



Low Settling Time All Digital DLL for VHF Application

H. Rahimpour^a, M. Gholami^{*b}, G. Ardeshir^c, H. MiarNaimi^c

^aDepartment of Electrical Engineering, University of Tehran, Iran

^bDepartment of Electrical and Electronic Engineering, University of Mazandaran, Iran

^cDepartment of Electrical and Computer Engineering, BabolNoshirvani University of Technology, Iran

PAPER INFO

Paper history:

Received 20 May 2013

Received in revised form 17 May 2014

Accepted 18 November 2014

Keywords:

DLL

Delay Locked Loop PRP

Conjugate Gradient

Algorithm

Synthesizer

ABSTRACT

Delay Locked Loops (DLLs) and Phase Locked Loops (PLLs) are commonly used as a synthesizer or clock and data recovery circuit in most of the communication systems. In this paper, a new DLL is designed based on PRP conjugate gradient algorithm. The proposed DLL do not need any phase frequency detector, charge pump and loop filters, hence it can contribute better jitter performance and higher speed in comparison with conventional DLLs. In this design, PRP conjugate gradient algorithm is used to optimize the delay amount of each delay cells therefore helps the DLL to lock more accurately and quickly compared with gradient algorithm. In addition, for applying the PRP conjugate gradient algorithm a digital signal processor is used in the proposed architecture. To show the accuracy of the proposed structure's operation, simulation has been done for 15 delay cells and f_{REF} is chosen 14MHz to have output frequency $14 \times 15 = 210$ MHz. $f_{OUT} = 210$ MHz is one of the channels in Iran VHF frequency band. As shown with simulation, the proposed architecture has a locking time of approximately 286nsec which is equal to 4 clock cycles of the reference clock.

doi: 10.5829/idosi.ije.2015.28.03c.11

1. INTRODUCTION

Nowadays, Delay Locked Loops (DLLs) and Phase Locked Loops (PLLs) are widely used in communication systems. They are applied in most of the clock synchronization circuits [1, 2], frequency synthesizers [3, 4], digital transceivers [5], RAMs [6, 7] and clock and data recovery circuits [8]. One of the most important parameter in design of transceivers is related to their jitter contribution. DLLs have better jitter performance than PLLs. Hence, in recent years they are widely used in communication systems [9, 10]. In addition, DLLs are used as a clock multiplier or synthesizer to multiply the reference frequency and control the carrier frequency of different channels [11]. Application of DLLs is increasing rather than PLLs because of the faster locking process [12], lower phase noise [13], lower jitter [14], and better stability conditions.

There are some design challenges in DLLs which show their performance. Speed limitations, settling time, working frequency, power consumption and their performance are the most important challenges in the design of DLLs. The conventional DLLs suffer from large lock time (their lock time is in the range of 50 and more clock cycles). Hence, new works in the field of DLL try to implement DLLs with lower lock time. Examples of high speed DLLs are [15] and [16] which proposed fast lock and wide range DLL, however, they need 15 and 22 clock cycles to lock, respectively. In high frequency application, it is still required to decrease the number of clock cycles to lock. In this regard, [12] propose a new digital with better lock time rather than pervious works. In this design, gradient algorithm is used for DLL architecture to reach better lock time. Also, a high speed DLL based frequency synthesizer is designed in [11] to cover VHF frequency band by using gradient algorithm. As we can see, nowadays having high speed DLLs is of importance. Therefore, to improve lock time of DLLs, a new all-digital and fast lock DLL-based frequency multiplier is proposed in this paper. One of the main advantages of

*Corresponding Author's Email: mgh_elec@yahoo.com (M. Gholami)

the proposed circuits is that it uses a digital signal processor instead of the phase-frequency detector, charge pump and loop filter. This results in the smaller chip area and locking time than conventional DLLs. To find optimized values for each delay cell, the PRP Conjugate Gradient algorithm is applied to the structure which has more speed than gradient algorithm. PRP Conjugate Gradient algorithm controls the error signal, which is defined as the difference of input and output signal tend to zero. Therefore, when the error signal becomes zero, input and output signals are exactly in phase, which is also needed in DLLs.

The paper is organized as follows. The next section describes the PRP Conjugate Gradient Algorithm and the proposed all-digital fast lock architecture for DLL-based frequency multipliers based on the limitation of conventional DLLs. Simulation and results will be presented in Section 3. Section 4, concludes the paper.

