Vibration Characteristics of Heavy Load Rack with Split-hom together Structure

B. Li*, L. Hou, R.Q. Mou, Y.Q. Wei

School of Manufacturing Science and Engineering, Sichuan University, Chengdu, China

1. INTRODUCTION

Nowadays, heavy load rack is widely used in forging hydraulic presses, free forging hydraulic presses, pipe extrusion machines, sheet metal forming presses, rolling mills and other heavy equipment. As a carrier to accumulate, heavy load racks play an important role in transferring and releasing huge energy. With the development of modern heavy industry, higher requirements have emerged for heavy machinery which is moving to the direction of large-scale, high reliability and manufacturability, simultaneously the prestress technology and split-hom together technology are gradually formed. With development of technology, the structure of heavy load rack has changed from the overall structure to prestressed bolt split-composite structure, at last, to the wire winded prestress split-hom together structure [1, 2].

Literature [3] studied the principal of carrying and influencing factors of integrity of bumpy-ridge beam in pre-stress wire winded framework. Literature [4] studied the stress of Bumpy-ridge structure. Literature [5] studied the parameters optimization of Bumpy-ridge structure. Literature [6] analyzed the reliability of the dissected frame of heavy equipment from the aspects of stress field, integrality and fatigue. Literature [7] analyzed the deformation characteristics and carrying capacities of the frame under the action of center loading and eccentric loading. Literature [8] discussed the influence of the prestress coefficient by the modal analysis. Literature [9] proposed the way to test prestress in finite element analysis. Although literature [3-9] did a lot of work about heavy load rack with split-hom together structure, eccentric load have important influence on the reliability of the rack when it is in the working state. Literature [10-14] established vibration model on wind blade, reducer casing and rotor system etc., and obtained the frequency capture characteristics of the system by numerical analysis, but has not been applied to the heavy load rack. So, this paper establishes a three-dimensional (3D) and mathematical model of the rack, through modal analysis and numerical analysis obtains the vibration characteristics of the rack, and the results of the analysis verify the reliability and rationality of the rack model.


*Corresponding Author’s Email: 433721805@qq.com (B. Li)
2. RACK PRESTRESSED HOM-CONNECTION PRINCIPLE

2.1. Prestressed Hom-connection

The Hom-connection with prestress makes multi-peak structures embed each other to resist lateral displacement and achieve fusion between the mechanical structures. The ability of resisting lateral displacement is determined by the embedded depth of multi-peak structure, and the deeper they embed each other, the stronger the ability to resist lateral displacement is, but the greater the likelihood of stress concentration as well. Therefore, this paper studies an embedded structure, whose depth is between 0.5 and 3mm. The structure has a high capacity of resistance to lateral displacement, which can effectively reduce stress concentration and improve the fatigue resistance.

2.2. Bionics Multi-peak Structure

In nature, there are many multimodal embedded structures for improving adhesion. For example, Boston-ivy grow towards the surface depression and the surface contour can be accurately replicated by Boston-ivy, then the Boston-ivy’s surface will harden, which can make the plant surface and the other surface interlock, thereby firmly adhere together. Gecko can make natural flexible micro setae under the feet and the contact surfaces interlock, then use the adhesion force to walk on walls or glasses. Such adhesion structure between animal and plant surfaces, in essence, is a combined multi-peak ridge structure that is the basis for generating mechanical resistance. Multi-peak structure may be hook shape, rivet-like shape or other shapes producing mechanical obstruction (Figure 1), which is very similar to mechanical connections.

In the biological multimodal interlocking structures, the multi-peaks not only can be generated before, but also after contact. Multi-peak structure has the following characteristics: small-scale, strong adaptability and contact surface with a hom together in the vertical and parallel direction [15].

2.3. Hom Combined Multimodal Contact Mechanics Principle

Elastic deformation and plastic deformation coexist in the multimodal contact zone of the hom combined structures. Therefore, this article uses a cylindrical peak to build mathematics, mechanics model of contact problems. In Figure 2, the cylinder under the load $P$ is pressed into an infinite flat plate, then the contact surface produce local elastic deformation and form a rectangular area of $2bL$ contact area. The contact width $b$ can be calculated by Hertz theory.

$$b = \frac{4PR}{\pi L \left( \frac{1 - \mu_1^2}{E_1} + \frac{1 - \mu_2^2}{E_2} \right)}$$

(1)

where $E_1 =$ cylinder elastic modulus, $E_2 =$ flat elastic modulus, $\mu_1 =$ cylinder Poisson's ratio and $\mu_2 =$ plate Poisson's ratio. In Figure 2, pressure on the contact area presents oval distribution and the maximum contact pressure in the midline of contact surface is $4/\pi$ times as big as the average compressive stress, namely [16]:

$$\sigma_{\text{max}} = \frac{4P}{\pi 2bL} = \frac{P}{\pi L R \left( \frac{1 - \mu_1^2}{E_1} + 1 - \mu_2^2 \right)}$$

(2)

From Figure 2, it is known that as the load $P$ increase, its plastic deformation will continue to increase. When the average pressure increases to $2.8\sigma_s$ ($\sigma_s =$ material yield strength), average pressure gets flat, which shows that most of the contact zone is elastic deformation [17].

