

International Journal of Engineering

Journal Homepage: www.ije.ir

A Two-Stage Green Supply Chain Network with a Carbon Emission Price by a Multiobjective Interior Search Algorithm

N. Torabia, R. Tavakkoli-Moghaddam*b,c, E. Najafia, F. Hosseinzadeh-Lotfid

- ^a Department of Industrial Engineering, Science and Research Branch, Islamic Azad University, Tehran, Iran
- ^b School of Industrial Engineering, South Tehran Branch, Islamic Azad University, Tehran, Iran
- ^c Arts et Métiers ParisTech, LCFC, Metz, France
- ^d Department of Mathematics, Science and Research Branch, Islamic Azad University, Tehran, Iran

PAPER INFO

Paper history: Received 15 January 2019 Received in revised form 15 March 2019 Accepted 21 April 2019

Keywords: Green Supply Chain Network Multi-objective Optimization Carbon Price Interior Search Algorithm Meta-Heuristic Algorithm

ABSTRACT

This paper presented a new two-stage green supply chain network, in which includes two innovations. Firstly, it presents a new multi-objective model for a two-stage green supply chain problem that considers the amount of shortage in the network, reworking, and carbon-trading cost produced in the green supply chain. Secondly, because of the complexity of this model, it uses a new multi-objective interior search algorithm (MOISA) to solve the presented model. The obtained results of the proposed algorithm were compared with the results of other multi-objective meta-heuristics, namely MOPSO, SPEA2, and NSGA-II. The outcomes demonstrate that the proposed MOISA gives better Pareto solutions and indicates the superiority of the proposed algorithm in most cases.

doi: 10.5829/ije.2019.32.06c.05

NOMENCLATURE

Indices		ub_{mwk}	Maximum amount of transportation between manufactury m and warehouse w by vehicle k	
i	Products	ub_{wjk}	Maximum amount of transportation between warehouse w and customer j by vehicle k	
r	Initial parts	ub_{mdk}	Maximum amount of transportation between manufactury m and rework center d by vehicle k	
n	Suppliers	ub_{dwk}	Maximum amount of transportation between rework center d and warehouse w by vehicle k	
d	Rework centers	em_{im}	Carbon emissions for producing one unit of product i in manufactury m	
m	Manufacturer	ed_{id}	Carbon emissions for reworking on the product i in rework center d	
w	Warehouses	et_{imwk}	Carbon emissions for transporting one unit of product i from manufactury m to warehouse w by vehicle k	
Parameters		et'_{iwjk}	Carbon emissions for transporting one unit of product i from warehouse w to customer j by vehicle k	
π	Price of selling and buying carbon emission permit	et''_{imdk}	Carbon emissions for transporting one unit of product i from manufactury m to rework center d by vehicle k	
d_{ij}	Demand of product i for customer j	$et_{idwk}^{\prime\prime\prime}$	Carbon emissions for transporting one unit of product i from rework center d to warehouse w by vehicle k	
cap	Maximum limit of supply chain network pollution	lt_m	Factor of converting the fixed cost of establishing manufactury m to annual cost	
f_m	Fixed cost of establishing manufactory m	lt_w'	Factor of converting the fixed cost of establishing warehouse w to annual cost	

^{*}Corresponding Author Email: tavakoli@ut.ac.ir (R. Tavakkoli-Moghaddam)

Please cite this article as: N. Torabi, R. Tvakkoli-Moghaddam, E. Najafi, F. Hosseinzadeh-Lotfi, A Two-Stage Green Supply Chain Network with a Carbon Emission Price by a Multi-objective Interior Search Algorithm, International Journal of Engineering (IJE), IJE TRANSACTIONS C: Aspects Vol. 32, No. 6, (June 2019) 828-834