2. PROPOSED FAST-LOCK DLL BASED ON PRP CONJUGATE GRADIENT ALGORITHM

Conventional DLL-based frequency multiplier consists of a Voltage Controlled Delay Line (VCDL), a Phase-Frequency Detector (PFD), a Charge Pump (CP), a first-order Loop Filter (LF) and an Edge Combiner. In the locked condition, the output of the last delay stage is exactly one cycle lagged from the reference clock. Assuming similar delay cells are used in the signal path, the resulting delay of each of them is equal to T_{REF}/N , where N is the number of delay cell and T_{REF} is the period of a reference signal. When the DLL is locked, the edge combiner combines the edges of delay stages output's to produce an integer multiple of the input frequency. In this case when N is even, the maximum output frequency is $(N/2) \times f_{REF}$ and when N is odd, the maximum output frequency is $N \times f_{REF}$ [17].

Conventional DLL based frequency multipliers occupy large area because of using capacitors in VCDL and LF [12]. Other parameters which are needed to be improved in conventional DLLs are locking time and working frequency. Also, there is another important limitation for conventional DLL-based frequency multipliers which is called a limited locking range. The DLL can be locked only when the following non-equality is satisfied [18]:

$$\frac{1}{2}T_{REF} \leq t_{VCDL} \leq \frac{3}{2}T_{REF} \quad (1)$$

where T_{REF} is the period of reference clock and t_{VCDL} the delay of the VCDL. If a delay of VCDL is in a range of (1) in whole time domain, the DLL can lock properly. Hence, harmonic lock and false lock cannot happen.

Optimization problems naturally arise from applications such as signal processing, data analysis, network design, etc. Among many applications, error signal optimization

(minimization) has attracted much attention. The general form of the optimization problem is to minimize (or maximize) $f(x)$ where $x \in R^n$.

One of the simplest and most efficient methods to solve the above equation is a gradient method proposed by Cauchy in [19]. In this method, the value of x is calculated by the following recursive relation:

$$x_{k+1} = x_k - \alpha_k g_k \quad (2)$$

where $g_k = \nabla f(x_k)$ is the gradient of $f(x)$ at $x = x_k$. Obviously, this method is useful when the gradient of $f(x)$ is available and is not complicated to obtain. α_k is a coefficient that determines the convergence speed.

In general form, x is n -dimensional. So, gradient vector is used in (3) to form n -dimensional variable in recursive relation, but in this paper target function for optimization has one-dimensional variable. Hence, gradient in general recursive relation (3) is replaced with derivative. As a result, (3) is converted to:

$$x_{k+1} = x_k - \alpha_k f'(x_k) \quad (3)$$

The larger the value of α_k , the faster the convergence speed. It should be noted that if this coefficient is too large, then the system will be unstable. The gradient algorithm experiences a constant evolutionary path to reach the optimum solution. So, gradient algorithm has some drawbacks ([20, 21]) such as low convergence speed. α_k in (2) can be considered as a variable value depending on the instantaneous gradient value. In this situation convergence of $f(x)$ can be expedited.

One of the most powerful methods for solving optimization problems is conjugate gradient due to its simplicity and low memory requirements. This method has proper performance especially for large-scale optimization problems. The general form of this algorithm is:

$$x_{k+1} = x_k - \alpha_k d_k \quad (4)$$

where α_k is a scalar, and d_k is considered as:

$$d_k = -f'(x_k) + \beta_k d_{k-1}, \quad d_0 = -f'(x_0) \quad (5)$$

β_k is a scalar in the above equation. Relations (4) and (5) form the core of the conjugate gradient algorithm. Also, β_k can be considered as a variable value which changes with the instantaneous gradient and x values. There are several relations for β_k which identify different methods of the conjugate gradient algorithm [22-26]. One of the most efficient relations for β_k in the point of computational view, is the following PRP (Polak Ribiere Polyak) method in which β_k^{PRP} will be calculated as follows:

$$\beta_k^{PRP} = \frac{g_{k+1}^T (g_{k+1} - g_k)}{\|g_k\|^2} \quad (6)$$

where g_k and g_{k+1} are representing the gradient values $\nabla f(x_k)$ and $\nabla f(x_{k+1})$ in the points of x_k and x_{k+1} respectively. So, the recursive relation to d_k in PRP

conjugate gradient algorithm will be obtained as follows:

$$d_k = -g_k + \frac{g_{k+1}^T(g_{k+1} - g_k)}{\|g_k\|^2} d_{k-1} \quad (7)$$

with changes convergence speed will not be linear. Thus, the performance of the conventional gradient method will be improved. In the next section, PRP conjugate gradient algorithm is used to find an optimum value for delay of each delay cells in proposed DLLs.

