MODIFICATION OF SIDELOBE CANCELLER SYSTEM IN PLANAR ARRAYS

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Abstract A Side Lobe Canceller (SLC) structure is a conventional partially adaptive technique which is used in large adaptive array radars. If a desired signal has long time duration in comparison with the SLC adaptation time, signal components may be cancelled. So, this paper presents a modified SLC which eliminates desired signal cancellation problems and allows using an unconstrained adaptive algorithm. Simulation results demonstrate the performance of this modified structure for a planar array.

Key Words Side Lobe Canceller, Generalized Side lobe Canceller, Adaptive Array, Planar Array

1. INTRODUCTION

An adaptive beamformer is a processor used in conjunction with an array of sensors that is able to separate signals collocated in the frequency band but separated in the spatial domain [1]. This provides a means for separating a desired signal from interfering signals.

Adaptive beamforming started with the invention of the SLC (side lobe canceller) [2] in the latter of 1950's. The fully adaptive array [3] was first conceived as a generalization of the side lobe canceller. A fully adaptive array with every element controllable provides theoretically the necessary side lobes to any arbitrary level.

In large fully adaptive arrays, high computational loads and low convergence speeds are two severe problems. For instance, large phased array radars possess thousands of elements, but practically it is only possible to process a few tens of adaptive degrees of freedom [4]. Hence, reducing adaptive dimension can reduce the system complexity and result in faster adaptive response [5-6]. SLC structure is used in large phased array radars as a partially adaptive technique [7,8].

Desired signal cancellation phenomenon is a problem in the SLC systems. In the initial applications of adaptive processing to radar antennas for sidelobe cancellation, the effects of signals in the main lobe of the adapted response...
were commonly neglected. This was justified by the usually valid assumption that the pulse signals reflected from targets of interest in the main beam were of sufficiently low power and/or duration that the control circuitry of the adaptive processor would not respond to them [9]. In more recent applications, high power and long-duration transmitted waveforms may cause to create a more serious signal cancellation problem [9].

A variety of approaches have been suggested for avoiding this problem in adaptive arrays [7-17]. These methods are categorized as:

1. **Constrained Adaptive Algorithms** [10-12]
   In these approaches, some constraints are imposed directly in the adaption control loops. These techniques can be used in both fully and partially adaptive arrays.

2. **Preadaption Spatial Filters** In this configuration, two beams are formed to applying constraints in an adaptive array. One beam has fixed weights (e.g., uniform, Chebyshev or Taylor) chosen to form the desired quiescent pattern. The second beam is formed by an adaptive processor following a spatial filter that removes the desired signal samples, e.g., fixed element-to-element subtraction [9], or generalized side lobe canceller (GSC) [13]. These methods are used in fully adaptive arrays. More recent partially adaptive arrays based on GSC structure require an accurate estimation of an input data covariance matrix [14-17].

In this paper, we suggested a new approach to SLC systems in the planar arrays based on preadaption spatial filtering which create a null in the direction of the desired signal in the auxiliary channel (adaptive channel) to avoid signal cancellation. The proposed solution method follows the idea first introduced in [7,8]. Simulation results demonstrate the performance of this modified SLC structure.

2. **FULLY ADAPTIVE ARRAY**

For array beamforming with full adaptivity, we consider a planar array with $N_x N_y$ elements shown in Figure 1. Let denote the received signal at $mn$th sensor, at $k$th time step as

$$x_{mn}(k)=S(k)v_{mn}(\theta_s,\phi_s)+\sum_{i=1}^{D}J_{i}(k)v_{mn}(\theta_{i},\phi_{i})+n_{mn}(k)$$

$k = 1, 2, ..., k$

![Figure 1. A planar array of $N_x N_y$ elements located in xy plane.](image-url)
where \( S(k) \) denotes the target signal, \( J_i(k) \) is the \( i \)th interference, \( n_{mn}(k) \) denotes the \( mn \)th element noise which is modeled as a zero-mean spatially white Gaussian random process, and \( v_{mn}(\theta, \phi) \) is expressed as

\[
v(\theta, \phi) = \exp[j \omega \tau_{mn}(\theta, \phi)]
\]

(2)

where \( \tau_{mn}(\theta, \phi) \) is the relation time delay of \( mn \)th element to an arbitrary chosen spatial reference point. With respect to this reference point, \( mn \)th element has location \((x_{mn}, y_{mn}, z_{mn})\). The time delay is given by

\[
\tau_{mn}(\theta, \phi) = \frac{x_{mn} \sin \theta \cos \phi + y_{mn} \sin \theta \sin \phi + z_{mn} \cos \theta}{c}
\]

(3)

where \( c \) is the propagation speed of the incoming waves (signals). Define the \( N_xN_y \) dimensional received vector \( x \), array steering vector \( \phi \theta \), and noise vector \( n \) as

\[
x(k) = \begin{bmatrix}
x_{11}(k), & \ldots, & x_{N_x1}(k), \\
x_{12}(k), & \ldots, & x_{N_xN_y}(k)
\end{bmatrix}^T
\]