£!	Fixed cost of establishing warehouse w	$lt_d^{\prime\prime}$	Factor of converting the fixed cost of establishing rework center <i>d</i>
f_w'	rixed cost of establishing waterlouse w	$\iota\iota_d$	to annual cost
$f_n^{\prime\prime}$	Annual cost of selecting supplier <i>n</i>	eta_i	Percent of product <i>i</i> that needs reworking
$f_d^{\prime\prime\prime}$	Fixed cost of establishing rework center d	eta_i'	Percent of product <i>i</i> that is turned into sound product after reworking
cm_{im}	Production cost of a product unit i in manufactuy m	b	Current budget for establishing manufactories, warehouses and reworking centers
cs_{rnm}	Cost of purchasing one unit of initial parts r from supplier n for manufactury m	Variables	
cd_{id}	Reworking cost of one unit of product <i>i</i> in rework center <i>d</i>	Q_{im}	Number of produced products <i>i</i> in manufactury <i>m</i>
cb_{ij}	Cost of each unit of shortage for product <i>i</i> and customer <i>j</i>	QD_{id}	Number of reworked product i in rework center d
ct_{imwk}	Transportation cost of one unit of product i from manufactury m to warehouse w by vehicle k	R_{rnm}	Number of initial parts r transported from supplier m to manufactury m
ct_{iwjk}^{\prime}	Transportation cost of one unit of product i from warehouse w to customer j by vehicle k	L_{imwk}	Number of product i transported from manufactury m to warehouse w by vehicle k
$ct_{imdk}^{\prime\prime}$	Transportation cost of one unit of product i from manufactury m to rework center d by vehicle k	L_{iwjk}^{\prime}	Number of product i transported from warehouse w to customer j by vehicle k
$ct_{idwk}^{\prime\prime\prime}$	Transportation cost of one unit of product i from rework center d to warehouse w by vehicle k	$L_{imdk}^{\prime\prime}$	Number of product i transported from manufactury m to rework center d by vehicle k
μ_i	Volume of one unit of product <i>i</i>	$L_{idwk}^{\prime\prime\prime}$	Number of product i transported from rework center d to warehouse w by vehicle k
μ_i'	Required time to produce product i	$B_{i j}$	Number of shortage for product i for customer j
$\mu_i^{\prime\prime}$	Required time to reworking on the product i	E	Number of traded carbon emission permit
α_{ri}	Number of required initial part r to produce product i	F_m	Binary decision variable for establishing or not establishing manufactury m
c_{im}	Production capacity (time) of product i in manufactury m	F_w'	Binary decision variable for establishing or not establishing warehouse w
c_w'	Storage capacity in warehouse w	$F_n^{\prime\prime}$	Binary decision variable for selecting or not selecting supplier n
$c_{rn}^{\prime\prime}$	Supply power of supplier n for initial part r	$F_d^{\prime\prime\prime}$	Binary decision variable for establishing or not establishing rework center d
$c_{id}^{\prime\prime\prime}$	Reworking capacity(time) on product i in rework center d	G_{mwk}	Binary decision variable for using or not using the transportation vehicle k between manufactury m and warehouse w
lb_{mwk}	Minimum amount of transportation between manufactury m and warehouse w by vehicle k	G'_{wjk}	Binary decision variable for using or not using the transportation vehicle k between warehouse w and customer j
lb_{wjk}	Minimum amount of transportation between warehouse w and customer j by vehicle k	$G_{mdk}^{\prime\prime}$	Binary decision variable for using or not using the transportation vehicle k between manufactury m and rework center d
lb_{mdk}	Minimum amount of transportation between manufactury m and rework center d by vehicle k	$G_{dwk}^{\prime\prime\prime}$	Binary decision variable for using or not using the transportation vehicle k between rework center d and warehouse w
lb_{dwk}	Minimum amount of transportation between rework center d and warehouse w by vehicle k		

1. INTRODUCTION

Characterized a green supply chain takes a significant role in the supply chain network design. To concern ecological issues, the supply chain management (SCM) forms including item plan, materials determination and sourcing, fabricating, last item conveyance to client and item administration after utilization and time span of usability [1].