As it has been shown in pervious section, conventional DLLs contain VCDL, CP, LF and PFD. It will be shown that these blocks can be substituted by a powerful digital signal processor (DSP). Therefore, input and output signals should be compared in a way to keep the phase difference exactly equal to T_{REF} between them. To determine feedback path of the proposed DLL an error signal is needed which should be optimized by a PRP conjugate gradient algorithm which will be explained in this section.

The general form of square signal is written as:

$$V_i(t) = A_1 \sin \omega t + A_2 \sin 2\omega t + A_3 \sin 3\omega t + \dots \quad (8)$$

Due to intrinsic delay in each signal path, the output signal can be written as $V_i(t - \tau)$. In other words, output signal is defined as input signal with delay of τ , where τ is the intrinsic delay in the signal path and it is a very small value. Due to intrinsic delay of VCDL, τ cannot be zero and in DLLs, a delay is needed to synchronize input and output of the VCDL. Hence, some blocks should be added to make the delay of signal path equal to T_{REF} . Having N similar delay blocks in the signal path with the same delay of μ , the total amount of delay will be $N\mu$. As a result, a feedback path should be added to control the amount of μ to set it to $\frac{T_{REF}}{N}$ in the lock condition. By using N delay cells, the output signal can be written as:

$$V_o(t) = V_i(t - N\mu) \quad (9)$$

The added feedback path should be controlled adaptively. Hence, a signal is required to identify the phase difference between the input and output signals. This signal can be obtained by subtracting the input signal from the output signal. So:

$$e(t) = V_o(t) - V_i(t) = A_1(\sin \omega(t - N\mu) - \sin \omega t) + A_2(\sin 2\omega(t - N\mu) - \sin 2\omega t) + A_3(\sin 3\omega(t - N\mu) - \sin 3\omega t) + \dots \quad (10)$$

This signal is known as an error signal which should tend to zero. When this error signal is equal to zero, then the output signal will be exactly in phase with the input signal. In this situation each cell propose a delay value of $\frac{T_{REF}}{N}$.

The target function for optimization is equal to:

$$J_\mu(t) = |e^2(t)| \quad (11)$$

The PRP conjugate gradient algorithm is used in the feedback path to control the amount of each delay cell dynamically. The reference signal which is used in this control process is $e(t)$. This means that μ is changed with the reference signal $e(t)$ by using an adaptive conjugate gradient algorithm. Since, $e(t)$ is a real function, $|e^2(t)|$ is equal with $e^2(t)$.

To obtain a recursive relation for μ , it is essential to calculate $\frac{\partial J_\mu(t)}{\partial \mu}$ as:

$$\frac{\partial J_\mu(t)}{\partial \mu} = \frac{\partial e^2(t)}{\partial \mu} = \left(\frac{\partial}{\partial \mu} [A_1(\sin \omega(t - N\mu) - \sin \omega t) + A_2(\sin 2\omega(t - N\mu) - \sin 2\omega t) + A_3(\sin 3\omega(t - N\mu) - \sin 3\omega t) + \dots]^2 \right) \quad (12)$$

The above equation will be arranged to:

$$\frac{\partial J_\mu(t)}{\partial \mu} = -2N \frac{\partial V_o(t)}{\partial t} [V_o(t) - V_i(t)] = -2N \frac{\partial V_o(t)}{\partial t} e(t) \quad (13)$$

As a function $f(x)$ in Equation (2), the target function for optimization is $J_\mu(t)$. Therefore, according to the PRP conjugate gradient algorithm, the recursive relation for μ is:

$$\mu_{k+1} = \mu_k - \alpha_k d_k \quad (14)$$

where d_k is:

$$d_k = -\frac{\partial J_\mu(k)}{\partial \mu} + \beta_k^{PRP} d_{k-1}, \quad d_0 = -\frac{\partial J_\mu(0)}{\partial \mu} \quad (15)$$

Substituting (13) in (15) and according to PRP conjugate gradient algorithm, d_k can be obtained:

$$d_k = -2N \frac{\partial V_o(k)}{\partial t} e(k) + \frac{\frac{\partial J_\mu(k)}{\partial \mu} (\frac{\partial J_\mu(k+1)}{\partial \mu} - \frac{\partial J_\mu(k)}{\partial \mu})}{\|\frac{\partial J_\mu(k)}{\partial \mu}\|^2} d_{k-1} \quad (16)$$

$$, d_0 = -2N \frac{\partial V_o(0)}{\partial t} e(0)$$

It should be mentioned that each delay cell is controlled with the same recursive relation. Using this method, the speed of convergence can be measured by analyzing the time evolution of the locking process. The step size parameters, α_k and β_k are chosen as a constant value to reduce the system transient time.