2.4. Prestressed Hom-Connection Method

Based on hom-connection principle, three kinds of hom-connection methods are put forward [18]. Figure 3a is a direct multimodal hom structure connected together, whose two contact surfaces are made of multi-peak structure, and then embed in each other. Figure 3b is embossed multi-peak combined structure with better adaptive capacity and less demand on the machining accuracy and positioning, but the multiple peaks and flat produce large plastic deformation, which have an effect on multimodal hom structure. Figure 3c is embossed multi-peak structure with a transition plate; the materials of transition plate and multi-peak structure are different, so it can ensure a reasonable embedded depth and achieve a good hom-connection. The transition plate imprint type is chosen in the paper.

---

Figure 1. Biosphere multi-peak structure [15]

Figure 2. Cylinder and flat contact force planar graph [15]
Figure 3. Schematic diagram of different multimodal hom structure [18]

3. WIRE WOUND SPLIT-HOM TOGETHER RACK 
FINITE ELEMENT ANALYSIS

3.1. Hom Combined Finite Element Model of the Rack

Hom together rack has: total height=20m, horizontal span=8.64m, frame thickness=3m, made of top and bottom arch whose big radius and small radius are: 4.2 and 2m, respectively; left and right column 2.2m wide and 2.3m high, transition plate with 0.03m thickness, and bearing components. The sub-block structures such as top and bottom arches and left and right columns are surrounded by wire, which can produce prestress.

The 3D model is established in the Unigraphics NX 8.0 based on the relevant parameters; then import the model in the finite element analysis software (ANSYS Workbench 13.0). During the modal analysis, the ‘Automatic Mesh Generation’ to mesh and set the mesh size to 100mm are used. Then, 43342 elements and 160394 nodes are obtained. Figures 4a, 4b are the rack arch beam rack column finite element models, and Figures 5 and 6 show the split-hom together rack finite element model and hom combined mesh rack, respectively.

3.2. Prestressed Hom Together Rack Modal Analysis

3.2.1. Finite Element Model and Boundary Conditions

When the press is inactive, the main load of press frame is generated by the prestress produced by steel wire. Figure 7 is the diagram of the loading rack finite element model. Rack prestress is:

\[ P = \frac{\eta P \delta (1 + 2\epsilon)}{2RB(1 + \epsilon)} \]

where: \( P \) = prestress; \( \eta \) = prestress coefficient; \( P_n \) = nominal load; \( \epsilon \) = working coefficient; \( R \) = radius; \( B \) = wire layer width [18].

Load \( P_1 = 40 \text{MP} \) and \( P_2 = 0.6 \text{MP} \) as the Figure 7, which is equivalent to the pressure when the wire is winding, thus the rack cannot be split. Then, impose constraints on the X / Y / Z three directions on the rack, and take the elastic modulus \( E = 2.0105 \text{MPa} \), poison's ratio \( \lambda = 0.28 \).
3.2.2 Modal Analysis Results and Discussion

Figure 8 is the rack overall deformation, and Figure 9 is the third principal stress of the rack called $\sigma_3$. The overall structure of the rack is under compressive stress; the compressive stress on the column between the 60-100MPa, and the coefficient of column hom together surfaces can be up to 0.4-0.5. So, the hom together surfaces can produce enormous friction, which ensure the security and integrity of the overall rack structure. Figure 10 is the first six order modal analysis results of the overall rack structure.

![Figure 7. Loading rack finite element model diagram](image)

![Figure 8. Rack overall deformation](image)

![Figure 9. Third principal stress of the rack](image)

![Figure 10. First six order modal analysis results of the overall rack structure](image)

<table>
<thead>
<tr>
<th>TABLE 1. Six order modal results</th>
</tr>
</thead>
<tbody>
<tr>
<td>Order number</td>
</tr>
<tr>
<td>1</td>
</tr>
<tr>
<td>2</td>
</tr>
<tr>
<td>3</td>
</tr>
<tr>
<td>4</td>
</tr>
<tr>
<td>5</td>
</tr>
<tr>
<td>6</td>
</tr>
</tbody>
</table>

From Figure 10 and Table 1, it is known that in prestressed state, the deformation of hom together rack is between 38 and 56mm, and resonance frequency increases from 554.41Hz to 3421.8Hz. 56mmis the maximum of rack deformation which is twisting deformation in third mode, and the resonance frequency is 1386.9Hz. In terms of the entire rack, the
maximum rack deformation is relatively small. There are hydraulic cylinders and workbench in the rack, which have inhibitory effect on the deformation of the rack, so the actual deformation is much less than this value.