In spite of the fact that the ideas of maintainable SCM and green SCM are normally utilized reciprocally all through the supply chain concept, these two ideas are not indistinguishable. Feasible SCM incorporates monetary measurements and ecological and social manageability. Along these lines, maintainable SCM is a more extensive idea in contrast with the green SCM and green SC is a piece of practical supply chain management [2]. Incentives for associations to receive green SCM are distinctive as far as the last client, state offices, private

associations and authoritative organizations. The significant motivator is laws and directions managing association to watch natural issues. Then again, a few associations perform them so as to upgrade the benefit of their principles or clients' request [3]. Taking the minimization of environmental pollution and economic issues into account in the SC design leads to the emergence of the concept of 'green supply chain network design' containing two of the three factors of sustainable development. In a sustainable development program, economic, social and environmental objectives should be simultaneously. Minimization of air considered pollution, collection and recycling commodities at the end of their shelf life are examples of environmental objectives. Concerning the consequences of establishing a factory in the development of a region is an example of social objectives. In this research, minimization of air pollution is studied in the fields of production, warehousing and distribution using emission trading method, in which some parameters are under uncertainty. Emission trading is one of the economic mechanisms of Kyoto Protocol. In this system, an overall limit on emissions is set for each chain, defined based on permits (also called allowances) to emit up to the level of the overall limit. The chains are allowed to trade these permits. After trading permits, each chain is allowed to emit up to the amount of possessed permits. Hence, each chain should decide on spending costs in order to benefit from environmentally better technology for production, transportation and to minimize emissions or on purchasing permits to meet its own needs. Since trading is performed the open market, the price of emission permits is determined based on supply and demand; which is of high uncertainty.

Fahimnia et al. [4] compared the performance of three meta-heuristic algorithms in solving a complex supply chain. Hassanzadeh et al. [5] proposed new NSGA-II and new MOPSO for a bi-objective supply chain scheduling in a flow shop environment. Chibeles-Martins et al. [6] used the multi-objective meta-heuristic approach for the planning and design of green supply chains, which explores the solution space by using a new local search model. Kumar et al. [7] used self-learning particle swarm optimization for multi-objective models of production and pollution routing problem, in this study time window is assumed. Moresi and Schwartz [8] considered a vertically integrated input monopolist supplying to a differentiated downstream rival. They analyzed vertical delegation as one mechanism for inducing expansion or contraction by the rival/customer. Kumar et al. [9] designed multi-objective and multi-period supply chain network with risk and emission, in this study they used NSGA-II for solving problem. Rezaee et al. [10] presented a two-stage model in a stochastic environment to design a green supply chain with carbon price. Qu et al. [11] proposed the taking inventory control out of the hands of competitive or exclusive retailers and assigning it to a manufacturer increases the value of a supply chain especially for goods whose demand is highly volatile. Kadzinski et al. [12] evaluated the applicability of different multi-objective optimization strategies for solving green supply chain problems. Fakhrzad et al. [13] developed a new multi product, multi period, and multi level closed-loop green supply chain planing model under uncertain conditions.

This paper contains two basic innovations. Firstly, a new supply chain model is applied in two stages, with multi-objective functions and the number of shortages and reworks in the model, in which this supply chain model has not been presented in this form of modeling so far in any previous research. Secondly, this new MOISA has not been applied to the supply chain so far, and this algorithm yields very good results in this study. In section 2 of this paper materials and methods presented. In section 3, results and discussion are provided, and a

numerical example is used to demonstrate the adequacy of the model and proposed algorithm. In section 4, conclusion and further studies are provided. In section 5, references are presented.

2. MATERIALS AND METHODS

The model of the intended problem included a multiobjective and two-stage mathematical model. The innovation of this research is to consider the multiobjective and trade off among these objectives in supply chain network and to consider reworking in this multiobjective model. Another innovation in this research is the application of an MOISA algorithm for solving a multi-objective supply chain model, which has not been used for these types of two-stage models yet.