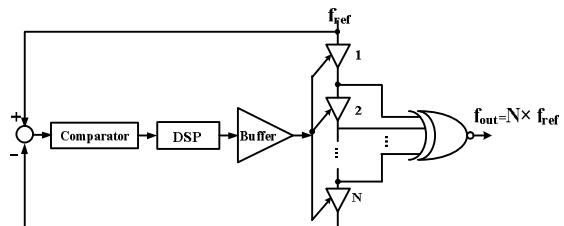


Figure 1. Proposed all-digital fast lock DLL

According to the above equations, the proposed DLL structure can be obtained which is shown in Figure 1. According to this figure, the proposed architecture consists of a comparator, buffer, subtractor, DSP, delay cells and an XOR gate. The input signal of DSP is the difference between input and output signals. DSP compute an optimum value of delay for each delay cell to have a zero error signal. It should be noted that, DSP in Figure 1 will not lead to consume any excess power for proposed DLL, because the presence of DSP in digital communication is inevitable and adding one more output and input ports in DSP will not change power consumption significantly. As an example, in transceivers which contain DLLs, a DSP is used for choosing different kinds of modulations [27]. Control signal of delay cells is provided from this DSP. This means PFD, CP, and LF is eliminated in the proposed architecture in comparison with conventional DLLs. Hence, power consumption and area of proposed architecture will be decreased significantly.

3. SIMULATIONS AND RESULTS

Simulation has been done for $N=15$ and $f_{REF} = 14\text{ MHz}$ to validate the function of the proposed all-digital fast lock DLL. Figure 2 shows the normalized magnitude of the error signal. When the output signal reaches about 95% of its steady state, it will be considered as lock condition. According to this figure, the error signal becomes zero after 286ns. This means that after 4 clock cycles, the proposed DLL will lock. In lock condition delay of each delay cells is equal with $\frac{T_{REF}}{N} = \frac{1}{N \cdot f_{REF}} = \frac{1}{15 \times 14 \times 10^6}$ which is around 4.76 nsec .

Figure 3 shows the delay value of each delay cell. In lock condition where the output signal reaches about 95% of its steady state, the delay of each delay cell is equal to 4.76 nsec . Figures 2 and 3 show that the proposed structure can lock very fast in only 4 clock cycles. Low jitter functionality of our proposed DLL can be proved by comparing the ripple of delay of each delay cell around its stable value and also the ripple of error signal (Figures 2 and 3). This work has little changes near the stable value, but other works propose more oscillation around their steady states which leads to more jitter of their works [17]. Figure 4 shows the related waveforms of the proposed all-digital fast lock DLL. This figure shows that output and input of the proposed architecture are exactly in phase after lock condition (output is one period lagged from input). This figure also illustrates that by combining edges of all delay stage's output with XOR gates, multiplied output frequency is $f_{out} = 15 \times f_{REF}$ which is equal to 210 MHz .

Figure 4 shows the magnitude of error, input and output signals. This figure shows that around $t=0.1\mu\text{s}$, input and output signals of DLL are not in phase. In this case the magnitude of the error signal is not exactly zero. In other words, this signal shows that the input and output of the DLL have some phase differences.

Then, DSP forces the error signal to tend to zero by using a PRP conjugate gradient algorithm. As shown in Figure 4, after 4 clock cycles, the DLL is approximately locked. This figure also shows that after $t=0.5\mu\text{s}$, input and output of DLL are exactly in phase and the lock condition is completely obtained. Since the DSP block can be implemented by analog circuits, the proposed DLL will operate at higher frequencies and consume lower power and area than conventional DLLs. Similar works such as [15, 16, 28] and [29] need minimum of 15, 22, 32 and 34 clock cycles to be locked, respectively, while as the simulations show, the proposed architecture needs only 4 clock cycles. To have the correct lock in DLLs, Equation (1) should be satisfied. It is the only limitation which does not allow DLLs to work in higher or lower frequencies because of delay amount of more than $3T/2$, DLL will have harmonic lock which causes an output signal to lag as much as mT_{REF} (m is an integer greater than one) from the input signal.

