Fault Detection of Bearings Using a Rule-based Classifier Ensemble and Genetic Algorithm

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Abstract

This paper proposes a reduct construction method based on discernibility matrix simplification. The method works with genetic algorithm. To identify potential problems and prevent complete failure of bearings, a new method based on rule-based classifier ensemble is presented. Genetic algorithm is used for feature reduction. The generated rules of the reducts are used to build the candidate base classifiers. Then, several base classifiers are selected according to their diversity and the scale of them. Weights of the selected base classifiers are calculated based on a measure of support rate. The classifier ensemble is constructed by the base classifiers. The accuracy reached 98.44% which is 4.5% higher than that of the three base classifiers.


1. Introduction

Data analysis, dependency analysis, and learning are some of the most important applications of rough set theory. In those applications, it is typically assumed that we have a finite set of objects described by a finite set of attributes. The values of objects on attributes can be conveniently represented by an information table, with rows representing objects and columns representing attributes. Failures of rotary machineries is a vital problem in plants which are expected for a long running of machines. There is an increasing demand for techniques able to utilize the sensor data to diagnose faults of rotary machineries. The faults arising in rotating machines are usually caused by damages and failures in bearings, gears and shafts. There are some variations in vibration signals of bearings when faults happen. Several advantages for machine condition monitoring and fault diagnosis, as reducing maintenance costs, improving productivity and increasing machine availability, were formerly reported. Bearing is one of the most vital components in the industries. The importance and need to the bearing is clear; therefore, fault diagnosis of bearings is a core research area in the condition monitoring field [1]. Variations of the vibration signal are either small or buried in strong noises, and cannot be detected easily from vibration signals. To solve these problems, the signal processing and feature extraction are performed first. The wavelet transform, empirical mode decomposition (EMD), local mean decomposition (LMD) and their improved method have been widely used to get the components with high signal-noise ratio, based on which features are extracted to describe the symptoms of bearings. Heidari et al. [2] used wavelet transform for fault diagnosis of bearing and gears of a gearbox. Six dimensionless time-domain features and five dimensionless frequency-domain features were extracted based on the EMD for fault diagnosis of rolling bearings [3]. The feature vectors for bearings under variable conditions were acquired by applying the singular value decomposition (SVD) to the product functions decomposed by the LMD [4]. In order to lessen human intervention, increasing the accuracy and shortening the time of fault diagnosis, plenty of works have been reported on the fault classification methods. The KNN algorithm, probabilistic NN, PSO optimized SVM and a rule-based method were compared in terms of accuracy, time consumption, intelligibility, and

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maintainability for fault diagnosis of two different types of bearings [5]. The fuzzy lattice classifier (FLC) and fuzzy lattice reasoning (FLR) were applied for faults diagnosis of bearing [6]. The rule-based method gave classification results based on the rules in the form of "if condition type". The advantage of this method was that they were much more transparent in decision making process. In this paper, rule-based fault diagnosis by semantic attributes is carried out using an ensemble of classifiers. The motivation behind the use of a classifier ensemble was that ensembles were proved to provide accuracies higher than any of the single base classifiers that constituted them [7]. Furthermore, reliance on different classifiers rendered the reasoning more robust. Yu [8] proposed a new manifold learning algorithm, joint global and local/nonlocal discriminant analysis, which aimed to extract effective intrinsic geometrical information from the given vibration data. Comparisons with other regular methods, principal component analysis, local preserving projection, linear discriminant analysis and local LDA, illustrate the superiority of GLNDA in machinery fault diagnosis. Yiqing et al. [9] proposed an adaptive multiple classifier system named AMCS to cope with multi-class imbalanced learning, which makes a distinction among different kinds of imbalanced data. The AMCS included three components, which were, feature selection, resampling and ensemble learning. Each component of AMCS was selected discriminatively for different types of imbalanced data. Rathore and kumar [10] presented ensemble methods for the prediction of number of faults in the given software modules. The experimental study was designed and conducted for five open-source software projects with their fifteen releases, collected from the PROMISE data repository. The results were evaluated under two different scenarios, intra-release prediction and inter-releases prediction. The prediction accuracy of ensemble methods was evaluated using absolute error, relative error and measure of completeness performance measures. In addition, a new classifier combination rule based on the consensus approach of different classification algorithms during the ensemble modelling phase has been proposed [11]. The remainder of the paper has been arranged as follows:

Section 2 describes the construction of base classifiers. Overview of classifier ensemble is presented in Section 3. More details of modeling with proposed method and the simulation results are given in Section 4; the paper is concluded with Section 5.