(4)

\[
v(\theta, \phi) = \begin{bmatrix}
v_{11}(\theta, \phi), & \ldots, & v_{N_x1}(\theta, \phi), \\
v_{12}(\theta, \phi), & \ldots, & v_{N_xN_y}(\theta, \phi)
\end{bmatrix}^T
\]

(5)

\[
n(k) = \begin{bmatrix}
n_{11}(k), & \ldots, & n_{N_x1}(k), \\
n_{12}(k), & \ldots, & n_{N_xN_y}(k)
\end{bmatrix}^T
\]

(6)

using 1-6, we can express \( x \) as

\[
x(k) = s(k) v(\theta, \phi) + \sum_{i=1}^{D} J_i(k) v(\theta_i, \phi_i) + n(k).
\]

(7)

in narrowband beamforming, a complex weight is applied to the signal at each sensor and sum to form the beamformer output

\[
y(k) = w^H x(k)
\]

(8)

where \( H \) denotes conjugate transpose, and \( w \) is defined as

\[
w^H = \begin{bmatrix} W_{11}, & \ldots, & W_{N_x1}, & W_{12}, & \ldots, & W_{N_xN_y} \end{bmatrix}
\]

(9)

The optimal weight vector \( w \) is found by minimizing the array output power subject to \( L \) linear or derivative constraints as follows

\[
\min_w w^H R_x w \quad \text{subject to} \quad C^H w = f
\]

(10)

where \( R_x \) is the data covariance matrix, \( C \) is the \( N_xN_y \times L \) constraint matrix, and \( f \) is the \( L \times 1 \) vector of constraint values. The optimal solution is

\[
w = R_x^{-1} C (C^H R_x^{-1} C)^{-1} f.
\]

(11)

The GSC, shown in Figure 2, is a widely used beamforming structure that allows an unconstrained adaptive algorithm to be implemented to solve the constrained optimization problem \([12]\). \( w_q \) is the \( N_xN_y \) dimensional quiescent weight vector, \( B \) is the \( N_xN_y \times (N_xN_y - L) \) signal blocking matrix where is orthogonal to \( C \), i.e. \( B^H C = 0 \) (see Appendix of \([17]\)), and \( w_o \) is the optimal weight vector given by
\begin{equation}
\mathbf{w}_a = \left( \mathbf{B}^H \mathbf{R}_x \mathbf{B} \right)^{-1} \mathbf{B}^H \mathbf{R}_x \mathbf{w}_q.
\end{equation}

Let \( y_q(k) = \mathbf{w}_q^H \mathbf{x}(k) \) and \( \mathbf{z}(k) = \mathbf{B}^H \mathbf{x}(k) \) denote the outputs of the quiescent portion of the beamformer and the signal blocking matrix, respectively. The adaptive weights can be expressed as

\begin{equation}
\mathbf{w}_a = \mathbf{R}_z^{-1} \mathbf{p}_z
\end{equation}

where \( \mathbf{R}_z = \mathbf{B}^H \mathbf{R}_x \mathbf{B} \) is the \((N_x N_y - L) \times (N_x N_y - L)\) covariance matrix of \( \mathbf{z}(k) \), and \( \mathbf{p}_z = \mathbf{B}^H \mathbf{R}_x \mathbf{w}_q \) is the \((N - L) \times 1\) cross-correlation vector of \( \mathbf{z}(k) \) and \( y_q(k) \).

### 3. SLC SYSTEM

Large radar arrays contain thousands of elements. Furthermore, digital hardware technology is rapidly advancing to the stage where huge element digitized arrays will be a reality. However, the difficulties of performing adaptive processing with such huge numbers of degree of freedom are well known [4]. Thus, partially adaptive processing techniques are used to reduce adaptive dimensions from thousands into a few tens of spatial degrees of freedom.

The SLC structure is a partially adaptive array, which can be used in two different forms [4] as shown in Figure 3. The conceptual scheme of an SLC system is shown in Figure 4. It consists of a non-adaptive phased-array that is called the main antenna, and an auxiliary array contains of a few controllable elements. The auxiliary antennas may be separate antennas or groups of receiving elements of a phased array antenna.

The purpose of the auxiliaries is to provide a replica of jamming signals in the sidelobes of the main pattern for cancellation. To this end the auxiliary patterns approximate the average sidelobe level of the main antenna receiving pattern [3]. The auxiliary antennas are placed sufficiently close to the phase center of the main antenna to ensure that the samples of the interference that are obtained may be correlated with the interference received in the main antenna sidelobes. Also note that the number of auxiliary antennas must at least equal the jamming signals to be suppressed [18].

In conventional SLC, to prevent target-signal cancellation, its time duration is assumed to be much smaller than the SLC adaptation time. The amount of desired target signal received by the auxiliaries is also assumed to be negligible compared to the target signal in the main channel.