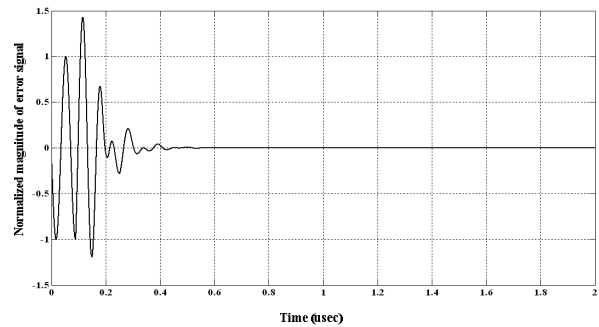


Figure 2. Normalized Magnitude of Error signal

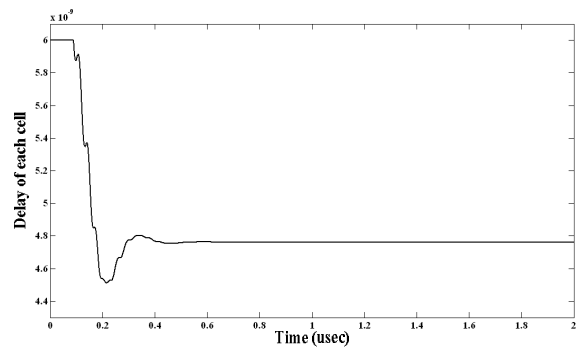


Figure 3. Delay of each delay cell

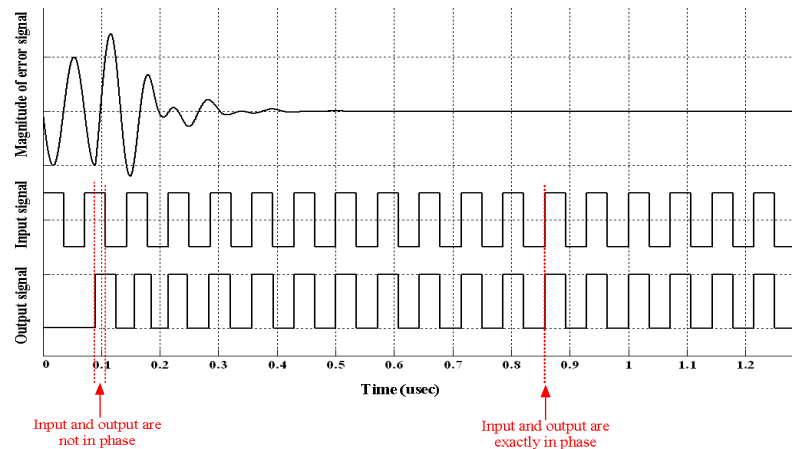


Figure 4 Transient waveforms of proposed all digital DLL to reach lock condition

Also, for a delay amount lower than $T/2$ DLL will not lock properly. The above explanations are the only limitations of DLLs lock range either in the circuit or system level design. It should be mentioned that in digital communication a processor should be used for example to choose different methods of modulations (Q-PSK, QAM,...) [27]. Hence, the delay is controlled by one of the outputs of this processor. In other words, no additional circuit is needed to control the delay of VCDL in the proposed structure. This means that the PFD and CP are eliminated in new architecture in comparison with conventional DLLs. Therefore, power consumption and area of proposed architecture will be lower than conventional DLLs.

4. CONCLUSIONS

A novel fast lock and high speed DLL-based frequency multiplier which has smaller area than conventional DLL is proposed in this paper. PRP conjugate gradient algorithm is used to control the delay of each delay cells in the VCDL. The output frequency is chosen as 210MHz to adopt with one of the Iran VHF band channels. To reach this goal, simulation has been done for 15 delay cells and $f_{REF}=14\text{MHz}$. Simulations show that output frequency is multiplied by 14 ($f_{OUT}=210\text{MHz}$), locking time is approximately 286nsec which is equal to 4 clock cycles of reference clock.