2. CONSTRUCTION of BASE CLASSIFIERS

Feature reduction is used with a method based on the rough set (RS) [12] and genetic algorithm (GA). Rough set theory is one of the mathematical tools that deals with feature reduction to find a minimal subset. The basic concept is by making an upper and a lower approximation of the data set. The feature reduction is achieved by comparing equivalence relations generated by feature sets considering the dependency degree as an important measure; features are removed and the reduced feature set provides the same dependency degree as the original. The base classifiers utilized the rules generated on the basis of the reducts of features to identify fault of the bearings.

2. 1. Discernibility Matrices

Two objects are discernible if their values are different in at least one attribute. Skowron and Rauszer [13] suggested a matrix representation for storing the sets of attributes that discern pairs of objects, called a discernibility matrix. An information table (IT) can be defined as follow:

\[
IT = (U, A, V)
\]

\[
A = C \cup D
\]

\[
U = \{x_1, x_2, \ldots, x_m\}
\]

\[
C = \{a_1, a_2, \ldots, a_n\}
\]

\[
D = \{d\}
\]

where \(U\) is a non-empty finite set of objects, \(A\) is a non-empty finite set of attributes and \(V\) is a value set of \(A\).

An information table represents all available information and knowledge. That is, objects are only perceived, observed, or measured using a finite number of attributes. In Equation (3), \(x_i (i=1, 2, \ldots, m)\) indicates the \(i\)th object. In Equation (4), \(a_j (j=1, 2, \ldots, n)\) indicates the \(j\)th condition attribute. Also parameter \(d\) shows the decision attribute. The discernibility matrices of \(IT\) is a \(m \times m\) matrices. Each entry \(e_{i,j}\) consists of the set of attributes that can be used to discern between objects \(x_i\) and \(x_j (j=1, 2, \ldots, m)\) [14],

\[
e_{i,j} = \begin{cases} \{a_k \in C | a_k(x_i) \neq a_k(x_j), d(x_i) \neq d(x_j)\} & \text{if } e_{i,j} \neq \emptyset \\ \emptyset, d(x_i) = d(x_j) & \text{if } e_{i,j} = \emptyset \end{cases}
\]

\[
E = \{e_{i,j} | e_{i,j} \neq \emptyset\}
\]

2. 2. Feature Reduction by GA

The GA is a heuristic for function optimization, where the minima or maxima of the function cannot be built analytically. A population of potential solutions is refined iteratively by employing a strategy inspired by Darwin instinctive evolution or natural selection. The GA promotes “survival of the fit test” [15]. It has been used successfully in many fields for optimization problems [16, 17]. In this paper, feature reduction is a process to compute minimal hitting sets [9] of the discernibility matrices. The GA is employed to solve the problem. The fitness function \(f_i\) of GA is defined as bellow:
\[ f_i(B) = (1 - \alpha) \left( \frac{|C \setminus |B|}{|C|} + \alpha \cdot \min \left\{ \frac{|x \in E | (x \notin B \cup \emptyset)}{|E|} \right\} \right) \]  
Equation (8)

In Equation (8), symbol |\|, \alpha and \varepsilon are the length of a set, a weighting between subset lengths and hitting fraction and a minimal value for the hitting fraction, respectively. The subsets \( B \) of \( C \) are found through the evolutionary search driven by the fitness function and are “good enough” hitting sets, i.e., have a hitting fraction of at least \( \varepsilon \), and are collected as reducts in a candidate collection.

3. CONSTRUCTION of CLASSIFIER ENSEMBLE

Each reduct in the above candidate set can be used as an independent classifier with its rules generated. Several of them can also be combined together to construct a classifier ensemble. Figure 1 shows the diagram of a classifier ensemble. A set of different base classifiers \( \{C_1, C_2, \ldots, C_p\} \) are constructed from a labelled data set \( X \).