2. 1. Two-Stage Green Supply Chain Network

The model presented in this study consists of two stages. Its first stage includes the selection of supplier, selection and location of establishing manufacturer, reworking centers, and warehouses. These places were selected with certain capacities among potential places. The second stage included the determining amount of products. transportation, type of selected vehicle for moving the products, the amount of initial materials purchased from each supplier, the amount of products that need reworking, the amount of created shortage for the final customer demand and the amount of carbon emission permit. The final products in this model are only delivered to customers through warehouses, so that the products are sent from manufacturer to warehouses or from manufacturer to reworking centers and then from reworking centers to warehouses. Finally, the products are delivered to the customers from warehouses. There are minimum and maximum amounts of transportation in the model and the transportation amount that should be certainly in this range. Figure 1 shows the schematic view of the desired model. After that, parameters, variables and model are presented.

The objective function (1) is related to minimization of manufacturing establishment cost. The objective function (2) is related to minimization of warehouse establishment cost. The objective function (3) is related to minimization of supplier selection cost. The objective function (4) is related to the minimization of rework center establishment cost. The objective function (5) is related to the minimization of the model's second phase. Equation (6) indicates the budget limitation for establishment of manufactories, rework centers and warehouses. Equations (7) to (9) indicate that at least one manufacturer, one warehouse and one rework center should be established. Equation (10) guarantees that the production amount of sound parts is more than the customer's demand. Equation (11) guarantees that the

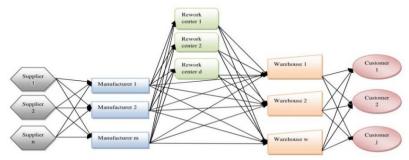


Figure 1. Schematic view of a green supply chain

capacity of rework centers meet the number of parts which need reworking. Equation (12) guarantees that the capacity of suppliers is more than the number of required initial parts. Equation (13) shows the type of decision variables for the model's first phase. The objective function (14) is related to carbon production costs. Equation (15) guarantees the more capacity(time) of manufactories than the required time to produce products. Equation (16) states the relationship between the number of parts, which need reworking and the number of parts which enter rework centers. Equation (17) guarantees the more capacity(time) of reworking center than the Required time for reworking. Equation (18) indicates the number of required parts for producing the final products. Equation (19) indicates the more capacity of suppliers than the number of required initial parts for production. Equation (20) indicates the relationship between the number of sound products and the number of sound products sent from manufactories to warehouses. Equation (21) shows the relationship between the numbers of products which need reworking and the number of products sent from manufactories to rework centers. Equation (22) shows the relationship between the number of sound products after reworking and the number of products sent from rework centers to warehouses. Equation (23) guarantees that the capacity of warehouses is more than the number of products sent from manufactories and rework centers to warehouses. Equation (24) shows the equality between the products imported to warehouse and the products exported. Equation (25) shows the relationship between the number of products imported to warehouse and the amount of shortage than the customer demand. Equation (26) shows the number of carbon emission permit than production pollution and transportation pollution. Equations (27) to (30) show the minimum and maximum limitations for transportation. Equations (31) to (33) show the type of decision variables for the model's second phase.

$$Min \sum_{m} lt_{m} f_{m} F_{m} \tag{1}$$

$$\operatorname{Min} \sum_{w} \operatorname{lt}'_{w} f'_{w} F'_{w} \tag{2}$$

$$\operatorname{Min} \, \sum_{\mathbf{n}} f_{\mathbf{n}}^{\prime\prime} F_{\mathbf{n}}^{\prime\prime} \tag{3}$$

$$\operatorname{Min} \ \sum_{\mathbf{d}} \operatorname{lt}_{\mathbf{d}}^{\prime\prime\prime} \mathbf{f}_{\mathbf{d}}^{\prime\prime\prime\prime} \mathbf{F}_{\mathbf{d}}^{\prime\prime\prime} \tag{4}$$