Then, the target signal will pass unchanged through the SLC, while the jammer, which is continuous in time, will be reduced by the adaptation process operated by the canceller [3], [18].

If target signal time duration is not much smaller than the SLC adaptation time, the auxiliary array steers a null in the direction of the target signal, and therefore signal components may be cancelled. To overcome this problem, the previous works consider constrained adaptive algorithms [10-12]. In this paper, we suggest a new technique that allows using an unconstrained adaptive algorithm. Now, we consider a constraint to prevent incoming desired signal samples into an adaptive processor.
\[ w^H_a v_a (\theta_s, \phi_s) = 0 \]  \hspace{1cm} (14)

where \( w^H_a \) is the adaptive weight vector of auxiliary array, and \( v_a (\theta_s, \phi_s) \) is the auxiliary array steering vector along the target-signal direction. Define a blocking matrix as
\[ B = I - v_a (v_a^H v_a)^{-1} v_a^H \]  \hspace{1cm} (15)

where \( v_a = v_a (\theta_s, \phi_s) \) and \( B \) is orthogonal to \( v_a \), i.e., \( B^T v_a (\theta_s, \phi_s) = 0 \). Received data vector of auxiliary array can be expressed as
\[ x(k) = [x_1(k), x_2(k), \ldots, x_{M}(k)]^T \]  \hspace{1cm} (16)

using blocking matrix \( B \), as shown in Figure 5, input data vector of adaptive processor is given by
\[ x_a(k) = B^T x(k) \]  \hspace{1cm} (17)

This input data vector contains just only interferences and noise components, therefore the adaptive processor can only suppress the interferences and noise signals, with independency of the target signal from other signals. In this structure, any unconstrained adaptive algorithm can be used.

4. SIMULATION RESULTS

In this section, several simulation results are presented for illustration and comparison of the performance of a modified SLC for a planar array. We consider a planar array with 14x14 elements and half wavelength element spacing. Quiescent array elements are weighted with 30 dB Dolph-Chebyshev coefficients. The environment consists of a desired signal of power 0 dB, from the look direction \( \theta = 0^\circ, \phi = 10^\circ \) and five jammers with powers 30 dB, 20 dB, 30 dB, 20 dB, and 20 dB from

\[ \theta_1 = -30^\circ, \phi_1 = 10^\circ, \]
\[ \theta_2 = -20^\circ, \phi_2 = 10^\circ, \]
\[ \theta_3 = 30^\circ, \phi_3 = 10^\circ, \]
\[ \theta_4 = 40^\circ, \phi_4 = 10^\circ, \]
\[ \theta_5 = 80^\circ, \phi_5 = 10^\circ, \] respectively.

The receiver noise power is -20 dB. The sample number is 1000. The performance of a conventional SLC, modified SLC and fully adaptive GSC beamformer are compared in Figures 6 and 7. In GSC structure, a constraint of unit gain in the desired signal direction is imposed, i.e. \( f = [1], C = [v(\theta_s, \phi_s)] \). In the modified SLC structure, a null constraint in auxiliary array in the desired signal direction is imposed. GSC and modified SLC structures allow using an unconstrained adaptive algorithm. In both SLC structures, 3 elements in each corner are chosen to
be auxiliary elements, i.e., totally 12 auxiliary elements. Considering the slow convergence speed of LMS algorithm, RLS algorithm has been used.

Figure 6(a) shows the beampattern of the fully adaptive GSC beamformer using a RLS adaptive algorithm. This beamformer maintains the unit gain in the direction of the desired signal and creates nulls in the direction of jammers. The beampattern of the conventional internal SLC is shown in Figure 6(b). This beamformer creates nulls in the direction of jammers, but also has a null in the main lobe in the direction of the desired signal. The modified SLC removes this problem as shown in Figure 6(c).

Figure 6. Azimuth cut at $\phi = 10^\circ$ of (a) fully adaptive GSC-RLS beampattern, (b) conventional Internal SLC-RLS beampattern and (c) modified Internal SLC-RLS beampattern.
Figure 7(a) shows the output of quiescent array that consists of a pulsive desired signal, five jammers and additive noise which are modeled as random processes. Outputs of fully adaptive GSC and conventional SLC are shown in Figures 7(b) and 7(c), respectively. Figure 7(c) shows that the desired signal is canceled as well as interferences and noise. A modified SLC improves the performance of the beamformer and maintains the desired signal as shown in Figure 7(d).
5. CONCLUSION

Conventional SLC systems in large phased arrays, cancel desired signals as well as undesired interferences. This paper suggested a new approach to combat this problem. The proposed technique imposes a null constraint in auxiliary array in the direction of the desired signal, and so eliminates undesirable effects of target signal cancellation phenomenon. This modified structure allows using an unconstrained adaptive algorithm. Several simulation results are shown to demonstrate the performance of this modified SLC in comparison with GSC and conventional SLC in a planar array.

6. REFERENCES