A popular pair wise diversity measure according to the correlation between the performances of the two classifiers (the numbers of patterns correctly/wrongly classified) is adopted. Let \( i \) and \( j \) be a pair of base classifiers. The correlation between the outputs of \( i \) and \( j \) can be measured as:

\[ \text{corr}_{i,j} = \frac{\sum_{k=1}^{n} (c_{ij} - \bar{c})(c_{ij} - \bar{c})}{\sqrt{\sum_{k=1}^{n} (c_{ij} - \bar{c})^2 \cdot \sum_{k=1}^{n} (c_{ij} - \bar{c})^2}} \]  
Equation (9)

where \( N^{ab} \) is the number of test patterns classified correctly (\( a = I \)) or incorrectly (\( a = 0 \)) by the classifier \( i \) and correctly (\( b = I \)) or incorrectly (\( b = 0 \)) by the classifier \( j \). Classifiers that tend to recognize the same patterns correctly will have positive values of \( \text{corr}_{i,j} \), whereas those which commit errors on different patterns will render \( \text{corr}_{i,j} \) negative. A correlation-based diversity index between classifiers \( i \) and \( j \) can then be defined based on the correlation coefficient of Equation (9) as:

\[ \text{div}_{i,j} = \frac{1 - \text{corr}_{i,j}}{2} \]  
Equation (10)

For a classifier ensemble \( G \) consists of more than two classifiers, its diversity index is calculated based on the average of diversity indexes of every pair of classifiers in \( G \) as:

\[ \text{div}(G) = \frac{2}{|\{i,j\}|} \sum_{i,j=1,i\neq j} |\{i,j\}| \text{div}_{i,j} \]  
Equation (11)

The GA is adopted to select the optimal combination of base classifiers considering the diversity and scale of the ensemble. The fitness function \( f_2 \) is defined below:

\[ f_2(G) = (1 - \beta) \left( \frac{|\{i,j\}|}{|H|} \right) + \beta \cdot \text{div}(G) \]  
Equation (12)

In Equation (12), \( H \) and \( \beta \) are the collection of all base classifiers and a weighting between the diversity and scale of the ensemble, respectively. An improved approach based on the static weighted voting (SWV) [18] is developed to integrate the predictions of the base classifiers in this paper. The SWV method involves in assigning a unitary vote to each base classifier \( C_k, k = 1, 2, \ldots, p \), and in multiplying that vote by a weight \( \omega_k \) proportional to the accuracy of the classifier measured in terms of the mean recognition rate (MRR), i.e. the fraction of patterns it correctly classifies. In this respect, a third set is required to compute the weights of the base classifiers. However, the \( \omega_k \) used in the SWV is a measure of accuracy on the whole despite of a specific class \( l \). Since the classification is implemented with rules, a measure called support rate (SR) is used to replace the MRR. It is defined as:

\[ SR_{k,l} = \frac{N_{c_{k,l}}}{N_{a_{k,l}}} \]  
Equation (13)

In Equation (13), \( N_{c_{k,l}} \) and \( N_{a_{k,l}} \) are the number of objects which are correctly assigned to class \( l \) by \( k \)th base classifier and the number of objects which are assigned to class \( l \) by \( k \)th base classifier, respectively. Each class \( l \) of the \( q \)th test object receives an ensemble vote given by the sum of all weights assigned to that class:

\[ v^q_l = \sum_{k=1}^{p} SR_{k,l} \delta_{l,k} \]  
Equation (14)

Finally, the \( q \)th object is assigned to the class \( l_q \) with the highest ensemble vote:

\[ l_q = \arg\left( \max_{1 \leq q \leq r} (v^q_l) \right) \]  
Equation (15)

where, \( r \) is the total number of classes.

4. MODELLING in FAULT DIAGNOSIS with VIBRATION SIGNAL

Vibration signals were obtained from the bearing data center [19]. Bearing of the motor shaft was SKF6203.

Electro-discharge machining has been used to introduce defects to the bearings. The fault diameters were 0.1778 mm. Four cases such as outer race fault, inner race fault, ball fault, and the normal bearing were
is discretized and partitioned into $X_{\text{TRN}}$, $X_{\text{IND}}$ and $X_{\text{TST}}$ at a ratio of 3:3:2.

Afterward, base classifiers are obtained by performing the GA with its fitness function defined in Equation (8) on the $X_{\text{TRN}}$. Then, base classifiers is selected to construct a classifier ensemble by GA on the $X_{\text{IND}}$. Next, the $X_{\text{IND}}$ is used to determine the weights of each base classifier. Finally, the performance of the classifier ensemble is evaluated by the $X_{\text{TST}}$.