Min
$$Q(F, F', F'', F''')$$
 (5)

$$\sum_{m} f_{m} F_{m} + \sum_{w} f'_{w} F'_{w} + \sum_{d} f'''_{d} F'''_{d} \le b$$
 (6)

$$\sum_{m} F_{m} \ge 1 \tag{7}$$

$$\sum_{w} F'_{w} \ge 1 \tag{8}$$

$$\sum_{\mathbf{d}} F_{\mathbf{d}}^{\prime\prime\prime} \ge 1 \tag{9}$$

$$(1 - \beta_i) \sum_i \sum_m c_{im} F_m + \beta_i' \sum_i \sum_d c_{id}^{"'} F_d^{"'} \ge \sum_i \sum_j d_{ij}$$
 (10)

$$\beta_{i} \sum_{i} \sum_{m} c_{im} F_{m} \le \sum_{i} \sum_{d} c_{id}^{\prime\prime\prime} F_{d}^{\prime\prime\prime}$$

$$\tag{11}$$

$$\sum_{n} c_{rn}'' F_{n}'' \ge \sum_{i} \sum_{j} d_{ij} \alpha_{ri} \qquad \forall r \tag{12}$$

$$F_{m}, F'_{w}, F''_{n}, F'''_{d} \in \{0,1\}$$
 (13)

$$Q(F, F', F'', F''') = \operatorname{Min} \sum_{i} \sum_{m} \sum_{w} \sum_{k} \operatorname{ct}_{imwk} L_{imwk}$$

$$+ \textstyle \sum_i \sum_w \sum_j \sum_k ct'_{iwjk} \, L'_{iwjk}$$

$$+\sum_{i}\sum_{m}\sum_{d}\sum_{k}\operatorname{ct}_{imdk}^{"}L_{imdk}^{"}$$
(14)

$$+ \textstyle \sum_{i} \sum_{d} \sum_{w} \sum_{k} ct_{idwk}^{\prime\prime\prime} L_{idwk}^{\prime\prime\prime} + \sum_{i} \sum_{m} cm_{im} Q_{im}$$

$$+\sum_{i}\sum_{d}cd_{id}QD_{id}$$

$$+\sum_{r}\sum_{m}\sum_{n}cs_{rnm}R_{rnm} + \sum_{i}\sum_{j}cb_{ij}B_{ij} + \pi E$$

$$\sum_{i} \mu_{i}' Q_{im} \le \sum_{i} c_{im} F_{m} \qquad \forall m$$
 (15)

$$\sum_{d} QD_{id} = \sum_{m} \beta_{i}Q_{im} \qquad \forall i \qquad (16)$$

$$\sum_{i} \mu_{i}^{\prime\prime} Q D_{id} \leq \sum_{i} c_{id}^{\prime\prime\prime} F_{d}^{\prime\prime\prime} \qquad \forall d \qquad (17)$$

$$\sum_{n} R_{rmn} = \sum_{i} \alpha_{ri} Q_{im} \qquad \forall r, m$$
 (18)

$$\sum_{m} R_{rmn} \le c_{rn}^{"} F_{n}^{"} \qquad \forall r, n \tag{19}$$

$$\sum_{\mathbf{w}} \sum_{\mathbf{k}} \mathbf{L}_{\text{imwk}} = (1 - \beta_{\mathbf{i}}) \mathbf{Q}_{\text{im}} \qquad \forall \mathbf{i}, \mathbf{m}$$
 (20)

$$\sum_{m} \sum_{k} L_{imdk}^{"} = QD_{id} \qquad \forall i, d \qquad (21)$$

$$\sum_{w} \sum_{k} L_{idwk}^{\prime\prime\prime} = \beta_{i}^{\prime} Q D_{id} \qquad \forall i,d \qquad (22)$$

$$\sum_{i} \sum_{m} \sum_{k} \mu_{i} L_{imwk} + \sum_{i} \sum_{d} \sum_{k} \mu_{i} L_{idwk}^{\prime\prime\prime} \le c_{w}^{\prime} F_{w}^{\prime} \quad \forall w \quad (23)$$

