficiency is achieved. As a consequence, according to the results, for tanks having blades not close to the bottom of the cylinder and for better mixing of fluids possessing higher viscosities, taking advantage of pitched blade impeller is more effective.

Among the important parameters studied in stirring systems is the power number $Np$, calculated according to Equation (5). The impact of attack angle on the parameter $Np$ for the above-mentioned fluid is depicted in Figure 4.

<table>
<thead>
<tr>
<th>TABLE 1. Rheological properties</th>
</tr>
</thead>
<tbody>
<tr>
<td>Concentration (%)</td>
</tr>
<tr>
<td>-------------------</td>
</tr>
<tr>
<td>0.045</td>
</tr>
<tr>
<td>0.05</td>
</tr>
<tr>
<td>0.08</td>
</tr>
<tr>
<td>0.1</td>
</tr>
</tbody>
</table>

Figure 2. Power number Vs. Blade attack angle for $Re = 1.2 \times 10^5$
It can be observed from this figure that for a specific Reynolds number, the value of $N_p$ grows with an increase in the attack angle, in a way that when using a flat blade, this value rises to more than four times the value of the case whose blades attack angle is 45°. In other words, according to Equation (5), the consumed power for stirring the fluid reduces by decreasing the angle of attack from 90° to 45°.

Figure 5 shows the ratio of radial, tangential and axial velocities to blade tip speed ($V/V_{tip}$) based on the dimensionless radial coordinate ($R^*$) for solution with $n = 0.71$ and $Re = 100000$. As can be seen, values of all three velocity parameters become smaller as the angle decreases. It can be inferred from Figure 5 that by distancing from the impellers and getting closer to the vessel walls, all three velocity components lessen, although their reduction patterns are not similar. Furthermore, in an approximate distance of $R^* = 0.8$ to 1, the value of velocity components become almost the same for various attack angles. Furthermore, within this level of study ($Z^* = 0$), radial and tangential velocities approach zero as they get closer to the vessel wall. This is in contrast to the fact that axial velocity has negative values in this region. In other words, the axial velocity which has a lower value compared to the other two velocity components, approaches zero when distancing from the impeller tip in the region $R^* = 0.6$ to 0.7 and then finds a negative value. It is obvious from the figure that the smaller the attack angle, the faster the axial velocity approaches zero and becomes negative.
6. EFFECT OF RHEOLOGICAL PARAMETER

In this section, the effect of fluid rheology is investigated on the stirring process. To achieve this goal, the variations of power number ($N_p$) for different solutions of Table 1 in the Reynolds number $= 20000$ and different attack angles are presented in Figure 6. It can be understood that as the power law index (n) increases, the power number at a specific angle and Reynolds number increases. It should be mentioned that rotational velocities for achieving a certain Reynolds number is not identical for different fluids. For instance, rotational velocities for reaching a Reynolds number of 20000 for a tank with the diameter of 450 mm and different solutions are shown in Table 2.

![Figure 6. Power number in Re=20000](image)

### TABLE 2. Rotational speed for Re= 20000.

<table>
<thead>
<tr>
<th>Solution</th>
<th>Wt%</th>
<th>$m \times 10^{-3}$ [Pa.S]</th>
<th>n[-]</th>
<th>N[rev/s]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water</td>
<td>-</td>
<td>1.0</td>
<td>1.00</td>
<td>0.4</td>
</tr>
<tr>
<td></td>
<td>0.045</td>
<td>9.5</td>
<td>0.8</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>0.05</td>
<td>16.5</td>
<td>0.71</td>
<td>2.5</td>
</tr>
<tr>
<td></td>
<td>0.08</td>
<td>34.0</td>
<td>0.64</td>
<td>3.6</td>
</tr>
<tr>
<td></td>
<td>0.1</td>
<td>74.8</td>
<td>0.56</td>
<td>5</td>
</tr>
<tr>
<td>Keltrol</td>
<td>0.045</td>
<td>9.5</td>
<td>0.8</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>0.05</td>
<td>16.5</td>
<td>0.71</td>
<td>2.5</td>
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<tr>
<td></td>
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<td></td>
<td>0.1</td>
<td>74.8</td>
<td>0.56</td>
<td>5</td>
</tr>
</tbody>
</table>

5. CONCLUSION

The purpose of the present study was to investigate the effects of changing the blades attack angle and fluid shear thinning rheology in turbulent flow on power consumption in a four-blade impeller. The result of computational fluid dynamics simulation shows that by decreasing the attack angle, more fluid will be pumped into the bottom of the vessel, resulting in a better mixture. Also, power consumption for stirring of the fluid is reduced by decreasing the blade attack angles.

Additionally, the results indicate that the flow index (n) is proportional to the power number.

6. REFERENCES


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چکیده
در این مطالعه، سازوکار اختلاط سیال shear-thinning توسط یک پروانه چهار پره در رزم جریان معکوس، بررسی شده است. سیستم اختلاط مشکل از یک مخزن استوانه‌ای با کف تخت است. با توجه به این افتراق معدال با قطر مخزن از سیال پروانه در وسط معکوس قرار دارد. شبیه‌سازی جریان معکوس با استفاده از مدل k-ω SST در تحلیل سه بعدی (CFD) انجام شده است. پارامترهای مورد بر توان مصرفی مخلوط کن نظیر زاویه حمله و شاخص جریان (flow index) تحت تاثیر پارامترات کاری شده است. مورد مطالعه قرار گرفت. توان مصرفی در اختلاص سیال shear-thinning کمتر از سیال نیوتنی آب می‌باشد و هر چه شاخص عدد توان کاهش یابد، این توان مصرفی نیز کاهش می‌یابد. همچنین، در یک زاویه حمله و شاخص عدد توان کاهش نشان داده شده است که تغییرات عدد رینولدز ابتدا سبب کاهش قابل ملاحظه توان مصرفی شده و از یک محدوده به بعد کاهش تدریجی در کاهش آن تدریجی و به مظور صحت سنجی نتایج شبیه‌سازی، عدد توان به دست آمده از این بررسی با نتایج مقایسه‌ای دیگر مقایسه شد و اطمینان حاصل‌ی شد.