4.2. Results Firstly, discretization was done. The mean of each feature was calculated, and the values in the vector which were less than the mean were designated to zero, otherwise were assigned to one. Zero and one indicated the low level and high level of the index, respectively. Perform the GA with its fitness function defined in Equation (8) on the $X_{\text{TRN}}$, where $\alpha=0.33$, $\varepsilon=0.85$. The initial population of GA was 70, probability of one-point crossover was 0.3 and probability of mutation was 0.05. 13 reducts were output. Their accuracy of fault classification on $X_{\text{TRN}}$ ranged from 78 to 100%. Scale of them ranged from 4 to 10. The large-scale reducts had higher accuracy on the training set, their generalization ability was usually not very good. At this point of view, reducts containing 5 features were put into the candidate collection. They are listed in Table 2.

Each reduct had a corresponding rule set. For example, 18 rules were generated based on the first reduct in Table 2. They were given in Table 3.

Classify objects in $X_{\text{IND}}$ using the reduct in the candidate collection and its generated rule set. Perform the GA with its fitness function defined in Equation (12) with $\beta=0.65$. The searching result showed that \{\{CF,FT,FC,FI,FB\},\{SK,FT,FC,FI,FB\},\{CF,SK,FT,FC,FI\}\} was a good enough choice balancing the diversity against the scale. The weights of $SR_{R,I}$ calculated on the $X_{\text{IND}}$ are listed in Table 4.

The classifier ensemble was constructed. The final step was to evaluate its performance on the $X_{\text{TST}}$. Comparison of the accuracy among the base classifiers and the classifier ensemble is given in Table 5.

### Table 1. Decision table [15]

<table>
<thead>
<tr>
<th>SI</th>
<th>IF</th>
<th>CF</th>
<th>CI</th>
<th>SK</th>
<th>KI</th>
<th>FT</th>
<th>FC</th>
<th>FI</th>
<th>FO</th>
<th>FB</th>
<th>Dec</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.308</td>
<td>5.269</td>
<td>4.033</td>
<td>6.282</td>
<td>0.063</td>
<td>4.189</td>
<td>7.711</td>
<td>13.858</td>
<td>38.618</td>
<td>4.549</td>
<td>2.559</td>
<td>IRF</td>
</tr>
<tr>
<td>1.399</td>
<td>6.332</td>
<td>4.535</td>
<td>7.757</td>
<td>0.065</td>
<td>5.998</td>
<td>13.882</td>
<td>25.542</td>
<td>39.17</td>
<td>17.302</td>
<td>5.039</td>
<td>IRF</td>
</tr>
<tr>
<td>1.559</td>
<td>10.371</td>
<td>6.669</td>
<td>13.201</td>
<td>0.005</td>
<td>12.479</td>
<td>32.058</td>
<td>22.125</td>
<td>7.018</td>
<td>22.252</td>
<td>9.812</td>
<td>ORF</td>
</tr>
</tbody>
</table>
The MLEM2-based method [3] was also utilized for fault diagnosis under the same condition. The accuracy was 98.44% with a common rule matching mechanism which was better than that of the three base classifiers. The reason was that discretizing the continuous values of features into semantic ones introduced errors to the fault decision table. However, using high level (1) or low level (0) describing the features and rules was much easier to understand than the ones using comparison operators such as “<”, “>”, “≤” and “≥” because it was not an easy work for site operators to understand or remember the meanings of figures and their corresponding levels in the variation range. For example, rule “CF=0 & FT=0 & FC=0 & FI=0 & FB=0 => Dec=01” was able to be interpreted as if the index FI was at a high level and others were normal, then a decision that inner race defect happened was made. Fortunately, combination of selective base classifiers as a classifier ensemble provided a higher performance like several people sat together and voted for a cleverer and more reliable decision.

5. CONCLUSION

This paper combined selective base classifiers together to give a better prediction of fault type of bearings. The base classifiers used rules described with semantic variables to identify faults. The former made the result more trustable which increased the accuracy by 7.5%, 7.5% and 5% compared with the three base classifiers, respectively. The latter made the diagnostic procedure easier for comprehension as it simulated how the field workers dealt with such problems. It provided a new way for failure analysis of rotating machinery based on semantic diagnostic rules. The drawbacks of the method lay in that arbitrary discretization introduced misinformation to the information table or fault decision table here in the other words, which resulted in a decrease in accuracy. Self-adaptive discretization methods may be a key to overcome the shortcoming in the future work.
6. REFERENCES


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PAPER INFO

Paper history:
Received 30 October 2016
Received in revised form 04 February 2017
Accepted 26 February 2017

Keywords
Fault Detection
Bearing
Classifier Ensemble
Genetic Algorithm