$$\sum_{i} \sum_{k} L'_{iwik} = \sum_{m} \sum_{k} L_{imwk} + \sum_{d} \sum_{k} L'''_{idwk} \quad \forall i, w$$
 (24)

$$\sum_{\mathbf{w}} \sum_{\mathbf{k}} \mathbf{L}'_{i\mathbf{w}i\mathbf{k}} + \mathbf{B}_{i\,i} = \mathbf{d}_{ii} \quad \forall i, j$$
 (25)

$$\begin{array}{l} \sum_{i} \sum_{m} \sum_{w} \sum_{k} \operatorname{et}_{imwk}^{i} L_{imwk} + \\ \sum_{i} \sum_{w} \sum_{j} \sum_{k} \operatorname{et}_{iwjk}^{i} L_{iwjk}^{i} + \sum_{i} \sum_{m} \sum_{d} \sum_{k} \operatorname{et}_{imdk}^{\prime\prime} L_{imdk}^{\prime\prime} + \\ \sum_{i} \sum_{d} \sum_{w} \sum_{k} \operatorname{et}_{idwk}^{\prime\prime} L_{idwk}^{\prime\prime\prime} + \sum_{i} \sum_{m} \operatorname{em}_{im} Q_{im} + \\ \sum_{i} \sum_{d} \operatorname{ed}_{id} Q D_{id} - \operatorname{cap} = E \end{array} \tag{26}$$

$$lb_{mwk}G_{mwk} \le \sum_{i} \mu_{i}L_{imwk} \le ub_{mwk}G_{mwk} \quad \forall m, w, k \quad (27)$$

$$lb_{wjk}G'_{wjk} \le \sum_{i} \mu_{i}L'_{iwjk} \le ub_{wjk}G'_{wjk} \quad \forall w, j, k$$
 (28)

$$lb_{mdk}G''_{mdk} \le \sum_{i} \mu_{i}L''_{imdk} \le ub_{mdk}G''_{mdk} \quad \forall m, d, k$$
 (29)

$$lb_{dwk}G'''_{dwk} \le \sum_{i} \mu_{i}L'''_{idwk} \le ub_{dwk}G'''_{dwk} \quad \forall d, w, k$$
 (30)

$$F_{m}$$
, F'_{w} , F''_{n} , F'''_{d} , G_{mwk} , G'_{wjk} , G''_{mdk} , G'''_{dwk} $\in \{0,1\}$
 $\forall m, w, n, d, k, j$ (31)

$$Q_{im}$$
, QD_{id} , B_{ij} , R_{rnm} , L_{imwk} , L'_{iwjk} , L''_{imdk} , $L'''_{idwk} \ge 0$ and integer $\forall i, m, w, n, d, k, j$ (32)

2. 2. Multi-objective Interior Search Algorithm

In the multi-objective interior search algorithm (MOISA), concepts of the ISA [14] are used in conjunction with the principles of the crowding distance and non-dominated sorting. In the proposed algorithm, those stages of process that require sorting out the original population use the two mentioned principles for this purpose. By considering literature [15] metaheuristic multi objective interior search algorithm used for solving gscm model presented in this paper. The pseudo code of MOISA is as follows:

Initialization
while any stop criteria is not satisfied
use the non dominated sorting
use the crowding distance
find the Pareto fronts
choose one of the solution in the first Pareto front as x^{j}_{gb}
for $i=1$ to n
$if x_{gb}$
$x^{j}_{gb} = x^{j-1}_{gb} + r_n \times \lambda$
else if r₁ ≤a
$x^{j}_{m,i} = r_3 x^{j-l}_{i} + (1-r_3) x^{j}_{gb}$
$x^{j}_{i}=2 x^{j}_{m,I}-x^{j-1}_{i}$
else
$x^{j}_{i}=LB^{j}+(UB^{i}-LB^{j})\times r_{2}$

```
end if check the boundaries except for decomposition elements end for for i=1 to n evaluate the f(x_i^j) x_i^j = \begin{cases} x_i^j & \text{if } f\left(x_i^j\right) \text{ dominates } f\left(x_i^{j-1}\right) \\ x_i^{j-1} & \text{else} \end{cases} end for end while
```