5. REFERENCES

- Mandal, A. and Mishra, R., "Design and implementation of digital demodulator for frequency modulated CW radar (research note)", *International Journal of Engineering-Transactions A: Basics*, Vol. 27, No. 10, (2014), 1581-1590.
- Gholami, M., Rahimpour, H., Ardeshir, G. and Miar-Naimi, H., "A new fast-lock, low-jitter, and all-digital frequency synthesizer for dvb-t receivers", *International Journal of Circuit Theory and Applications*, (2013).
- Gholami, M., Ardeshir, G. and Ghonoodi, H., "A novel architecture for low voltage-low power dll-based frequency multipliers", *IEICE Electronics Express*, Vol. 8, No. 11, (2011), 859-865.
- Moallem, P. and Ehsanpour, M., "A novel design of reversible multiplier circuit", *International Journal of Engineering*, Vol. 26, No. 6, (2013), 577-586.
- Coban, A.L., Koroglu, M.H. and Ahmed, K.A., "A 2.5-3.125-gb/s quad transceiver with second-order analog dll-based cdrs", *Solid-State Circuits, IEEE Journal of*, Vol. 40, No. 9, (2005), 1940-1947.
- Yun, W.-J., Lee, H.-W., Shin, D. and Kim, S., "A 3.57 gb/s/pin low jitter all-digital dll with dual dcc circuit for GDDR3 dram in 54-nm cmos technology", *Very Large Scale Integration (VLSI) Systems, IEEE Transactions on*, Vol. 19, No. 9, (2011), 1718-1722.
- Kim, N.-S., Cho, U.-R. and Byun, H.-G., "Low voltage wide range dll-based quad-phase core clock generator for high speed network sram application", in Custom Integrated Circuits Conference, 2005. Proceedings of the IEEE 2005, IEEE, (2005), 533-536.
- Gao, X., Klumperink, E.A. and Nauta, B., "Advantages of shift registers over dlls for flexible low jitter multiphase clock generation", *Circuits and Systems II: Express Briefs, IEEE Transactions on*, Vol. 55, No. 3, (2008), 244-248.
- Oh, K.-I., Kim, L.-S., Park, K.-I., Jun, Y.-H. and Kim, K., "Low-jitter multi-phase digital dll with closest edge selection scheme for ddr memory interface", *Electronics Letters*, Vol. 44, No. 19, (2008), 1121-1123.
- Gholami, M. and G. Ardeshir, "Dual phase detector based delay locked loop for high speed applications", *International Journal of Engineering-Transactions A: Basics*, Vol. 27, No. 4, (2014), 517-522.
- Gholami, M., Rahimpour, H., Ardeshir, G. and Miar-Naimi, H., "Digital delay locked loop-based frequency synthesiser for digital video broadcasting-terrestrial receivers", *IET Circuits, Devices & Systems*, Vol. 8, No. 1, (2014), 38-46.
- Rahimpour, H., Gholami, M., Miar-Naimi, H. and Ardeshir, G., "All digital fast lock dll-based frequency multiplier", *Analog*