4. NUMERICAL ANALYSIS OF HOM TOGETHER STRUCTURE RACK

4.1. Hom Together Structure Rack Model

Hom together structure rack is made of top and bottom arch, column, transition plate and wire, which needs high installment precision when it is assembled. Due to improper installation and loading, when the rack is working, there will be eccentric loading, which has a significant impact on the rack. Therefore, the paper construct the mathematical model of hom together structure rack shown as in Figure 11. Obtain the motion equation based on the Lagrange principle [19] expressed as follows:

$$W = \frac{1}{2} m \left( \frac{dx}{dt} - r \frac{d\phi}{dt} \sin \phi \right)^2 + \frac{1}{2} m \left( \frac{dy}{dt} + r \frac{d\phi}{dt} \cos \phi \right)^2$$

$$U = \frac{1}{2} \left( kx^2 + \frac{1}{2} k\phi^2 - T\phi \right)$$

$$D = \frac{1}{2} \left( \frac{dx}{dt} \right)^2 + \frac{1}{2} \left( \frac{dy}{dt} \right)^2 + \frac{1}{2} \left( \frac{d\phi}{dt} \right)^2 \tag{5}$$

where, $W$ is the vibration system kinetic energy, $U$ the system potential energy, $D$ the energy dissipation function, $x$, $y$ the vibration substrate horizontal and vertical displacements, and $\phi$ eccentric blocks of the rotation angle. $M$, $m$, $r$ represent the vibrating substrate mass, eccentric mass, inertia and eccentric distance, respectively. $k$, $c$ and $c_\phi$ are supporting stiffness coefficient, damping, and rotary movement damping; $T$ is the input torque of the motor [19]. Obtain the following equations by Lagrange equations [20]:

$$(M + m) \frac{d^2x}{dt^2} + kx + c \frac{dx}{dt} = mr \left( \frac{d\phi}{dt} \right)^2 \sin \phi + \left( \frac{d\phi}{dt} \right)^2 \cos \phi \tag{8}$$

$$(M + m) \frac{d^2y}{dt^2} + ky + c \frac{dy}{dt} = mr \left( \frac{d\phi}{dt} \right)^2 \cos \phi - \left( \frac{d\phi}{dt} \right)^2 \sin \phi \tag{9}$$

$$\left( J + mr^2 \right) \frac{d^2\phi}{dt^2} = mr \frac{d^2x}{dt^2} \sin \phi + mr \left( \frac{d\phi}{dt} \right)^2 \cos \phi + c_\phi \frac{d\phi}{dt} \tag{10}$$

4.2. Properties of Hom Together Structure Rack

According to Equations (8)-(10), confirm the initial condition: $M=32500kg$, $m=3000kg$, $r=0.8m$, $J=50000 \text{kg} \cdot \text{m}^2$, $k=3000N/m$, $c=60000N \cdot \text{s/m}$, $c_\phi=1000 \text{N} \cdot \text{s/m}$, $T=20000N \cdot \text{m}$, $M=325000kg$. Then, obtain the displacement, velocity and displacement response spectrum of the system by numerical simulation shown in Figure 12. From Figure 12, it is known that the rack vibration characteristics of horizontal and vertical direction are approximate, and the rack resonance frequency is 201Hz. When in the resonance, the amplitude of rack is about 60mm. From (a) and (d), it is known that the maximum speed of eccentric block is about 2.63rad/s, which is far less than the rated speed, thus it is indicated that the hom together structure satisfies the design requirements. Numerical simulation results is consistent with modal analysis results, maximum deformation of rack is slightly larger than the modal analysis, while resonant frequency is lower than the resonant frequency of the modal analysis. It is known that natural frequency of an object is inversely proportional to quality. Through analysis, finite element model natural frequency is larger than mathematical model because of considering the weight of the rack and the eccentric load in the numerical simulation analysis. The results verify that the prestressed hom together structure is reasonable.

Figure 11. Hom together structure rack mathematical model

(a)

(b)
Figure 12. Hom tighet rack system response and resonance spectrum

5. CONCLUSION

(1) Establish the heavy load rack 3D model on the basis of studying the principal of the split-hom together structure. Then analyze the vibration characteristics of heavy load rack in the prestress state and working state. (2) In the prestress state, modal analysis has been done for the rack. The minimum resonance frequency is 554.41Hz, while the maximum deformation is 56mm. The two indexes satisfy the requirements. (3) In the working state, the results of modal analysis could not verify the reliability of the rack because of the eccentric load, so the paper establishes the mathematical model and numerical simulation have been conducted. The resonance frequency is 201Hz and the amplitude of rack is about 60mm. The two indexes satisfy the requirement, too. At the same time, the amplitudes in two states are approximate, but the frequency in the working state is smaller than the other.

Whether in the prestress state or in the working state, the vibration characteristics of heavy load rack can satisfy the requirement, so the reliability of the rack can be verified.

6. REFERENCES

Vibration Characteristics of Heavy Load Rack with Split-hom together Structure

B. Li, L. Hou, R.Q. Mou, Y.Q. Wei

School of Manufacturing Science and Engineering, Sichuan University, Chengdu, China

Keywords:
Fault detection
Thau Observer
Nonlinear Force
Micro-Parallel Plate Capacitor
Noise And Uncertainty

Received 28 June 2014
Received in revised form 21 September 2014
Accepted 13 November 2014