3. RESULTS AND DISCUSSION

Numerical examples should be used to guarantee the efficiency of the presented model. Four meta-heuristic algorithms, namely MOPSO, NSGA-II, SPEA 2 and MOISA, are used to solve the given examples. The following four comparative factors are considered to determine the algorithms that have a better performance in solving the proposed model.

- 1. Mean ideal distance (MID): This criterion calculates the mean Pareto solutions from the coordinate's origin. The less is this criterion, the more is the algorithm efficiency.
- 2. Spacing (S): This criterion calculates the relative distance of consecutive solutions. The less is the index, the better it is [16].
- 3. Number of Pareto solutions (NOS): The more is the number of Pareto solutions, the more optimal will be that method.
- 4. Solving time (TIME): This factor is measured based on the number of function evaluations, the less is the better.

Numerical examples are considered at three levels of small, medium and large. The values of the model's indices for these three levels are given in Table 1. Table 2 shows the parameter setting results from Taguchi method. The stopping condition of algorithms is equal to the number of function evaluation=10000. Each example is run 50 times with each algorithm. Table 3 shows the average results of model solving.

TABLE 1. Values for three levels of the indices.

	Level 1	Level 2	Level 3
i	[3,5]	[10,14]	[25,35]
r	[3,5]	[10,14]	[25,40]
n	[5,7]	[15,18]	[25,35]
d	[4,6]	[10,14]	[20,25]
m	[6,8]	[12,15]	[25,35]
w	[5,8]	[9,14]	[25,35]
k	[7,10]	[15,20]	[35,50]
<u>j</u>	[10,15]	[20,25]	[35,45]

TABLE 2. Parameter setting results from Taguchi method

NSGA II	MOPSO	SPEA II	MOISA
Population size=	Population size= 1000	Population size= 1000	Population size= 1000
Mutation Rate= 0.1	Repository Size=300	Archive Size=500	Alpha=0.4
P Crossover=0.7 P Mutation=0.2	Inertia Weight=0.5 Personal Learning Coefficient=1	P Crossover=0.7 P Mutation=0.3	
	Global Learning Coefficient=2		
	Number of Grids per Dimension=10		
	Alpha=0.1		
	Beta=2		
	Gamma=2		
	Mutation Rate=0.1		

TABLE 3. Average results of model solving

Criterion				
Level 1	Time	NOS	S	MID
NSGAII	920.797	40	3.3438×10^5	2.2132×10^7
SPEA-2	850.15	43	3.0012×10^5	2.0744×10^7
MOPSO	950.51	39	3.4431×10^5	2.3332×10^7
MOISA	880.31	48	2.8911×10^5	2.0232×10^7
Level 2	Time	NOS	S	MID
NSGAII	16854.23	41	7.8823×10^6	1.8061×10^9
SPEA-2	15120.16	47	7.2451×10^6	1.7319×10^9
MOPSO	17001.65	38	8.2141×10^6	2.0198×10^9
MOISA	14790.21	46	6.9917×10^6	1.6531×10^9
Level 3	Time	NOS	S	MID
NSGAII	294671.34	40	1.2556×10^7	8.4346×10^9
SPEA-2	290154.23	43	1.1144×10^7	8.1978×10^9
MOPSO	295771.98	35	1.5071×10^7	8.7712×10^9
MOISA	288156.32	47	1.0142×10^7	8.0011×10^9

Figure 2 shows the average results obtained by solving the model using different algorithms. In the first level, the performance of the proposed MOISA is better in the MID, S and NOS criteria. The performance of the SPEA-2 algorithm is better in criterion TIME. In the second level, the performance of the proposed MOISA is better in the MID and S criteria. The performance of the SPEA-II algorithm is better in criterion NOS. The performance of MOISA algorithm was better in criterion TIME. In the third level, the performance of the proposed MOISA is better in MID, S, NOS and TIME criteria.