- Integrated Circuits and Signal Processing*, Vol. 78, No. 3, (2014), 819-826.
13. Liao, F.-R. and Lu, S.-S., "A waveform-dependent phase-noise analysis for edge-combining DLL frequency multipliers", *Microwave Theory and Techniques, IEEE Transactions on*, Vol. 60, No. 4, (2012), 1086-1096.
 14. Gholami, M. and Ardeshir, G., "Jitter of delay-locked loops due to pfd", (2014).
 15. Shin, D., Song, J., Chae, H. and Kim, C., "A 7 ps jitter 0.053 mm fast lock all-digital DLL with a wide range and high resolution dcc", *Solid-State Circuits, IEEE Journal of*, Vol. 44, No. 9, (2009), 2437-2451.
 16. Cheng, K.-H. and Lo, Y.-L., "A fast-lock wide-range delay-locked loop using frequency-range selector for multiphase clock generator", *Circuits and Systems II: Express Briefs, IEEE Transactions on*, Vol. 54, No. 7, (2007), 561-565.
 17. Gholami, M., "A novel low power architecture for DLL-based frequency synthesizers", *Circuits, Systems, and Signal Processing*, Vol. 32, No. 2, (2013), 781-801.
 18. Y. Moon, D.-K. Jeong, G. Ahn and . "A 0.6-2.5-gbaud cmos tracked oversampling 3x transceiver with dead-zone phase detection for robust clock/data recovery", *IEEE Journal of Solid-State Circuits*, Vol. 36, No. 1974-1983.
 19. Cauchy, A., "Méthode générale pour la resolution des systemes d'equations simultanées", *Comp. Rend. Sci. Paris*, Vol. 25, No. 1847, (1847), 536-538.
 20. Akaike, H., "On a successive transformation of probability distribution and its application to the analysis of the optimum gradient method", *Annals of the Institute of Statistical Mathematics*, Vol. 11, No. 1, (1959), 1-16.
 21. Forsythe, G.E., "On the asymptotic directions of these-dimensional optimum gradient method", *Numerische Mathematik*, Vol. 11, No. 1, (1968), 57-76.
 22. Dai, Y.-H. and Yuan, Y., "A nonlinear conjugate gradient method with a strong global convergence property", *SIAM Journal on Optimization*, Vol. 10, No. 1, (1999), 177-182.
 23. Li, G., Tang, C. and Wei, Z., "New conjugacy condition and related new conjugate gradient methods for unconstrained optimization", *Journal of Computational and Applied Mathematics*, Vol. 202, No. 2, (2007), 523-539.
 24. Wei, Z.X., Li, G.Y. and Qi, L.Q., "Global convergence of the polak-ribiere-polyak conjugate gradient method with an armijo-type inexact line search for nonconvex unconstrained optimization problems", *Mathematics of Computation*, Vol. 77, No. 264, (2008), 2173-2193.
 25. Yuan, G., "Modified nonlinear conjugate gradient methods with sufficient descent property for large-scale optimization problems", *Optimization Letters*, Vol. 3, No. 1, (2009), 11-21.
 26. Yu, G., Zhao, Y. and Wei, Z., "A descent nonlinear conjugate gradient method for large-scale unconstrained optimization", *Applied Mathematics and Computation*, Vol. 187, No. 2, (2007), 636-643.
 27. Kavalov, D. and Kalinin, V., "Neural network surface acoustic wave rf signal processor for digital modulation recognition", *Ultrasonics, Ferroelectrics, and Frequency Control, IEEE Transactions on*, Vol. 49, No. 9, (2002), 1280-1290.
 28. Chang, H.-H. and Liu, S.-I., "A wide-range and fast-locking all-digital cycle-controlled delay-locked loop", *Solid-State Circuits, IEEE Journal of*, Vol. 40, No. 3, (2005), 661-670.
 29. Yang, R.-J. and Liu, S.-I., "A 40-550 MHz harmonic-free all-digital delay-locked loop using a variable sar algorithm", *Solid-State Circuits, IEEE Journal of*, Vol. 42, No. 2, (2007), 361-373.

APPENDIX

To examine validation of Equation (14), the first two harmonics of the input signal are calculated. Differentiating of (11) with respect to μ , we have:

$$\frac{\partial J_{\mu}(t)}{\partial \mu} = \left(\frac{\partial}{\partial \mu} [A_1(\sin \omega(t - N\mu) - \sin \omega t) + A_2(\sin 2\omega(t - N\mu) - \sin 2\omega t)]^2 \right) \quad (\text{A-1})$$

This results in:

$$\begin{aligned} \frac{\partial J_{\mu}(t)}{\partial \mu} = & \left(\frac{\partial}{\partial \mu} [A_1^2(\sin^2 \omega(t - N\mu) + \sin^2 \omega t - 2 \sin \omega(t - N\mu) \sin \omega t) + A_2^2(\sin^2 2\omega(t - N\mu) + \sin^2 2\omega t - \right. \\ & \left. 2 \sin 2\omega(t - N\mu) \sin 2\omega t)] + 2A_1A_2(\sin \omega(t - N\mu) \sin 2\omega(t - N\mu) + \sin \omega t \sin 2\omega t - \sin \omega(t - N\mu) \sin 2\omega t - \right. \\ & \left. \sin \omega t \sin 2\omega(t - N\mu)) \right] \end{aligned} \quad (\text{A-2})$$

After applying a derivative operation to (A-2), we have:

$$\begin{aligned} \frac{\partial J_{\mu}(t)}{\partial \mu} = & (-2\omega NA_1^2[\sin \omega(t - N\mu) \cos \omega(t - N\mu) - \cos \omega(t - N\mu) \sin \omega t] - 2\omega NA_2^2[2 \sin 2\omega(t - N\mu) \cos 2\omega(t - \\ & N\mu) - 2 \cos 2\omega(t - N\mu) \sin 2\omega t] - 2\omega NA_1A_2[2 \sin \omega(t - N\mu) \cos 2\omega(t - N\mu) + \cos \omega(t - N\mu) \sin 2\omega(t - N\mu) - \\ & \cos \omega(t - N\mu) \sin 2\omega t - 2 \sin \omega t \cos 2\omega(t - N\mu)]) \end{aligned} \quad (\text{A-3})$$