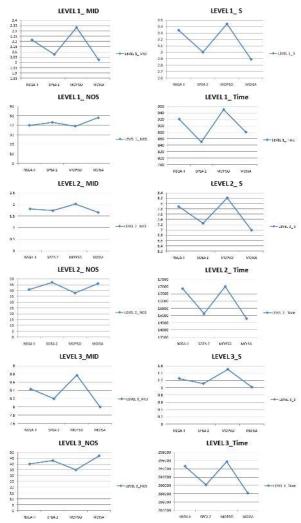


Figure 2. Values of the criteria for the average results

4. CONCLUISION

This study present the application of a new multiobjective interior search algorithm (MOISA) has studied to solve a two-stage green supply chain network. The innovation of this research is to consider the multiobjective and trade off among these objectives in supply chain network and to consider shortage and reworking in this multi objective model. Another innovation in this research is the application of a MOISA algorithm for solving a multi-objective supply chain model, which has not yet been used for this model. A comparison between the proposed MOISA and three well-known algorithms, namely NSGA-II, MOPSO and SPEA2, was carried out by using four specific criteria of Pareto solutions. The numerical example was considered for solutions at three different problem sizes. In most cases, the proposed MOISA showed better results than other algorithms. For future study, the presented model can be expanded under uncertainty. The model can be used for examples

in the field of fuzzy, interval and gray numbers. Additionally, by combining single-objective metaheuristic algorithms, we can also create new methods for solving multi-objective models by combining their properties together. Furthermore, other factors (e.g., considering products return by customers, initial inventory, and time periods for production) can be considered in the model.

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A Two-Stage Green Supply Chain Network with a Carbon Emission Price by a Multiobjective Interior Search Algorithm

N. Torabia, R. Tavakkoli-Moghaddamb,c, E. Najafia, F. Hosseinzadeh-Lotfid

^a Department of Industrial Engineering, Science and Research Branch, Islamic Azad University, Tehran, Iran

چكيده PAPER INFO

Paper history: Received 15 January 2019 Received in revised form 15 March 2019 Accepted 21 April 2019

Keywords: Green Supply Chain Network Multi-objective Optimization Carbon Price Interior Search Algorithm Meta-Heuristic Algorithm این مقاله به ارائه یک مدل نوین دو مرحلهای از شبکه زنجیره تامین سبز میپردازد. این مطالعه شامل دو نوآوری است. نخست، یک مدل جدید چند هدفه برای مسئله زنجیره تامین سبز دو مرحلهای ارائه می دهد که میزان کمبود در شبکه، دوباره کاری و هزینههای کربن تولید شده در زنجیره تامین سبز را در نظر می گیرد. ثانیا، به دلیل پیچیدگی مدل ارائه شده، از یک الگوریتم جستجوی داخلی چند هدفه (MOISA) برای حل آن استفاده شده است. نتایج به دست آمده از الگوریتم پیشنهادی با دیگر الگوریتمهای فراابتکاری چند هدفه، مثل SPEA2 'MOPSO و SPEAZ مقایسه گردیده است. نتایج نشان می دهد که الگوریتم پیشنهادی در مقایسه با دیگر دهد که الگوریتم پیشنهادی در مقایسه با دیگر الگوریتمها نتایج بهتری حاصل نموده است.

doi: 10.5829/ije.2019.32.06c.05

^b School of Industrial Engineering, South Tehran Branch, Islamic Azad University, Tehran, Iran

^cArts et Métiers ParisTech, LCFC, Metz, France

 $^{{}^}d$ Department of Mathematics, Science and Research Branch, Islamic Azad University, Tehran, Iran