Rearranging this equation as:

$$\frac{\partial J_{\mu}(t)}{\partial \mu} = (-2N\omega(A_1 \cos \omega(t - N\mu) + 2A_2 \cos 2\omega(t - N\mu)) \times (A_1 \sin \omega(t - N\mu) - A_1 \sin \omega t + A_2 \sin 2\omega(t - N\mu) - A_2 \sin 2\omega t)) \quad (\text{A-4})$$

We have:

$$\omega(A_1 \cos \omega(t - N\mu) + 2A_2 \cos 2\omega(t - N\mu)) = \frac{\partial V_o(t)}{\partial t} \quad (\text{A-5})$$

And:

$$A_1 \sin \omega(t - N\mu) - A_1 \sin \omega t + A_2 \sin 2\omega(t - N\mu) - A_2 \sin 2\omega t = V_o(t) - V_i(t) \quad (\text{A-6})$$

Substituting Equation (A-6) and (A-5) into (A-4), we obtain:

$$\frac{\partial J_\mu(t)}{\partial \mu} = \left[-2N \frac{\partial V_o(t)}{\partial t} [V_o(t) - V_i(t)] \right] \quad (\text{A-7})$$

The above equation is the same as (14). Therefore, Equation (14) has been proved for first two harmonics of Equation (7). Also, the same procedure can be applied to higher harmonics of the input signal to validate (14) for all harmonics.

Low Settling Time All Digital DLL for VHF Application

H. Rahimpour^a, M. Gholami^b, G. Ardeshir^c, H. MiarNaimi^c

^aDepartment of Electrical Engineering, University of Tehran

^bDepartment of Electrical and Electronic Engineering, University of Mazandaran

^cDepartment of Electrical and Computer Engineering, BabolNoshirvani University of Technology

PAPER INFO

چکیده

Paper history:

Received 20May 2013

Received in revised form 17May 2014

Accepted 18November 2014

Keywords:

DLL, Delay Locked Loop

PRP Conjugate Gradient

Algorithm

Synthesizer

حلقه‌های قفل شده تاخیر (DLL) و حلقه‌های قفل شده فاز (PLL) به طور گسترده‌ای به عنوان سترکننده‌های فرکانسی و مدارهای بازیابی کلاک و داده در سیستم‌های مخابراتی مورد استفاده قرار می‌گیرند. در این مقاله، یک DLL جدید مبتنی بر الگوریتم‌گرادیان مزدوج PRP طراحی شده است. ساختار ارائه شده، به آشکارساز فاز-فرکانس، پمپ بار و فیلتر حلقه نیاز ندارد، بنابراین می‌تواند عملکرد بهتری از لحاظ جیتر و سرعت نسبت به ساختار متداول حلقه‌های قفل شده تاخیر داشته باشد. در این ساختار، الگوریتم‌گرادیان مزدوج PRP جهت بهینه کردن تأخیر هر سلول تاخیر مورد استفاده قرار گرفته است که این موضوع به قفل دقیق‌تر و سریع‌تر نسبت به الگوریتم‌بهینه‌سازی‌گرادیان متبهمی می‌شود. علاوه بر این، جهت استفاده از الگوریتم‌گرادیان مزدوج PRP به یک بخش پردازش دیجیتال نیاز است. برای نشان دادن دقت این ساختار، شبیه‌سازی برای ۱۵ سلول تاخیر با انتخاب فرکانس ورودی ۱۴ مگاهرتز جهت دریافت فرکانس خروجی ۲۱۰ مگاهرتز انجام گرفته است. فرکانس خروجی ۲۱۰ مگاهرتز، یکی از کانال‌های موجود در باند فرکانسی VHF ایران است. همانگونه که در شبیه‌سازی‌ها نشان داده شده است، ساختار پیشنهادی زمان قفلی در حدود ۲۸۶ نانوثانیه داشته که این معادل با ۴ سیکل کلاک ورودی است.

.doi: 10.5829/idosi.ije.2014.28.03c.11